

Supplementary material: Nomenclature

Roman symbols

C_d	drag coefficient (-)
C_n	mesh cell (-)
d_p	particle diameter (m)
e_c	particle-particle normal restitution coefficient (-)
f	force (N)
g	gravitational acceleration vector ($\text{m} \cdot \text{s}^{-2}$)
g_0	radial distribution function (-)
$I_{g \rightarrow p}$	Interphase momentum transfer ($\text{kg} \cdot \text{m}^{-2} \cdot \text{s}^{-2}$)
K	diffusivity ($\text{m}^2 \cdot \text{s}^{-1}$)
k_n	spring stiffness ($\text{N} \cdot \text{m}^{-1}$)
m_p	particle mass ($\text{kg} \cdot \text{m}^{-3}$)
n_p	particle density (m^{-3})
P	pressure ($\text{N} \cdot \text{m}^{-2}$)
q_p^2	kinetic energy of particle agitation ($\text{m}^2 \cdot \text{s}^{-2}$)
\mathbf{R}	particle velocity covariance ($\text{m}^2 \cdot \text{s}^{-2}$)
R_c	cylinder radius (m)
Re_p	particle Reynolds number (-)
\mathbf{S}	rate of deformation tensor (s^{-1})
T_c	collision time (s)
t	time (s)
\mathbf{u}	velocity vector ($\text{m} \cdot \text{s}^{-1}$)
V_p	particle volume (m^3)
V_f	fluidisation velocity ($\text{m} \cdot \text{s}^{-1}$)
\check{r}_w	normalised distance to the wall (-)

Greek symbols

α	volume fraction (-)
α_p^{\max}	close-packing limit (-)
α_p^{\min}	frictional-pressure activation threshold (-)
γ_n	spring damping coefficient (s^{-2})
η	dynamic viscosity ($\text{kg} \cdot \text{m}^{-1} \cdot \text{s}^{-1}$)
μ	coefficient of friction (-)
ν	kinematic viscosity (m^{-2}/s)
ρ	density ($\text{kg} \cdot \text{m}^{-3}$)
Σ	stress tensor ($\text{kg} \cdot \text{m}^{-1} \cdot \text{s}^{-2}$)
τ_p^c	collisional timescale (s)
τ_{gp}	mean gas-particle relaxation timescale (s)

Subscripts

g	gas
p	particle
w	wall

Superscripts

cnt	contact (collisional-frictional)
col	collisional
fr	frictional

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kin kinetic
kin-col kinetic-collisional
tot total