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> #Hello! This is a transcript of the cluster Latent Class Analysis performed to classify meta
1 findings into groups or clusters
> #Before this cluster analysis, many other ones were carried changing the variables
> #THE CLUSTERS OR LATENT CLASSES PRODUCED IN THIS PARTICULAR TRANSCRIPT ARE THE ONES
WHICH MAKE MORE SENSE ACCORDING TO THE AUTHOR, other possibilities exist *(see supplementary material 3)
>
> #Quick explanation: lines followed by a hashtag symbol # are clarifications with no function
al use, segments highlighted in yellow are lines of code with intructions to do the statistica
l analysis
>
> #The program employed to do the Latent Class Analysis is the open-source free software R Pro
gramming Environment for statistical computing
> #My thanks to my undergrad professor Manuel Dominguez-Rodrigo (Alcalá University) for introd
ucing me to this program
> #It is easy and free to use, the way it is employed here could potentially be used with virt
ually any archaeological database with sites and variables of any period and region of the wor
ld
> #To do the Latent Class Analysis the R package poLCA is employed, "poLCA" is an abbreviation
of "Polytomous Variable Latent Class Analysis"
> #poLCA was developed by professors Jeff Lewis (UCLA) and Drew A. Linzer (Emory University, S
tanford, now director at Civiqs) you can follow them in twitter
> #Check their paper "poLCA: An R Package for Polytomous Variable Latent Class Analysis" in th
e bibliography
> #There is a great video in youtube with a quick introduction to the poLCA package "https://w
ww.youtube.com/watch?v=LL6tio9V-Vw"
> #You can also watch a far more advanced youtube video to have a glimpse of the math behind th
e Latent Class Analysis "https://www.youtube.com/watch?v=rVfZHWTwXSA"
> #The R version used is the 4.1.2 (poLCA does not work in previous versions)
>
> #First we install the packages required to use poLCA in the R Programming Enviroment
> library(scatterplot3d)
> library(MASS)
> library(poLCA)
>
> #Now we insert a table called "bay_of_biscay_dataset" with all findings and their variables
> bay_of_biscay_dataset <- read.table(file.choose(), header = TRUE, row.names = 1)
>
> #We can ask R to show us an overview of the data inserted so we know it has been correctly i
nserted
> #The first column are the twenty variables, the second (int) indicates we are dealing with i
nteger values (no decimal numbers), the third and following columns with numbers are the findi
ngs studied
> #Each column of numbers is a metal finding defined by a sequence of numbers, for example two
early bronze age collective burials with flat axes will be defined by the same sequence of nu
mbers and so on
> #Each number in each variable means something different, for example number 1 in context mea
ns "hoard" and number 1 in artefact's columns (flat axes and so on) means "zero" (see figure 5
in the paper for the meaning of each number)
> str(bay_of_biscay_dataset)
'data.frame': 1273 obs. of 20 variables:
 $ context : int 1 1 1 1 1 1 1 1 1 1 ...
 $ chronology_terminus_post_quem : int 5 5 5 5 5 5 5 5 5 5 ...
 $ arrowheads : int 1 1 1 1 1 1 1 1 1 1 ...
 $ awls : int 1 1 1 1 1 1 1 1 1 1 ...
 $ bujoes_barcelos_axes : int 1 1 1 1 1 1 1 1 1 1 ...
 $ ch_eba_archaic_tanged_blades : int 1 1 1 1 1 1 1 1 1 1 ...
 $ eba_advanced_blades : int 1 1 1 1 1 1 1 1 1 1 ...
 $ chalcolithic_decorative_items : int 1 1 1 1 1 1 1 1 1 1 ...
 $ copper_bronze_bracelets : int 2 1 1 1 1 1 2 1 2 1 ...
 $ early_bronze_age_decorative_items : int 1 1 1 1 1 1 1 1 1 1 ...
 $ palstaves_or_flanged_axes_of_the_MBA : int 2 2 2 2 2 2 2 2 2 2 ...
 $ flat_axes : int 1 1 1 1 1 1 1 1 1 1 ...
 $ halberds : int 1 1 1 1 1 1 1 1 1 1 ...
 $ mba_archaic_short_riveted_blades : int 1 1 1 1 1 1 1 1 1 1 ...
 $ mba_advanced_short_riveted_blades : int 1 1 1 1 1 1 1 1 2 1 ...
 $ Atlantic_and_CE_long_riveted_blades : int 2 1 1 2 1 1 1 1 1 1 ...
 $ Iberian_long_riveted_blades_type_cuevallusa_emtrambasaguas : int 1 1 1 1 1 1 1 1 1 1 ...
 $ middle_bronze_age_decorative_items : int 1 1 1 2 1 1 1 1 1 1 ...
 $ palmela_points : int 1 1 1 1 1 1 1 1 1 1 ...
 $ spearheads : int 1 1 1 2 1 1 1 1 2 1 ...
>
> #Now we set the settings of the Latent Class Anlysis and we give them a name (here they are
named "alpha_lca")
> #The expression "cbind" tells R that we want to do a Latent Class Analysis with the variable

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s inside the parenthesis
> #The expression "~ 1" tells R that we want a normal Latent Class Analysis, other options are
available in poLCA
> alpha_lca <- cbind(context, chronology_terminus_post_quem, arrowheads, awls, bujoes_barcelos
axes, ch_eba_archaic_tanged_blades, eba_advanced_blades, chalcolithic_decorative_items, coppe
r_bronze_bracelets, early_bronze_age_decorative_items, palstaves_or_flanged_axes_of_the_MBA, f
lat_axes, halberds, mba_archaic_short_riveted_blades, mba_advanced_short_riveted_blades, Atlan
tic_and_CE_long_riveted_blades, Iberian_long_riveted_blades_type_cuevallusa_emtrambasaguas, mi
ddle_bronze_age_decorative_items, palmela_points, spearheads) ~ 1
>
> #Finally we can do the Latent Class Analysis
> #We name our analysis "lcal", the entities "alpha_lca" and "bay_of_biscay_dataset" were intr
duced above
> #It is important to add other settings to the analysis:
> #First: "nclass=5" indicates the number of Latent Classes or clusters to find, default is 2,
the number 5 is the result of running this code several times and deciding that 5 clusters is
what makes more sense
> #Second: "maxiter=100000" indicates the number of iterations, default is 1000, what are iter
ations?
> #Iterations are a complex concept, poLCA uses an EM algorithm to find the "best" clustering
solution (the one which makes more statistical sense) repeating iteratively two steps
> #The first step estimates class membership probabilities and in the second step these estima
tes are altered to maximise the likelihood function, each of these two steps is an iteration
> #Simplifying the more complex the dataset, the more iterations it requires
> #Third: "nrep=10" indicates the R program will do the anlysis ten times and give you the "be
st" result
> #Fourth: "verbose=TRUE" indicates we want a written report of the analysis (the different pa
rts of the report are explained below after the report)
> #Fifth: "graph=False" indicates we don't want a visual representation of the results (it doe
s not look very well as we are using many variables, it looks great with up until 8 variables)
> lcal <- poLCA (alpha_lca, bay_of_biscay_dataset, nclass=5, maxiter=100000, nrep=10, verbose=
TRUE, graph=FALSE)
Model 1: llik = -4518.546 ... best llik = -4518.546
Model 2: llik = -4525.805 ... best llik = -4518.546
Model 3: llik = -4970.385 ... best llik = -4518.546
Model 4: llik = -4738.961 ... best llik = -4518.546
Model 5: llik = -4562.286 ... best llik = -4518.546
Model 6: llik = -4698.385 ... best llik = -4518.546
Model 7: llik = -5132.365 ... best llik = -4518.546
Model 8: llik = -4758.127 ... best llik = -4518.546
Model 9: llik = -5235.504 ... best llik = -4518.546
Model 10: llik = -4654.659 ... best llik = -4518.546
Conditional item response (column) probabilities,
by outcome variable, for each class (row)

$context
      Pr(1) Pr(2) Pr(3) Pr(4) Pr(5)
class 1: 0.9055 0.0000 0.0945 0.0000 0.0000
class 2: 0.3317 0.5829 0.0000 0.0854 0.0000
class 3: 0.4252 0.0070 0.4977 0.0000 0.0701
class 4: 0.9659 0.0000 0.0161 0.0000 0.0179
class 5: 1.0000 0.0000 0.0000 0.0000 0.0000

$chronology_terminus_post_quem
      Pr(1) Pr(2) Pr(3) Pr(4) Pr(5)
class 1: 0.0000 0.0000 0 1.0000 0
class 2: 0.0000 0.0000 1 0.0000 0
class 3: 1.0000 0.0000 0 0.0000 0
class 4: 0.0000 0.0000 0 0.0000 1
class 5: 0.0012 0.8379 0 0.1609 0

$arrowheads
      Pr(1) Pr(2)
class 1: 0.7166 0.2834
class 2: 0.9950 0.0050
class 3: 1.0000 0.0000
class 4: 0.9964 0.0036
class 5: 1.0000 0.0000

$awls
      Pr(1) Pr(2)
class 1: 0.9685 0.0315
class 2: 0.9799 0.0201
class 3: 0.8037 0.1963

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class 4: 0.9982 0.0018
class 5: 1.0000 0.0000
```

```
$bujoes_barcelos_axes
      Pr(1) Pr(2)
class 1: 0.4227 0.5773
class 2: 1.0000 0.0000
class 3: 1.0000 0.0000
class 4: 0.9964 0.0036
class 5: 1.0000 0.0000
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```
$sch_eba_archaic_tanged_blades
      Pr(1) Pr(2)
class 1: 0.9790 0.0210
class 2: 1.0000 0.0000
class 3: 0.7827 0.2173
class 4: 0.9982 0.0018
class 5: 1.0000 0.0000
```

```
$seba_advanced_blades
      Pr(1) Pr(2)
class 1: 0.9895 0.0105
class 2: 0.4422 0.5578
class 3: 1.0000 0.0000
class 4: 1.0000 0.0000
class 5: 0.9964 0.0036
```

```
$schalcolithic_decorative_items
      Pr(1) Pr(2)
class 1: 1.0000 0.0000
class 2: 0.9950 0.0050
class 3: 0.7266 0.2734
class 4: 1.0000 0.0000
class 5: 1.0000 0.0000
```

```
$copper_bronze_bracelets
      Pr(1) Pr(2)
class 1: 1.0000 0.0000
class 2: 1.0000 0.0000
class 3: 1.0000 0.0000
class 4: 0.9032 0.0968
class 5: 1.0000 0.0000
```

```
$searly_bronze_age_decorative_items
      Pr(1) Pr(2)
class 1: 1.0000 0.0000
class 2: 0.7538 0.2462
class 3: 0.9790 0.0210
class 4: 1.0000 0.0000
class 5: 1.0000 0.0000
```

```
$spalstaves_or_flanged_axes_of_the_MBA
      Pr(1) Pr(2)
class 1: 1.0000 0.0000
class 2: 1.0000 0.0000
class 3: 1.0000 0.0000
class 4: 0.1792 0.8208
class 5: 0.9964 0.0036
```

```
$flat_axes
      Pr(1) Pr(2)
class 1: 0.9867 0.0133
class 2: 0.8643 0.1357
class 3: 0.8551 0.1449
class 4: 1.0000 0.0000
class 5: 0.0000 1.0000
```

```
$shalberds
      Pr(1) Pr(2)
class 1: 0.9895 0.0105
class 2: 0.7889 0.2111
class 3: 1.0000 0.0000
class 4: 1.0000 0.0000
class 5: 1.0000 0.0000
```

\$mba_archaic_short_riveted_blades

	Pr(1)	Pr(2)
class 1:	0.9265	0.0735
class 2:	0.9950	0.0050
class 3:	1.0000	0.0000
class 4:	0.9946	0.0054
class 5:	1.0000	0.0000

\$mba_advanced_short_riveted_blades

	Pr(1)	Pr(2)
class 1:	1.0000	0.0000
class 2:	1.0000	0.0000
class 3:	1.0000	0.0000
class 4:	0.9767	0.0233
class 5:	1.0000	0.0000

\$Atlantic_and_CE_long_riveted_blades

	Pr(1)	Pr(2)
class 1:	1.0000	0.0000
class 2:	1.0000	0.0000
class 3:	1.0000	0.0000
class 4:	0.9158	0.0842
class 5:	1.0000	0.0000

\$Iberian_long_riveted_blades_type_cuevallusa_emtrambasaguas

	Pr(1)	Pr(2)
class 1:	0.9160	0.0840
class 2:	1.0000	0.0000
class 3:	1.0000	0.0000
class 4:	0.9982	0.0018
class 5:	1.0000	0.0000

\$middle_bronze_age_decorative_items

	Pr(1)	Pr(2)
class 1:	1.0000	0.0000
class 2:	1.0000	0.0000
class 3:	1.0000	0.0000
class 4:	0.9624	0.0376
class 5:	1.0000	0.0000

\$palmela_points

	Pr(1)	Pr(2)
class 1:	0.9895	0.0105
class 2:	0.9347	0.0653
class 3:	0.6706	0.3294
class 4:	1.0000	0.0000
class 5:	0.9964	0.0036

\$spearheads

	Pr(1)	Pr(2)
class 1:	1.0000	0.0000
class 2:	1.0000	0.0000
class 3:	1.0000	0.0000
class 4:	0.9014	0.0986
class 5:	1.0000	0.0000

Estimated class population shares

0.0748 0.1563 0.1121 0.4383 0.2184

Predicted class memberships (by modal posterior prob.)

0.0746 0.1563 0.1123 0.4383 0.2184

=====
Fit for 5 latent classes:
=====

number of observations: 1273
number of estimated parameters: 134
residual degrees of freedom: 1139
maximum log-likelihood: -4518.546

AIC(5): 9305.092
BIC(5): 9995.076
G²(5): 1557.962 (Likelihood ratio/deviance statistic)

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X^2(5): 2802874110 (Chi-square goodness of fit)
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> #Don't be intimidated by the all the numbers above (see page 12 of the paper "poLCA: An R Pa
ckage for Polytomous Variable Latent Class Analysis" in the bibliography for a complete explan
ation
> #There are three main things we must pay attention to: degrees of freedom, the tables that o
ccupy most of the results of the analysis and the BIC value at the end
>
> #Degrees of freedom is the result of a complex relation between the number of subjects studi
ed and the number of variables (see page 636 of the 2019 book "Multivariate data analysis: Eig
hth edition" by Joseph Hair for an excellent and complete definition)
> #Oversimplifying, the number of subjects studied must be larger than the variables analysed,
it is a way to avoid the researcher to study datasets with a few entities and many variables
which does not make sense
> #If there is a problem with the degrees of freedom the R program will say "ALERT: negative d
egrees of freedom; respecify model", only models with positive degrees of freedom should be co
nsidered
>
> #The tables that occupy most of the results of the Latent Class Analysis tell us important i
nformation about the groups or clusters (the label "latent classes" is more precise) created
> #Each table refers to one of the twenty variables studied (chronology, context and each of t
he eighteen artefact categories in the analysis)
> #Each table has rows with five classes (class 1 to 5), each class is one of our latent class
es or clusters or groups of metal findings
> #Each table also has columns, each column refers to one of the values of the variable, for e
xample chronology has five (1=Chalcolithic, 2=Chalcolithic-Early Bronze Age, and so on, see fi
gure 2 in the paper for the rest)
> #Each table has decimal numbers which are actually a %, we have to mentally multiply by 100
to have the %, for example 0.5625 is 56.25%
> #The percentage expresses the possibility a metal finding classified in one of the five clas
ses or clusters has a particular value
> #For example if a class has a value of 1 (i.e., 100%) it means that ALL its members have tha
t value, conversely a value of 56.25% indicates the percentage the members of the class may ha
ve that value
> #For example, if in the table "$flat_axes" a class has a value of 1, it means that 100% of
its findings contain flat axes
> #More important, if in the table "$context" the same class has a value of for example 96.59%
, it means that virtually all its findings are hoards
> #This shows that there are many hoards with flat axes that the Latent Class Analysis has dec
ided to group together into a class or cluster
> #Simplifying, patterns like this one in the dataset are used by poLCA to group similar findi
ngs into homogenous latent classes or clusters with homogenous features (chronology, content,
context)
>
> #At the end of the results there are four values, BIC (Bayesian Information Criterion) among
others (AIC, G^2, X^2), that are also important
> #They can be used to compare different Latent Classes Analyses, Latent Classes Analyses coul
d differ for example (and very importantly) in the number of latent classes or clusters we ask
them to find (here 5)
> #As we vary the Latent Class Analysis to study the same dataset, the four previous measures
(BIC being the most used one in the literature) also change
> #The values of these four measures can help us decide which Latent Class Analysis creates a
"better" model
> #In the case of BIC, if we compare several Latent Class Analyses of the same dataset, the on
e with a lower BIC is statistically speaking the one with the "best" results
> #In this study the author has followed another philosophy focusing not in these four measure
s but in which Latent Class Anlysis produces a result that makes more sense
> #Weller (see Weller et al. 2020 page 292 in the bibliography) has synthesised this "philosph
y" in the sentence "A class solution with superior statistics is not useful if it makes no sen
se theoretically"
> #The Latent Class Analysis with 5 latent classes in this transcript is the one which accordi
ng to the author made more sense and was therefore superior to the others
>
> #AFTER THIS LONG EXPLANATION WE FOCUS ON THE RESULTS OF THE LATENT CLASS ANALYSIS
>
> #To see the results, we can create a table named "lca_final" in which each finding in the st
udy and their assigned cluster appear in two columns (one for findings and other for the assign
ed cluster)
> #Clusters, which should be actually called latent classes, appear as numbers from 1 to 5
> #We also ask R to name the column with the findings "findings_id" and the column with the la
tent classes (or "clusters") "latent_class"
> #With the command below the table is created but R does not show it to us, it is a long tabl
e with 1273 rows each corresponding to a find
> lca_final <- data.frame(findings_id=row.names(bay_of_biscay_dataset),latent_class=lca1$predc
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lass)
>
> #We can ask R to see the first seven rows just to see how the table with the results looks like
> #The column to the left numbered from 1 to 7 is automatically created by the program R to name each row
> head(lca_final, 7)
  findings_id latent_class
1           877           4
2          1030           4
3           353           4
4           836           4
5          1163           4
6            44           4
7           838           4
>
> #We can export this table to an excel (.csv) document in the following way
> #The expression "row.names=FALSE" eliminates the numbers in the column to the left naming each row
> write.csv(lca_final, file.choose(), row.names=FALSE)
>
> #Before this transcript finishes I show the entire final table with each finding id and its corresponding assigned latent class or cluster
> #Remember each of the 5 clusters or latent classes is represented by a number from 1 to 5, each row is a metal findings
> #This transcript ends with the table below, live long and prosper
> lca_final
  findings_id latent_class
1           877           4
2          1030           4
3           353           4
4           836           4
5          1163           4
6            44           4
7           838           4
8            106           4
9             83           4
10           576           4
11           651           4
12           144           4
13          1322           4
14          1150           4
15           754           4
16           983           4
17           897           4
18            15           4
19           462           4
20           693           3
21          1016           4
22           469           4
23           360           5
24           366           4
25           368           4
26           369           1
27           365           4
28           371           4
29           363           3
30           367           4
31           359           2
32           358           5
33           357           4
34           356           4
35           354           4
36           351           5
37           350           4
38           349           1
39           347           5
40           346           4
41           345           2
42           344           4
43           343           1
44           355           4
45           400           5
46           374           4

```

47	393	5
48	395	4
49	396	4
50	397	4
51	390	2
52	399	3
53	389	2
54	401	5
55	402	4
56	403	4
57	404	1
58	405	2
59	406	4
60	398	4
61	381	2
62	373	4
63	375	5
64	338	4
65	376	4
66	377	2
67	391	4
68	379	2
69	372	2
70	383	3
71	384	2
72	385	5
73	386	5
74	387	5
75	388	2
76	378	5
77	300	2
78	307	4
79	294	4
80	295	5
81	296	4
82	297	4
83	292	2
84	299	2
85	291	5
86	301	5
87	302	4
88	303	4
89	304	4
90	305	3
91	340	4
92	298	5
93	283	5
94	275	2
95	276	4
96	278	5
97	279	4
98	280	4
99	293	3
100	282	3
101	308	4
102	284	5
103	286	4
104	287	2
105	288	2
106	289	4
107	290	4
108	281	5
109	334	2
110	306	4
111	328	4
112	329	2
113	330	2
114	331	4
115	325	5
116	333	4
117	324	4
118	336	4
119	337	1
120	415	2

121	339	3
122	407	2
123	341	2
124	332	4
125	317	2
126	309	2
127	310	2
128	312	4
129	313	2
130	314	2
131	326	2
132	316	4
133	342	2
134	318	3
135	319	4
136	320	4
137	321	4
138	322	5
139	323	4
140	315	4
141	488	4
142	503	4
143	502	4
144	501	5
145	500	2
146	499	1
147	498	3
148	497	1
149	496	4
150	495	1
151	494	4
152	493	1
153	492	4
154	491	4
155	474	2
156	482	3
157	413	4
158	476	1
159	477	4
160	478	5
161	479	5
162	490	4
163	481	1
164	489	4
165	483	4
166	484	3
167	485	4
168	486	2
169	487	5
170	506	4
171	480	4
172	531	2
173	504	3
174	524	3
175	526	2
176	527	3
177	528	2
178	522	4
179	530	2
180	521	4
181	533	4
182	534	4
183	535	4
184	536	4
185	537	1
186	538	4
187	529	2
188	513	5
189	473	5
190	507	1
191	508	5
192	509	1
193	510	5
194	523	5

195	512	4
196	505	4
197	514	5
198	516	5
199	517	5
200	518	2
201	519	3
202	520	3
203	511	1
204	423	2
205	438	2
206	437	2
207	436	4
208	435	4
209	434	5
210	433	5
211	432	2
212	431	4
213	430	4
214	429	4
215	428	3
216	427	4
217	426	1
218	475	5
219	417	5
220	409	5
221	410	1
222	411	4
223	274	3
224	414	4
225	425	4
226	416	4
227	424	2
228	418	2
229	419	4
230	420	2
231	421	4
232	422	4
233	441	3
234	267	4
235	465	1
236	439	4
237	458	3
238	459	4
239	460	5
240	461	2
241	456	4
242	464	4
243	455	4
244	466	2
245	467	4
246	468	1
247	470	5
248	471	4
249	472	5
250	463	3
251	448	3
252	408	5
253	442	3
254	443	2
255	444	4
256	445	5
257	457	4
258	447	4
259	440	5
260	449	5
261	450	4
262	451	2
263	452	5
264	453	5
265	454	4
266	446	2
267	87	2
268	269	5

269	101	3
270	100	3
271	99	4
272	98	4
273	97	3
274	96	4
275	95	4
276	94	4
277	93	4
278	92	2
279	91	1
280	90	4
281	103	5
282	80	2
283	73	1
284	74	4
285	75	5
286	76	1
287	77	4
288	89	2
289	79	4
290	88	2
291	81	5
292	82	2
293	84	2
294	85	5
295	86	4
296	104	4
297	78	4
298	120	4
299	135	5
300	134	5
301	133	4
302	132	1
303	131	4
304	130	4
305	129	4
306	128	4
307	127	4
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>

> #POSTSCRIPT

> #just to clarify things completely

> #A final comment

> #In the table above: 1=Iota 2=Gamma 3=Kappa 4=Tau 5=

Chi