Supplemental Material for Manuscript: Salience and Social Choice

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- 1. Algebraic Calculations for SWUP demonstrating the predictions for the basic specification

We apply the basic specification of SWUP to explain eight behavioral patterns:

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Basic Specification of SWUP

To focus on the role of the salience functions in driving our results, we set w(x) = x in our analysis. We illustrate SWUP using the basic salience function from the main text, reproduced below, when it is not the case that both arguments of the function are zero, and $\mu(0,0) = \phi(0,0) = 0$.

$$\mu(x, y) = \frac{|x - y|}{|x| + |y|}, \qquad \varphi(n, m) = \frac{|n - m|}{n + m}$$

SWUP formula for Social Choice: Allocation A is chosen over Allocation B if and only if (A.1) holds: A.1 $\rho(A, B) = \sum_{j} \left[\phi(n_{j}, m_{j})(n_{j} - m_{j}) \left(\frac{w(x_{j}) + w(y_{j})}{2} \right) + \mu(x_{j}, y_{j})(w(x_{j}) - w(y_{j})) \left(\frac{n_{j} + m_{j}}{2} \right) \right] \ge 0.$ Substituting in the basic salience functions, and setting w(x) = x for all x, A.1 becomes A.2:

A.2.
$$\rho(A, B) = \sum_{j} \left[\frac{(n_j - m_j)|n_j - m_j|}{n_j + m_j} \right] \left(\frac{x_j + y_j}{2} \right) + \left[\frac{(x_j - y_j)|x_j - y_j|}{x_j + y_j} \right] \left(\frac{n_j + m_j}{2} \right) \ge 0.$$

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1.1. Demonstration that SWUP predicts the Common Consequence Effect in Social Choice

The common consequence choice pairs from the experiment are reproduced below:

Common Consequence Pair 1

A) 5 people receive \$3, 4 people receive \$3, and 1 other person receives \$3

B) 5 people receive \$5, 4 people receive \$3, and 1 other person receives \$0

Common Consequence Pair 2

A) 6 people receive \$3 and the other 4 people receive \$0

B) 5 people receive \$5 and the other 5 people receive \$0

The SWUP model predicts the majority choices from the experiment: A in Pair 1 and B in Pair 2. Applying A.1, SWUP predicts that allocation A is chosen over allocation B if the following inequality holds:

$$\mu(3,5)(3-5)(5) + \mu(3,0)(3-0)(1) > 0.$$

Applying A.2, allocation A is chosen over B for the basic salience function since -(20/8) + 3 > 0.

In addition, SWUP predicts that B is chosen over A in Common Consequence Pair 2 if

$$\frac{\mu(3,5)(3-5)(6+5)}{2} + \frac{\phi(6,5)(6-5)(3+5)}{2} < 0.$$

Applying A.2, allocation B is chosen over A for the basic salience function since $\left(-\frac{44}{16}\right) + \left(\frac{8}{22}\right) < 0$.

1.2. Demonstration that SWUP predicts the Common Ratio Effect in Social Choice

The common ratio choice pairs from the experiment are reproduced below:

Common Ratio Pair 1

B) 5 people receive \$5 and the other 5 people receive \$0

Common Ratio Pair 2

A) 2 people receive \$2 and the other 8 people receive \$0

B) 1 person receives \$5 and the other 9 people receive \$0

The SWUP model predicts the majority choices from the experiment: A in Pair 1 and B in Pair 2. Applying A.1, SWUP predicts that allocation A is chosen over allocation B if the following inequality holds:

$$\mu(2,5)(-3)(5) + \mu(2,0)(2)(5) > 0.$$

Applying A.2, allocation A is chosen over B for the basic salience function since $\left(\frac{-45}{7}\right) + 10 > 0$.

In addition, SWUP predicts that B is chosen over A in Common Ratio Pair 2 if

$$\frac{\mu(2,5)(-3)(2+1)}{2} + \frac{\phi(2,1)(1)(2+5)}{2} < 0.$$

Applying A.2, allocation B is chosen over A for the basic salience function since $\left(\frac{-27}{14}\right) + \left(\frac{7}{6}\right) < 0$.

1.3. Demonstration that SWUP predicts a Magnitude Effect in Social Choice

The choice pairs investigating scale invariance from the experiment are reproduced below:

Magnitude Effect Pair 1

A)	1	person	receives	\$5	and	the	other	9	peo	ple	receiv	e \$	\$5
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B) 1 person receives \$50 and the other 9 people receive \$0

Magnitude Effect Pair 2

A) 1 person receives \$0.25 and the other 9 people receive \$0.25

B) 1 person receives \$2.50 and the other 9 people receive \$0

The basic SWUP specification predicts the majority choices in the experiment: A in Pair 1 and A in Pair 2: Applying A.1, SWUP predicts that allocation A is chosen over B if the following inequality holds:

$$\mu(5,50)(-45)(1) + \mu(5,0)(5)(9) > 0$$

Applying A.2, allocation A is chosen in Pair 1 for the basic salience function since $-\frac{2025}{55} + 45 > 0$.

In addition, the basic specification of SWUP predicts that A is chosen over B in Pair 2 if

$$\mu(0.25, 2.50)(-2.25)(1) + \mu(0.25, 0)(0.25)(9) > 0.$$

Applying A.2, allocation A is chosen in Pair 2 for the basic salience function since $-\frac{5.0625}{2.75} + 2.25 > 0$.

Bordalo et al. (2013) apply the basic salience function to consumer choice. Bordalo et al. (2012) employ the following salience function for payoffs in their salience model of choice under risk, where $\theta > 0$:

$$\mu(\mathbf{x}, \mathbf{y}) = \frac{|\mathbf{x}-\mathbf{y}|}{|\mathbf{x}|+|\mathbf{y}|+\theta}$$

The predictions of SWUP for the common consequence, common ratio, skewness, and framing effect pairs are robust to whether $\theta = 0$ (as in the basic specification we use) or whether $\theta > 0$ for the payoff salience function μ (for instance, they each hold for $\theta = 1$). For the test of scale invariance, the predictions of SWUP differ depending on whether $\theta = 0$ or whether $\theta = 1$. For instance, if the payoff salience function has the form from Bordalo et al. (2012) with $\theta = 1$, then the analysis changes as follows:

Applying A.2, allocation A is chosen in Pair 1 since $-\frac{2025}{56} + \left(\frac{225}{6}\right) > 0$.

Applying A.2, allocation B is chosen in Pair 2 since $-\frac{5.0625}{3.75} + \left(\frac{0.5625}{1.25}\right) < 0.$

1.4. Demonstration that SWUP predicts a Preference for Tail-increasing Transfers

The 'tail-increasing transfers' choice pairs from the experiment are reproduced below:

Tail-increasing Transfers: Pair 1 (Top panel) and Pair 2 (Bottom panel)

A) 7 people receive \$12 and the other 3 people receive \$11

B) 7 people receive \$16 and the other 3 people receive \$6

A) 7 people receive \$12 and the other 3 people receive \$11

B) 7 people receive \$10 and the other 3 people receive \$20

The SWUP model predicts the majority choices from the experiment: A in Pair 1 and B in Pair 2. Applying A.1, SWUP predicts that allocation A is chosen over allocation B in Pair 1 if the following inequality holds:

 $\mu(12,16)(-4)(7) + \mu(11,6)(5)(3) > 0.$

Applying A.2, allocation A is chosen over B in Pair 1 for the basic salience function since $-\frac{112}{28} + \frac{75}{17} > 0$. In addition, SWUP predicts that B is chosen over A in Pair 2 if

$$\mu(12,10)(2)(7) + \mu(11,20)(-9)(3) < 0.$$

Applying A.2, allocation B is chosen over A in Pair 2 for the basic salience function since $\frac{28}{22} - \frac{243}{31} < 0$.

1.5. Demonstration that SWUP predicts the Alignment Framing Effect in Social Choice The framing effect choice pairs from the experiment are reproduced below:

Alignment Framing Effect Pair 1

A) 2 people receive \$5, 2 others receive \$5, 4 others receive \$0, and 2 others receive \$12

B) 2 people receive \$0, 2 others receive \$13, 4 others receive \$5, and 2 others receive \$0

Alignment Framing Effect Pair 2

A) 2 people receive \$0, 2 others receive \$0, 4 others receive \$5, and 2 others receive \$12

B) 2 people receive \$0, 2 others receive \$0, 4 others receive \$5, and 2 others receive \$13

For the alignment framing effect pairs, SWUP predicts that A is chosen over B in Pair 1 if:

$$\mu(5,0)(5)(2) + \mu(5,13)(-8)(2) + \mu(0,5)(-5)(4) + \mu(12,0)(12)(2) > 0.$$

Applying A.2, A is chosen over B in Pair 1 for the basic salience function since $10 - \frac{128}{18} - 20 + 24 > 0$.

For the alignment framing effect pairs, SWUP predicts that B is chosen over A in Pair 2 if:

$$\mu(12,13)(-1)(2) < 0.$$

Allocation B is chosen over A in Pair 2 for all salience functions since salience functions are non-negative (e.g., as in Definition 2 in Section 4.1 of the main text).

1.6. Demonstration that SWUP can explain a preference for lower inequality

The choice pairs from Figure 5 of the main text are reproduced below:

Preference for Lower Inequality					Pref	Preference for Higher Efficiency							
	\$	Ν	\$	Ν		\$	Ν	\$	Ν	\$	Ν		
Α	5	1	5	1	А	10	1	8	1	1	1		
В	10	1	0	1	В	16	1	8	1	5	1		

Preference for Minimizing Inequality and Maximizing Efficiency

For the example of inequality aversion in the left panel in Figure 5, SWUP predicts that allocation A is chosen over B if the following inequality holds: $\mu(5,10)(-5) + \mu(5,0)(5) > 0$. This inequality holds for any salience function as a result of the properties of symmetry and diminishing sensitivity. In particular, by symmetry and diminishing sensitivity, $\mu(5,10) = \mu(10,5) = \mu(5 + \epsilon, 0 + \epsilon) < \mu(5,0)$.

1.7. Demonstration that SWUP can explain a preference for higher efficiency

For the example of a preference for efficiency in the right panel in Figure 5, SWUP predicts that allocation B is chosen over A if the following inequality holds: $\mu(10, 16)(-6)(1) + \mu(1,5)(-4)(1) < 0$. This inequality holds generally for all salience functions since salience functions are non-negative.

1.8. Demonstration that SWUP can explain the Medical Treatment Paradox

The example from Figure 6 of the main text is reproduced below:

	Health	Ν	Health	Ν
Treatment 1	1	48	0.91	27
Treatment 2	1	27	0.95	48

Observed deviation from Inequity Aversion, Rawls and Utilitarianism

For the medical treatment example in Figure 6, SWUP predicts that Treatment 1 is chosen over Treatment 2 if the following inequality holds:

 $\phi(48,27)(21) + \mu(0.91,0.95)(-0.04)(37.5) + \phi(27,48)(-21)(0.93) > 0.$

Applying A.2, Treatment 1 is chosen over Treatment 2 since $\frac{441}{75} - \frac{0.06}{1.86} - \frac{410.13}{75} > 0$.

2. Screen Shots from Experiment

Experimental subjects responded to the choices as presented below. Only one choice was displayed on a screen at any time. The order of choices and the option that appeared on the top or bottom row in each choice were both randomized within subjects. The labels in bold font above each screen shot were not shown to subjects. They are included below to facilitate comparison to the main text.

Instructions

In this experiment, you will be asked several questions. In each question, you will be given a choice between 2 different allocations of funds to be given to ten experiment participants in this room. Your choice may determine the payment of ten participants in this room but it will not determine your payment. Once all participants have completed the questions, one choice from a participant in the first or second row (the front two rows in this room) and one choice from a participant in the third or fourth row (the back two rows in this room) will be randomly selected. The choice from the person in the first or second row will determine the payment of the ten participants in the third and fourth rows. The choice from the person in the third or fourth row will determine the payment of the ten participants in the first and second rows.

All choices will be anonymous. No one will know the identity of the participants whose choices are randomly selected to determine payments.

The following is an example of the types of options you will consider:

- 1 person receives \$3 and the other 9 people receive \$7
- 1 person receives \$4 and the other 9 people receive \$6

It is important to emphasize there are no "right" answers to these questions. Please choose according to your own preferences. In addition to the payoff you receive from the selected allocation, you will also receive \$3 for completing the survey.

Common Consequence Pair 1

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

[©] 5 people receive \$5, 4 people receive \$3, and 1 other person receives \$0

5 people receive \$3, 4 people receive \$3, and 1 other person receives \$3

Common Consequence Pair 2

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

6 people receive \$3 and the other 4 people receive \$0

5 people receive \$5 and the other 5 people receive \$0

Common Ratio Pair 1

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

- 5 people receive \$2 and the other 5 people receive \$2
- 5 people receive \$5 and the other 5 people receive \$0

Common Ratio Pair 2

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

- 2 people receive \$2 and the other 8 people receive \$0
- 1 person receives \$5 and the other 9 people receive \$0

Magnitude Effect Pair 1

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

- 1 person receives \$0.25 and the other 9 people receive \$0.25
- 1 person receives \$2.50 and the other 9 people receive \$0

Magnitude Effect Pair 2

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

1 person receives \$50 and the other 9 people receive \$0

1 person receives \$5 and the other 9 people receive \$5

Skewness Effect Pair 1

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

- 7 people receive \$12 and the other 3 people receive \$11
- 7 people receive \$10 and the other 3 people receive \$20

Skewness Effect Pair 2

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

- 7 people receive \$12 and the other 3 people receive \$11
- 7 people receive \$16 and the other 3 people receive \$6

Alignment Framing Effect Pair 1

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

- 2 people receive \$5, 2 others receive \$5, 4 others receive \$0, 2 others receive \$12
- 2 people receive \$0, 2 others receive \$13, 4 others receive \$5, 2 others receive \$0

Alignment Framing Effect Pair 2

Please select the allocation of money below that you most prefer to be randomly distributed to ten people in this room (*not* including yourself)

2 people receive \$0, 2 others receive \$0, 4 others receive \$5, and 2 others receive \$13

2 people receive \$0, 2 others receive \$0, 4 others receive \$5, and 2 others receive \$12

Cognitive Reflection Test (Seven-question version from Toplak et al., 2014)

Please answer the following questions		
A bat and a ball cost \$1.10 in total. The bat cost	ts \$1.00 more than the ball. How much does	s the ball cost?
If it takes 5 machines 5 minutes to make 5 widg	ets, how long would it take 100 machines to	o make 100 widgets?
In a lake there is a patch of lily pads. Every day	, the patch doubles in size. If it takes 48 day	s for the patch to cover the entire lake, how
long would it take for the patch to cover half of	the take?	
If John can drink one barrel of water in 6 days	and Mary can drink one barrel of water in 1	2 days how long would it take them to drink
one barrel of water together?		
_		
Jerry received both the 15th highest and the 15t	h lowest mark in the class. How many stude	ents are in the class?
A man buys a pig for \$60, sells it for \$70, buys	it back for \$80, and sells it finally for \$90. I	How much has he made?
Circus desided to instant CO 0000 in the start	dest and des and in 2000 Circumster C	the innerted on Tabe 17 stands to take to
Simon decided to invest \$8,000 in the stock ma	rket one day early in 2008. Six months after	ne mvested, on July 17, the stocks he had he had nurchased went up 75%. At this point
Simon has:	ion, nom only 17 to October 17, the stocks f	at has porchased went up 7570. At this point,
broken even	gained money	lost money
0		