

Supplementary Appendix for the Simulation Studies in: “Using a Probabilistic Model to Assist Merging of Large-scale Administrative Records.”*

Ted Enamorado[†] Benjamin Fiffield[‡] Kosuke Imai[§]

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In this section we present the full set of simulation results. The tables present the estimation error for the turnout rate among matched voters, its corresponding root mean square error, the false discovery rate (FDR), the false negative rate (FNR), the estimated FDR and FNR, and the match rate of exact matching. The size of the datasets and the amount of overlap between them vary across each simulation setup. To declare a pair of records to be in the set of matches, three different thresholds are considered. The Online Supplementary Information Appendix S9 presents the details about how the data sets for these simulation exercises were constructed.

For the models assuming independence across linkage fields conditional on the matching status, two major are found under these other simulation scenarios. First, regardless of the missing data or measurement error mechanism structures, `fastLink` controls FDR, FNR, and estimation error well. Second, a greater degree of overlap between datasets leads to better merging results in terms of FDR and FNR as well as the accuracy of their estimates. Once we move away from the conditional independent model and dependencies are allowed, not only FDR, FNR, and the estimation error are controlled, but even in cases where the degree of overlap is small the parameters of the model are more accurate.

*The proposed methodology is implemented through an open-source R package, `fastLink`: Fast Probabilistic Record Linkage, which is freely available for download at the Comprehensive R Archive Network (CRAN; <https://CRAN.R-project.org/package=fastLink>)

[†]Ph.D. Candidate, Department of Politics, Princeton University, Princeton NJ 08544. Email: tede@princeton.edu

[‡]Ph.D. Candidate, Department of Politics, Princeton University, Princeton NJ 08544. Email: bfiffield@princeton.edu, URL: <http://www.benfiffield.com>

[§]Professor, Department of Government and Statistics, Harvard University. Phone: 617-384-6778, Email: imai@harvard.edu, URL: <https://imai.fas.harvard.edu>

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Scenario	Size Balance	Degree of Overlap	Conditional independence
Missing information under MAR	1:100	20% (Table S.A.1); 50% (Table S.A.2); 80% (Table S.A.3)	✓
	1:10	20% (Table S.A.4); 50% (Table S.A.5); 80% (Table S.A.6)	✓
	1:1	20% (Table S.A.7); 50% (Table S.A.8); 80% (Table S.A.9)	✓
Missing information as disagreements	1:100	20% (Table S.A.10); 50% (Table S.A.11); 80% (Table S.A.12)	✓
	1:10	20% (Table S.A.13); 50% (Table S.A.14); 80% (Table S.A.15)	✓
	1:1	20% (Table S.A.16); 50% (Table S.A.17); 80% (Table S.A.18)	✓
Measurement error	1:100	20% (Table S.A.19); 50% (Table S.A.20); 80% (Table S.A.21)	✓
	1:10	20% (Table S.A.22); 50% (Table S.A.23); 80% (Table S.A.24)	✓
	1:1	20% (Table S.A.25); 50% (Table S.A.26); 80% (Table S.A.27)	✓
Measurement error	1:100	20% (Table S.A.28); 50% (Table S.A.29); 80% (Table S.A.30)	✗
	1:10	20% (Table S.A.31); 50% (Table S.A.32); 80% (Table S.A.33)	✗
	1:1	20% (Table S.A.34); 50% (Table S.A.35); 80% (Table S.A.36)	✗

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95									
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact				
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	-1.50	3.38	27.01	0.00	9.08	7.20	-1.10	3.35	20.00	0.00	1.73	40.65	-1.93	3.83	13.04	0.00	0.20	50.62	57.50
10%	0.50	3.21	21.60	2.00	1.29	21.73	-0.42	3.32	15.58	2.50	0.99	40.90	-1.50	3.68	12.61	3.00	0.18	45.55	40.50
15%	-1.04	3.56	13.89	7.00	3.09	31.68	-1.50	3.80	10.68	8.00	0.57	38.52	-2.01	4.09	8.08	9.00	0.19	41.08	28.00
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.53	3.09	27.68	2.00	1.51	9.58	-0.46	3.26	18.67	2.00	1.06	37.43	-1.28	3.55	14.41	2.00	0.18	44.85	60.50
10%	1.73	3.54	25.86	2.50	6.59	16.13	1.17	3.42	20.58	3.50	1.94	39.69	-0.17	3.34	14.60	3.50	0.40	50.00	47.50
15%	1.39	3.50	25.21	9.50	6.41	25.20	0.73	3.42	20.54	11.00	2.58	43.03	2.12	4.07	14.49	11.50	0.45	56.38	28.50
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	-0.60	3.07	28.52	1.00	2.26	11.88	-1.50	3.52	20.16	1.00	2.23	37.62	-1.07	3.45	15.81	1.50	0.24	50.32	59.50
10%	0.93	3.20	26.97	2.50	6.79	15.86	1.22	3.46	18.83	3.00	2.19	39.03	0.99	3.51	12.22	3.00	0.19	52.95	43.00
15%	-0.30	3.18	23.20	4.00	5.45	23.50	1.11	3.48	18.26	6.00	2.01	40.45	1.25	3.61	14.68	7.00	0.39	51.97	30.00
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-1.13	3.25	26.67	1.00	8.96	6.45	-0.87	3.37	16.88	1.50	1.38	41.76	-1.07	3.47	14.78	2.00	0.14	49.78	62.50
10%	-1.69	3.51	26.79	3.00	5.86	17.95	-0.88	3.33	20.58	3.50	1.91	37.32	-1.50	3.67	14.29	4.00	0.34	48.64	39.00
15%	-4.39	5.44	25.21	9.50	5.40	26.37	-3.94	5.17	20.89	11.00	2.14	42.19	-4.36	5.56	15.24	11.00	0.46	53.77	26.00
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-1.50	3.35	30.00	2.00	9.29	6.48	-3.11	4.45	20.97	2.00	1.78	40.11	-3.02	4.47	15.58	2.50	0.15	50.27	59.50
10%	-2.07	3.72	26.62	3.50	7.24	15.70	-2.12	3.86	21.16	5.00	2.74	36.67	-4.41	5.54	15.70	6.00	0.29	54.68	32.00
15%	-3.41	4.73	24.68	11.50	5.37	26.35	-3.43	4.75	24.46	12.00	2.06	32.24	-2.96	4.57	16.02	13.50	0.47	55.04	29.00

Table S.A.1: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where the one is of 100,000 records and the other has 1000 records. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
MISSING COMPLETELY AT RANDOM (MCAR)																		
5%	-0.29	2.22	3.30	0.40	0.12	2.28	-0.39	2.24	3.31	0.60	0.09	2.42	-0.29	2.23	3.12	0.60	0.01	2.68
10%	-0.69	2.33	2.96	1.60	0.26	4.50	-0.69	2.33	2.96	1.60	0.18	4.80	-0.60	2.31	2.79	2.40	0.11	5.80
15%	0.82	2.40	1.63	3.60	0.39	6.46	0.61	2.35	1.64	4.00	0.20	7.11	0.63	2.38	0.84	5.60	0.05	9.94
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																		
5%	-0.10	2.21	3.51	1.00	0.17	1.92	0.00	2.21	3.52	1.20	0.11	2.21	0.10	2.22	3.33	1.20	0.09	2.55
10%	1.30	2.59	3.41	3.60	0.28	7.20	2.04	3.04	3.27	5.20	0.25	8.44	2.59	3.45	3.11	6.40	0.11	9.92
15%	2.75	3.59	3.18	8.60	0.76	13.53	3.10	3.87	3.21	9.60	0.53	14.39	5.18	5.69	2.93	13.80	0.13	18.37
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																		
5%	-0.29	2.22	3.29	0.00	0.18	1.78	-0.29	2.22	3.29	0.00	0.18	1.78	0.10	2.22	3.33	1.20	0.02	2.88
10%	0.89	2.40	3.78	3.20	0.43	4.41	1.20	2.54	3.80	3.80	0.22	5.01	1.84	2.91	3.06	5.00	0.03	7.22
15%	1.93	2.97	3.67	5.40	0.75	11.54	2.27	3.21	3.72	6.80	0.39	12.94	2.55	3.44	3.40	9.20	0.06	16.31
MISSING AT RANDOM (MAR): INDEPENDENCE																		
5%	-0.19	2.21	3.88	0.80	0.13	2.44	-0.19	2.22	3.89	1.20	0.10	2.72	-0.39	2.25	3.91	1.60	0.08	3.05
10%	-0.89	2.40	2.78	2.20	0.31	4.80	-1.00	2.46	2.61	3.00	0.25	5.67	-1.43	2.67	2.65	4.60	0.10	7.36
15%	-1.21	2.56	4.45	5.60	0.64	11.89	-1.53	2.73	4.09	6.20	0.39	12.99	-1.06	2.54	3.60	9.00	0.09	16.34
MISSING AT RANDOM (MAR): DEPENDENCE																		
5%	-0.39	2.23	3.86	0.40	0.16	1.61	-0.39	2.23	3.86	0.40	0.14	1.75	-0.29	2.22	3.68	0.40	0.08	2.24
10%	-0.40	2.27	3.00	3.00	0.24	5.06	-0.51	2.31	3.03	4.00	0.21	5.77	-0.10	2.27	2.45	4.60	0.09	6.94
15%	-1.12	2.52	4.48	6.20	0.36	9.32	-1.34	2.64	4.54	7.40	0.31	10.27	-1.37	2.67	4.21	9.00	0.11	12.56

Table S.A.2: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	0.19	1.78	0.37	0.25	0.01	1.32	0.19	1.78	0.37	0.25	0.00	1.41	0.19	1.78	0.37	0.25	0.00	1.41	61.38
10%	-0.13	1.78	0.63	1.62	0.18	2.59	-0.20	1.79	0.51	1.62	0.07	3.35	-0.13	1.78	0.51	1.75	0.02	4.52	38.00
15%	-0.60	1.89	0.39	3.25	0.18	6.05	-0.53	1.87	0.39	3.38	0.10	6.18	-0.36	1.84	0.39	4.75	0.02	7.63	23.25
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.06	1.77	0.75	0.88	0.22	1.63	0.12	1.78	0.63	0.88	0.08	1.74	0.50	1.85	0.51	1.50	0.01	3.12	57.38
10%	1.46	2.31	0.90	3.50	0.30	6.70	1.46	2.31	0.90	3.50	0.29	6.80	2.06	2.74	0.78	4.75	0.04	8.95	40.25
15%	3.27	3.75	0.95	8.75	0.45	10.67	3.27	3.75	0.95	8.75	0.25	11.16	4.04	4.45	0.42	10.75	0.06	14.21	30.00
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.13	1.77	1.12	0.88	0.04	1.60	0.13	1.77	1.12	0.88	0.04	1.60	0.37	1.81	0.75	1.25	0.02	3.21	60.00
10%	1.46	2.31	1.03	3.62	0.30	6.29	1.46	2.31	1.03	3.62	0.26	6.39	1.80	2.55	0.78	4.75	0.04	8.26	39.75
15%	2.73	3.29	0.68	8.50	0.54	11.89	2.73	3.29	0.68	8.50	0.45	12.27	4.23	4.63	0.42	12.00	0.04	16.44	29.25
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.06	1.77	0.75	0.38	0.24	1.22	-0.06	1.77	0.75	0.38	0.04	1.33	-0.07	1.77	0.50	0.88	0.00	3.03	60.12
10%	-0.00	1.77	1.01	1.50	0.35	3.23	-0.00	1.77	1.01	1.50	0.21	3.81	-0.08	1.79	0.51	2.62	0.05	5.95	38.75
15%	-1.02	2.08	0.92	6.00	0.58	10.44	-0.96	2.05	0.79	6.00	0.41	10.62	-1.28	2.25	0.54	8.75	0.08	14.56	26.12
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-0.06	1.77	0.87	0.50	0.18	0.94	-0.19	1.78	0.75	0.62	0.03	1.61	-0.13	1.78	0.50	0.75	0.01	2.70	60.38
10%	-0.27	1.80	0.76	2.50	0.23	4.65	-0.20	1.80	0.64	2.50	0.13	4.87	-0.41	1.84	0.52	3.75	0.05	6.60	40.38
15%	-1.04	2.10	1.07	7.38	0.39	9.71	-1.11	2.14	1.07	7.50	0.32	10.02	-0.89	2.06	0.55	9.75	0.04	12.96	23.75

Table S.A.3: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	-0.87	1.34	16.74	0.80	2.35	28.12	-0.84	1.32	16.55	0.95	1.99	28.75	-1.01	1.46	12.20	1.05	0.15	39.08	58.15
10%	-1.18	1.57	17.06	2.50	3.50	27.04	-1.07	1.51	12.31	2.75	0.53	38.54	-1.03	1.49	10.31	3.40	0.17	41.31	35.25
15%	-0.59	1.23	11.59	4.65	1.32	35.43	-0.76	1.33	10.98	5.55	1.11	36.25	-0.79	1.36	8.78	7.05	0.26	41.19	21.75
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	-0.68	1.19	24.79	0.80	1.88	10.92	-1.03	1.45	17.58	0.85	1.84	30.89	-0.51	1.17	12.70	1.05	0.16	41.06	58.75
10%	0.45	1.10	23.43	4.90	2.42	20.62	0.82	1.32	18.02	5.40	2.24	33.85	1.09	1.53	12.34	6.20	0.20	44.89	42.20
15%	1.81	2.09	18.92	9.55	3.48	34.30	2.81	3.02	14.33	11.80	0.97	43.35	3.29	3.47	11.68	13.00	0.25	48.54	29.55
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	-1.29	1.62	25.06	0.70	1.99	11.20	-0.89	1.36	17.18	0.95	1.87	32.03	-0.38	1.12	12.92	1.30	0.16	42.96	59.65
10%	-0.26	1.03	23.81	5.10	6.49	18.62	-0.08	1.04	18.50	5.50	2.41	33.57	0.39	1.15	12.09	6.60	0.17	48.05	40.70
15%	2.18	2.43	18.47	9.75	3.91	32.71	3.12	3.31	13.93	11.65	1.06	40.88	3.12	3.31	11.17	12.95	0.31	45.75	29.90
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-2.02	2.24	24.32	0.90	1.93	10.50	-1.41	1.74	16.81	1.05	1.87	30.26	-1.43	1.78	12.56	1.15	0.15	41.40	57.60
10%	-1.37	1.72	18.54	4.45	2.89	30.99	-1.42	1.76	17.99	5.15	2.68	31.74	-1.87	2.16	11.18	6.25	0.19	45.18	38.85
15%	-1.98	2.25	18.27	8.05	3.93	31.77	-2.65	2.87	13.55	10.35	1.07	41.89	-3.00	3.21	10.72	11.70	0.28	47.59	26.30
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-1.85	2.09	24.37	0.85	1.74	10.35	-1.29	1.64	16.94	0.95	1.28	32.04	-1.66	1.96	13.05	1.10	0.16	40.67	57.70
10%	-1.45	1.78	17.63	3.55	3.03	29.83	-1.64	1.95	16.30	4.50	1.59	34.35	-2.02	2.29	11.93	5.10	0.21	43.85	39.05
15%	-2.36	2.59	18.60	8.55	3.91	31.53	-3.08	3.27	14.29	11.20	1.01	41.12	-3.49	3.67	10.88	12.35	0.25	46.23	26.60

Table S.A.4: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
MISSING COMPLETELY AT RANDOM (MCAR)																		
5%	-0.12	0.71	2.35	0.32	0.20	1.75	-0.10	0.71	2.20	0.42	0.16	2.18	-0.10	0.71	2.05	0.54	0.02	2.57
10%	-0.08	0.71	2.09	1.56	0.27	3.98	0.02	0.71	1.82	1.86	0.19	4.56	0.15	0.73	0.87	2.38	0.03	6.87
15%	-0.31	0.78	1.89	3.46	0.52	7.86	-0.34	0.79	1.74	4.26	0.28	8.95	-0.31	0.79	0.90	5.68	0.06	11.42
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																		
5%	0.26	0.75	2.38	0.62	0.25	2.51	0.32	0.77	2.21	0.78	0.14	2.99	0.45	0.84	2.16	1.10	0.10	3.38
10%	1.09	1.30	2.70	3.30	0.47	7.19	1.37	1.55	2.42	4.02	0.22	8.31	1.77	1.91	2.29	5.40	0.10	9.68
15%	3.18	3.26	2.77	8.02	0.80	14.66	3.53	3.60	2.53	9.22	0.42	16.10	4.52	4.58	2.09	12.12	0.09	19.46
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																		
5%	0.10	0.71	2.43	0.30	0.28	2.32	0.28	0.75	2.28	0.60	0.16	2.90	0.45	0.84	2.16	1.10	0.10	3.50
10%	1.34	1.51	2.51	3.56	0.47	7.11	1.62	1.77	2.25	4.32	0.21	8.32	2.02	2.14	2.18	5.58	0.09	9.60
15%	2.57	2.67	3.07	8.42	0.87	12.94	2.93	3.02	2.80	9.72	0.38	14.50	3.84	3.91	2.28	12.44	0.09	17.94
MISSING AT RANDOM (MAR): INDEPENDENCE																		
5%	-0.09	0.71	2.41	0.36	0.24	2.21	-0.08	0.71	2.30	0.48	0.15	2.59	-0.13	0.71	2.19	0.82	0.11	3.12
10%	-0.27	0.76	2.32	2.30	0.47	6.44	-0.26	0.75	2.16	2.92	0.24	7.44	-0.58	0.92	1.95	4.46	0.09	9.10
15%	-0.70	1.01	2.16	6.62	0.75	13.12	-0.90	1.16	1.81	7.96	0.34	14.86	-1.22	1.43	1.70	10.80	0.09	17.66
MISSING AT RANDOM (MAR): DEPENDENCE																		
5%	-0.03	0.70	2.35	0.26	0.24	2.45	-0.03	0.70	2.20	0.38	0.14	2.90	-0.18	0.72	2.15	0.76	0.10	3.35
10%	-0.67	0.98	2.49	3.04	0.47	6.59	-0.74	1.03	2.21	3.74	0.22	7.75	-1.03	1.26	2.10	5.04	0.10	9.11
15%	-1.23	1.42	2.60	6.96	0.85	13.64	-1.58	1.74	2.33	8.42	0.38	15.28	-2.23	2.35	1.90	11.24	0.08	18.70

Table S.A.5: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate $\widehat{\text{FDR}}$, and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95						
	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	0.02	0.56	0.46	0.31	0.05	1.06	0.04	0.56	0.23	0.33	0.05	2.24	0.06	0.56	0.19	0.56	0.01	2.64	59.25
10%	0.03	0.56	0.46	1.58	0.27	3.06	0.02	0.56	0.43	1.61	0.11	3.31	-0.06	0.57	0.27	2.28	0.02	4.92	36.10
15%	-0.01	0.57	0.45	3.80	0.23	6.80	0.00	0.57	0.41	3.80	0.20	6.89	0.03	0.57	0.30	5.15	0.03	8.45	22.43
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.31	0.64	0.54	0.67	0.24	1.55	0.32	0.65	0.54	0.70	0.22	1.64	0.52	0.76	0.24	1.14	0.01	3.69	59.71
10%	1.25	1.37	0.67	3.25	0.38	4.74	1.25	1.37	0.63	3.24	0.33	4.95	1.77	1.86	0.29	4.62	0.02	7.62	40.60
15%	3.52	3.57	0.83	8.47	0.51	11.89	3.59	3.63	0.68	8.46	0.43	12.23	4.46	4.50	0.42	11.05	0.07	15.55	29.34
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.11	0.57	0.67	0.51	0.25	1.41	0.15	0.58	0.60	0.51	0.19	1.87	0.35	0.66	0.24	0.99	0.01	4.09	60.39
10%	1.24	1.36	0.76	3.71	0.37	4.98	1.23	1.35	0.68	3.74	0.32	5.31	1.74	1.83	0.37	5.17	0.05	8.03	40.10
15%	2.98	3.04	0.76	8.21	0.53	10.35	3.01	3.06	0.56	8.20	0.40	10.88	3.75	3.80	0.33	10.53	0.08	14.04	28.09
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.07	0.56	0.60	0.44	0.24	1.22	-0.07	0.56	0.60	0.47	0.22	1.30	-0.04	0.56	0.19	0.89	0.01	3.42	59.04
10%	-0.16	0.58	0.57	2.28	0.35	4.03	-0.16	0.59	0.53	2.28	0.31	4.17	-0.29	0.64	0.23	3.54	0.02	6.58	37.52
15%	-0.59	0.83	0.56	6.24	0.49	9.52	-0.59	0.83	0.56	6.26	0.46	9.61	-1.12	1.26	0.22	8.69	0.09	12.93	26.29
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-0.04	0.56	0.57	0.41	0.27	1.16	-0.03	0.56	0.52	0.46	0.17	1.42	-0.05	0.56	0.28	0.85	0.01	3.36	57.96
10%	-0.34	0.66	0.74	2.47	0.38	4.53	-0.35	0.66	0.70	2.49	0.29	4.72	-0.65	0.86	0.34	4.10	0.02	7.87	38.17
15%	-1.00	1.16	0.72	6.75	0.57	9.75	-0.99	1.14	0.59	6.75	0.46	10.22	-1.38	1.50	0.23	9.40	0.09	13.46	26.79

Table S.A.6: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	-0.39	0.51	12.85	0.73	2.49	26.33	-0.29	0.45	9.87	0.88	0.35	34.86	-0.26	0.43	9.19	1.09	0.17	36.32	54.92
10%	-0.39	0.52	13.14	2.62	3.33	24.05	-0.24	0.42	9.45	3.62	0.74	34.12	-0.25	0.43	7.83	4.31	0.21	37.64	32.09
15%	-0.32	0.47	13.58	6.50	4.93	28.09	-0.31	0.47	9.82	8.69	1.16	39.00	-0.20	0.41	7.25	10.00	0.24	44.72	17.94
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	-0.19	0.38	12.94	1.04	2.25	27.25	0.06	0.34	10.29	1.31	0.35	34.81	0.23	0.41	9.69	1.56	0.19	36.17	58.01
10%	1.00	1.05	13.76	4.61	3.29	28.24	1.60	1.63	10.46	5.83	0.72	36.74	2.03	2.06	8.97	6.66	0.22	40.35	39.30
15%	3.33	3.35	12.94	9.72	2.81	34.15	4.09	4.11	10.37	12.23	1.09	39.78	4.77	4.79	8.16	13.66	0.29	44.35	27.84
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	-0.17	0.37	13.18	1.36	2.28	27.32	0.08	0.34	11.40	1.56	0.38	33.27	0.29	0.44	9.79	1.84	0.18	36.64	57.63
10%	0.95	1.01	14.07	4.61	3.50	27.00	1.68	1.71	10.59	5.88	0.74	36.20	1.97	2.00	9.03	6.61	0.22	39.98	39.24
15%	3.09	3.11	13.85	10.09	3.32	31.94	3.66	3.68	10.63	12.31	1.05	39.49	4.22	4.24	8.65	13.57	0.28	44.25	27.92
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.45	0.56	13.10	1.03	1.92	29.54	-0.48	0.59	12.13	1.17	0.88	32.62	-0.61	0.70	9.61	1.39	0.18	37.91	56.89
10%	-0.79	0.85	13.88	3.67	3.25	28.35	-1.01	1.07	10.13	4.74	0.62	37.45	-1.17	1.22	8.66	5.45	0.22	40.52	36.66
15%	-1.44	1.48	14.22	8.64	3.97	33.00	-1.80	1.83	10.74	11.44	1.01	41.46	-2.13	2.16	8.44	13.00	0.27	46.16	25.15
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-0.56	0.65	13.05	1.10	2.37	26.92	-0.68	0.76	11.44	1.27	1.02	32.47	-0.83	0.89	9.78	1.50	0.18	36.68	56.84
10%	-0.92	0.98	13.91	4.03	3.37	27.24	-1.18	1.23	10.37	5.24	0.67	36.53	-1.50	1.54	8.82	5.97	0.22	39.88	37.51
15%	-1.91	1.94	13.16	9.24	2.68	32.76	-2.20	2.23	10.54	11.59	1.10	38.24	-2.66	2.68	8.26	12.81	0.29	43.12	26.29

Table S.A.7: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets with of 100,000 records each. In addition, there is a 20% overlap and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	-0.03	0.22	1.09	0.52	0.24	2.17	-0.02	0.22	1.02	0.63	0.15	2.60	-0.02	0.22	0.94	0.92	0.11	3.18	54.95
10%	-0.00	0.22	1.12	1.83	0.45	4.51	0.01	0.23	0.98	2.34	0.22	5.49	-0.04	0.23	0.89	3.55	0.10	6.92	31.72
15%	-0.09	0.24	1.18	4.97	0.72	9.33	-0.05	0.23	0.92	5.99	0.33	11.06	-0.03	0.23	0.53	8.51	0.05	14.44	17.84
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.24	0.32	1.26	0.74	0.23	3.01	0.33	0.40	1.20	0.93	0.13	3.50	0.46	0.52	1.18	1.37	0.10	3.99	58.17
10%	1.39	1.41	1.35	3.48	0.53	7.32	1.67	1.68	1.25	4.15	0.25	8.27	2.20	2.22	1.06	5.69	0.09	10.24	39.78
15%	3.45	3.46	1.51	8.80	0.75	14.22	3.86	3.87	1.30	9.92	0.38	15.60	4.65	4.66	0.99	12.31	0.10	18.58	28.01
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.21	0.31	1.24	0.83	0.21	3.06	0.28	0.36	1.19	1.00	0.13	3.44	0.43	0.48	1.16	1.42	0.09	3.96	58.34
10%	1.29	1.31	1.34	3.53	0.48	6.68	1.55	1.57	1.26	4.28	0.28	7.57	2.09	2.11	1.08	5.74	0.09	9.54	39.67
15%	3.18	3.19	1.54	8.71	0.74	13.06	3.49	3.50	1.38	9.76	0.44	14.33	4.14	4.15	1.06	12.07	0.10	17.34	28.25
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.10	0.25	1.24	0.58	0.20	2.83	-0.13	0.26	1.14	0.70	0.13	3.21	-0.19	0.29	1.12	1.09	0.09	3.67	56.35
10%	-0.31	0.38	1.26	2.68	0.44	6.50	-0.38	0.44	1.09	3.30	0.21	7.55	-0.57	0.61	1.01	4.75	0.09	9.04	37.01
15%	-0.68	0.72	1.36	6.88	0.78	12.66	-0.87	0.90	1.20	8.11	0.42	14.09	-1.16	1.19	0.94	10.81	0.10	17.36	25.37
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-0.12	0.25	1.21	0.59	0.21	2.60	-0.14	0.26	1.13	0.71	0.13	2.94	-0.20	0.30	1.11	1.11	0.10	3.39	56.99
10%	-0.48	0.53	1.34	2.79	0.46	6.10	-0.59	0.63	1.18	3.46	0.22	7.24	-0.80	0.83	1.07	5.00	0.09	8.99	37.78
15%	-1.22	1.24	1.38	7.24	0.75	12.19	-1.42	1.44	1.23	8.47	0.44	13.50	-1.94	1.95	1.01	11.24	0.10	16.73	26.31

Table S.A.8: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets with of 100,000 records each. In addition, there is a 50% overlap and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
MISSING COMPLETELY AT RANDOM (MCAR)																		
5%	-0.01	0.18	0.14	0.43	0.21	1.37	-0.01	0.18	0.13	0.47	0.19	1.57	0.00	0.18	0.05	0.69	0.02	3.28 54.57
10%	-0.00	0.18	0.15	1.83	0.29	3.66	0.00	0.18	0.14	1.86	0.26	3.79	0.01	0.18	0.08	2.87	0.05	5.65 31.56
15%	0.00	0.18	0.23	4.83	0.49	7.62	0.01	0.18	0.20	4.91	0.39	8.17	-0.01	0.18	0.12	7.28	0.09	11.06 17.91
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																		
5%	0.27	0.32	0.14	0.70	0.22	1.81	0.27	0.32	0.13	0.75	0.18	2.01	0.41	0.44	0.05	1.11	0.02	4.15 58.02
10%	1.39	1.40	0.19	3.57	0.38	5.78	1.40	1.41	0.17	3.62	0.29	6.17	1.96	1.97	0.08	5.06	0.05	8.85 39.32
15%	3.57	3.57	0.24	8.53	0.50	12.56	3.58	3.59	0.20	8.56	0.41	12.96	4.40	4.40	0.10	11.04	0.08	16.34 27.78
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																		
5%	0.25	0.30	0.14	0.69	0.22	1.80	0.24	0.30	0.13	0.73	0.18	2.02	0.39	0.43	0.04	1.10	0.02	4.20 58.07
10%	1.33	1.34	0.20	3.62	0.34	5.48	1.32	1.33	0.18	3.64	0.28	5.80	1.75	1.76	0.09	5.02	0.05	8.47 39.55
15%	3.27	3.27	0.24	8.73	0.50	11.48	3.27	3.28	0.23	8.79	0.38	11.80	3.86	3.86	0.10	11.11	0.09	15.30 28.05
MISSING AT RANDOM (MAR): INDEPENDENCE																		
5%	-0.05	0.18	0.13	0.49	0.20	1.66	-0.05	0.18	0.13	0.54	0.18	1.88	-0.08	0.19	0.05	0.83	0.02	3.86 56.46
10%	-0.32	0.37	0.17	2.53	0.34	5.08	-0.32	0.37	0.15	2.56	0.28	5.37	-0.52	0.55	0.08	3.89	0.05	7.89 36.79
15%	-0.76	0.78	0.24	6.64	0.55	10.96	-0.77	0.79	0.23	6.70	0.43	11.23	-1.11	1.12	0.12	9.47	0.09	15.00 25.41
MISSING AT RANDOM (MAR): DEPENDENCE																		
5%	-0.07	0.19	0.16	0.59	0.22	1.68	-0.06	0.19	0.14	0.63	0.17	1.91	-0.09	0.20	0.06	0.94	0.02	3.99 57.00
10%	-0.38	0.42	0.19	2.77	0.36	4.78	-0.38	0.42	0.15	2.78	0.27	5.18	-0.61	0.63	0.07	4.18	0.05	7.82 37.53
15%	-1.24	1.25	0.28	7.37	0.54	10.48	-1.24	1.25	0.26	7.43	0.42	10.76	-1.69	1.70	0.12	10.04	0.09	14.45 26.32

Table S.A.9: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets with of 100,000 records each. In addition, there is a 80% overlap and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95							
	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact				
MISSING COMPLETELY AT RANDOM (MCAR)																				
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE	5%	-2.25	3.81	25.94	1.50	0.27	10.87	-3.06	4.53	12.44	1.50	0.21	49.17	-3.99	5.22	12.67	3.50	0.03	51.57	57.50
	10%	-0.24	3.26	21.43	6.50	7.05	15.43	-2.92	4.51	12.74	7.50	0.17	45.58	-3.16	4.68	12.80	8.00	0.15	45.81	40.50
	15%	-0.62	3.38	20.18	9.00	1.08	27.54	-2.26	4.23	7.61	9.00	0.70	45.05	-2.31	4.35	6.49	13.50	0.18	48.06	28.00
MISSING NOT AT RANDOM (MNAR): DEPENDENCE	5%	0.37	3.08	27.61	3.00	0.20	10.01	-1.28	3.56	14.54	3.00	0.17	44.42	-1.06	3.50	14.60	3.50	0.13	44.73	60.50
	10%	2.07	3.77	25.79	6.50	9.68	7.67	-0.35	3.42	13.82	6.50	0.28	46.61	-0.56	3.49	14.15	9.00	0.17	47.80	47.50
	15%	2.58	4.16	24.89	12.50	11.27	8.76	2.80	4.61	10.75	17.00	0.21	50.57	3.45	5.05	10.99	19.00	0.16	51.39	28.50
MISSING AT RANDOM (MAR): INDEPENDENCE	5%	-0.02	3.05	28.15	3.00	0.38	9.48	-0.84	3.42	15.28	3.00	0.34	47.89	0.54	3.41	15.84	7.00	0.18	49.48	59.50
	10%	1.26	3.38	25.59	5.50	9.86	11.65	0.84	3.52	12.15	6.00	0.26	49.43	1.08	3.60	12.21	6.50	0.24	49.63	43.00
	15%	1.06	3.44	22.65	9.50	8.42	11.62	1.83	4.02	12.31	14.50	0.27	48.40	1.59	3.93	11.86	14.50	0.23	48.86	30.00
MISSING AT RANDOM (MAR): DEPENDENCE	5%	-1.31	3.33	26.59	2.00	0.22	7.06	-1.50	3.63	14.78	2.00	0.19	47.43	-1.28	3.56	14.98	3.50	0.02	49.56	62.50
	10%	-2.28	3.87	26.56	6.00	8.36	14.10	-3.39	4.83	11.79	6.50	0.24	47.71	-3.63	5.01	11.85	7.00	0.22	47.93	39.00
	15%	-5.12	6.07	25.96	13.00	9.87	11.72	-6.64	7.58	12.43	19.00	0.17	49.39	-7.37	8.25	12.85	22.00	0.15	50.23	26.00
MISSING AT RANDOM (MAR): DEPENDENCE	5%	-2.05	3.65	29.82	3.50	0.24	8.04	-2.60	4.22	14.98	3.50	0.18	48.07	-3.06	4.53	15.11	4.50	0.03	50.04	59.50
	10%	-3.88	5.00	26.98	8.00	0.34	15.41	-4.77	5.87	14.02	8.00	0.22	49.89	-5.02	6.08	14.08	8.50	0.21	50.10	32.00
	15%	-4.13	5.30	25.00	14.50	9.67	11.26	-6.64	7.58	12.97	19.50	0.16	50.06	-7.54	8.40	13.19	21.00	0.15	50.55	29.00

Table S.A.10: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where the one is of 100,000 records and the other has 1000 records. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95						
	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	-0.29	2.22	3.50	0.60	0.16	2.81	-0.29	2.22	3.50	0.60	0.16	2.81	0.39	2.26	3.35	1.80	0.05	4.50	60.60
10%	-0.30	2.26	3.59	3.40	0.40	10.87	-0.30	2.27	3.03	4.00	0.15	12.56	-0.41	2.29	3.05	4.60	0.14	13.01	36.00
15%	1.23	2.58	2.88	5.60	0.31	18.46	1.23	2.58	2.88	5.60	0.31	18.46	1.28	2.64	1.91	7.80	0.14	20.95	21.40
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.39	2.26	3.35	1.80	0.10	3.55	0.59	2.30	3.36	2.20	0.07	3.85	0.79	2.37	3.37	2.60	0.05	4.19	57.20
10%	2.60	3.46	4.16	7.80	0.36	12.75	3.04	3.80	3.98	8.40	0.30	13.30	5.07	5.58	3.08	12.00	0.05	17.19	41.20
15%	5.36	5.85	4.46	14.40	0.83	23.58	6.55	6.97	3.91	16.40	0.38	25.76	7.24	7.63	3.50	17.40	0.14	27.41	29.00
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.29	2.23	3.70	1.20	0.10	3.93	0.30	2.24	3.55	2.20	0.09	4.82	0.30	2.24	3.55	2.20	0.09	4.82	61.20
10%	1.74	2.85	4.91	7.00	0.34	10.23	1.86	2.94	4.75	7.80	0.19	10.95	2.42	3.34	3.79	8.60	0.09	12.88	36.80
15%	3.43	4.14	4.51	11.00	0.51	30.29	3.46	4.17	4.33	11.60	0.31	31.32	3.74	4.42	4.19	13.00	0.13	32.93	27.40
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.67	2.29	5.76	1.80	0.27	3.60	-0.20	2.22	4.31	2.40	0.07	5.70	-0.20	2.22	4.31	2.40	0.07	5.70	58.20
10%	-1.41	2.65	4.02	4.40	0.62	22.20	-1.53	2.73	3.48	5.60	0.11	24.08	-2.11	3.12	3.59	8.60	0.10	25.76	41.60
15%	-1.28	2.64	4.89	10.60	0.38	23.87	-1.50	2.75	4.70	10.80	0.32	24.41	-1.73	2.90	4.55	11.80	0.19	25.68	25.00
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-0.39	2.23	3.86	0.40	0.12	4.11	-0.39	2.23	3.86	0.40	0.12	4.11	-0.39	2.26	3.94	2.40	0.05	5.73	56.00
10%	-1.13	2.53	3.70	6.20	0.19	12.30	-1.13	2.53	3.70	6.20	0.19	12.30	-1.16	2.57	2.95	7.80	0.07	14.84	38.60
15%	-2.32	3.23	9.29	10.20	0.75	20.18	-1.58	2.79	5.47	10.20	0.65	33.08	-2.32	3.30	4.86	13.80	0.11	36.56	24.60

Table S.A.11: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95						
	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	0.13	1.77	0.75	0.50	0.16	2.20	0.13	1.77	0.75	0.50	0.16	2.20	-0.13	1.78	0.75	1.25	0.03	3.78	61.38
10%	-0.07	1.78	0.76	2.12	0.56	7.51	-0.02	1.79	0.51	3.25	0.13	9.99	-0.02	1.79	0.51	3.25	0.13	9.99	38.00
15%	-0.03	1.81	0.65	5.12	0.50	11.62	-0.30	1.84	0.40	5.88	0.19	13.25	-0.26	1.86	0.41	8.25	0.07	15.29	23.25
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.75	1.93	0.63	2.12	0.15	2.88	0.75	1.93	0.63	2.12	0.15	2.88	1.20	2.16	0.64	3.25	0.05	4.11	57.38
10%	3.13	3.62	1.19	6.38	0.42	6.88	3.28	3.76	0.93	6.88	0.12	8.75	3.28	3.76	0.93	6.88	0.12	8.75	40.25
15%	4.59	4.96	1.27	12.88	0.68	12.26	4.54	4.91	0.85	12.88	0.33	13.00	5.79	6.09	0.88	16.00	0.07	17.00	30.00
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.81	1.95	1.13	2.00	0.17	2.76	0.94	2.01	1.14	2.25	0.14	2.96	1.33	2.22	1.15	3.00	0.05	3.87	60.00
10%	1.95	2.67	0.93	6.38	0.31	8.67	2.29	2.93	0.93	7.00	0.14	9.30	2.29	2.93	0.93	7.00	0.11	10.62	39.75
15%	5.00	5.35	1.17	15.25	0.44	13.24	5.26	5.60	0.88	15.88	0.18	14.52	5.63	5.95	0.30	16.62	0.08	15.93	29.25
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.13	1.77	0.75	0.75	0.19	1.92	-0.06	1.77	0.75	0.88	0.17	2.12	-0.33	1.82	0.76	2.62	0.04	3.95	60.12
10%	-0.21	1.81	0.90	4.00	0.38	6.97	-0.35	1.84	0.78	4.62	0.10	8.82	-0.35	1.84	0.78	4.62	0.10	8.82	38.75
15%	-1.74	2.55	0.97	10.88	0.45	22.89	-1.74	2.55	0.97	10.88	0.45	22.89	-2.27	2.96	0.72	14.12	0.10	26.41	26.12
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	0.06	1.77	0.75	0.88	0.20	2.44	0.06	1.77	0.75	1.12	0.09	2.76	0.12	1.79	0.76	2.50	0.05	4.08	60.38
10%	-0.83	2.00	0.53	5.75	0.10	6.10	-0.83	2.00	0.53	5.75	0.10	6.10	-0.83	2.00	0.53	5.75	0.10	6.10	40.38
15%	-0.62	1.96	1.38	10.75	0.53	15.51	-1.43	2.37	0.71	12.50	0.25	17.66	-2.76	3.36	0.74	15.62	0.08	20.61	23.75

Table S.A.12: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95										
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact						
MISSING COMPLETELY AT RANDOM (MCAR)																				
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE	5%	-1.14	1.50	24.93	1.70	0.24	14.84	-0.85	1.35	12.51	1.70	0.22	41.40	-1.01	1.46	12.17	2.55	0.13	42.18	58.15
	10%	-1.35	1.68	22.89	3.80	7.79	17.34	-0.56	1.22	10.97	6.25	0.23	45.00	-0.58	1.23	10.76	6.25	0.21	45.21	35.25
	15%	-0.58	1.18	20.35	6.85	1.33	28.97	-0.45	1.21	9.48	9.30	0.58	46.18	-0.67	1.32	8.77	12.60	0.21	48.66	21.75
MISSING NOT AT RANDOM (MNAR): DEPENDENCE	5%	0.02	0.98	24.97	2.35	0.32	14.02	0.04	1.05	13.24	2.35	0.29	41.51	0.36	1.12	13.00	4.00	0.15	42.70	58.75
	10%	1.40	1.73	23.99	8.60	7.72	14.50	1.88	2.18	12.44	9.20	0.27	43.59	2.17	2.43	12.46	9.70	0.25	43.91	42.20
	15%	2.69	2.89	22.92	12.75	8.05	16.76	4.07	4.22	11.62	14.85	0.39	43.37	4.25	4.40	11.27	17.35	0.22	44.91	29.55
MISSING AT RANDOM (MAR): INDEPENDENCE	5%	-0.58	1.14	25.12	2.50	0.28	14.22	0.09	1.06	13.06	2.50	0.24	43.12	0.10	1.07	12.77	3.35	0.15	43.90	59.65
	10%	0.15	1.02	24.45	7.00	8.30	14.23	1.05	1.52	12.05	9.10	0.24	45.48	1.41	1.79	12.05	10.20	0.21	46.01	40.70
	15%	2.92	3.10	22.72	12.60	1.46	23.88	3.83	3.99	11.12	15.25	0.60	44.04	4.33	4.48	10.88	17.65	0.22	45.96	29.90
MISSING AT RANDOM (MAR): DEPENDENCE	5%	-2.07	2.29	24.31	1.90	0.26	14.40	-1.47	1.81	12.68	1.90	0.24	42.00	-1.68	1.99	12.51	3.10	0.14	42.90	57.60
	10%	-2.38	2.59	23.78	8.50	0.57	21.16	-2.09	2.36	11.50	9.15	0.27	43.79	-2.18	2.45	11.49	9.85	0.25	44.18	38.85
	15%	-3.31	3.48	21.68	11.65	1.43	22.85	-3.49	3.67	10.59	14.35	0.60	43.23	-3.81	3.98	10.59	16.80	0.26	45.08	26.30
MISSING AT RANDOM (MAR): DEPENDENCE	5%	-1.94	2.17	24.97	2.20	0.27	13.89	-1.72	2.02	13.45	2.20	0.24	41.58	-1.89	2.17	13.28	3.05	0.16	42.30	57.70
	10%	-2.65	2.84	23.09	7.25	0.65	20.81	-2.29	2.54	12.00	8.00	0.28	43.44	-2.51	2.74	11.95	8.60	0.25	43.83	39.05
	15%	-4.15	4.28	22.56	12.10	1.28	24.51	-3.57	3.75	10.78	13.10	0.58	43.06	-4.05	4.21	10.58	16.75	0.22	45.41	26.60

Table S.A.13: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95										
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
MISSING COMPLETELY AT RANDOM (MCAR)																				
5%	-0.20	0.73	2.78	0.68	0.31	3.75	-0.12	0.71	2.73	0.92	0.17	4.01	-0.09	0.71	2.21	1.90	0.09	6.20	59.70	
10%	-0.01	0.71	2.93	3.14	0.51	9.49	-0.00	0.71	2.31	3.70	0.16	11.49	0.06	0.72	2.24	3.90	0.15	11.75	35.32	
15%	-0.42	0.84	3.07	6.68	0.63	22.24	-0.41	0.83	2.99	6.70	0.39	22.68	-0.54	0.91	2.17	9.82	0.11	26.45	20.90	
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																				
5%	0.54	0.89	2.84	1.44	0.33	4.17	0.63	0.94	2.81	1.64	0.20	4.39	0.99	1.22	2.82	2.84	0.14	5.41	59.66	
10%	2.11	2.22	3.53	6.50	0.46	9.47	2.25	2.36	3.39	7.08	0.22	10.18	2.55	2.66	2.72	7.56	0.10	12.25	40.92	
15%	4.93	4.99	3.37	13.38	0.64	20.72	5.37	5.42	3.19	14.32	0.41	21.68	5.79	5.84	2.99	15.64	0.16	23.27	29.26	
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																				
5%	0.48	0.85	2.92	1.66	0.33	4.73	0.58	0.91	2.83	1.84	0.30	4.97	0.97	1.20	2.79	3.18	0.10	6.25	58.82	
10%	2.25	2.36	3.50	6.68	0.42	11.43	2.47	2.57	3.44	7.36	0.20	12.19	2.55	2.65	2.71	7.36	0.17	13.74	39.14	
15%	4.09	4.15	3.54	13.40	0.66	21.97	4.41	4.48	3.33	14.60	0.38	23.20	4.61	4.67	3.19	15.70	0.17	24.63	28.56	
MISSING AT RANDOM (MAR): INDEPENDENCE																				
5%	-0.20	0.73	2.89	1.04	0.26	4.95	-0.14	0.71	2.83	1.14	0.25	5.07	-0.25	0.75	2.84	2.22	0.08	6.09	56.86	
10%	-0.83	1.10	3.38	5.70	0.55	14.63	-0.89	1.15	3.21	6.44	0.21	15.76	-0.80	1.08	2.56	6.44	0.11	17.50	37.50	
15%	-1.51	1.68	3.47	11.98	0.61	24.26	-1.50	1.67	3.36	11.98	0.37	24.62	-2.04	2.17	2.93	14.48	0.16	27.11	26.32	
MISSING AT RANDOM (MAR): DEPENDENCE																				
5%	-0.34	0.78	2.86	0.98	0.28	4.97	-0.38	0.80	2.81	1.08	0.16	5.14	-0.48	0.85	2.78	2.18	0.11	6.16	58.20	
10%	-1.37	1.55	3.52	6.20	0.61	13.17	-1.55	1.71	3.28	6.90	0.19	14.30	-1.44	1.61	2.49	6.90	0.17	16.05	38.24	
15%	-2.47	2.58	3.44	12.32	0.57	26.25	-2.50	2.61	3.29	12.32	0.36	26.65	-3.04	3.13	3.14	14.98	0.16	28.99	26.66	

Table S.A.14: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate $\widehat{\text{FDR}}$, the estimated false discovery rate $\widehat{\text{FNR}}$, and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95						
	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	0.07	0.56	0.58	0.75	0.21	2.02	0.06	0.56	0.58	0.83	0.17	2.12	0.10	0.57	0.46	1.96	0.04	3.93	59.25
10%	-0.04	0.57	0.54	2.67	0.25	6.54	-0.07	0.57	0.49	3.70	0.12	7.70	-0.07	0.57	0.49	3.70	0.11	7.73	36.10
15%	-0.07	0.58	0.88	5.53	0.49	11.95	0.01	0.58	0.60	6.71	0.18	13.92	0.07	0.59	0.55	9.20	0.09	16.15	22.43
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.70	0.90	0.69	1.62	0.25	2.28	0.76	0.95	0.70	1.88	0.17	2.54	1.15	1.28	0.65	2.94	0.06	3.72	59.71
10%	2.57	2.63	0.84	6.49	0.42	5.48	2.80	2.86	0.75	7.21	0.16	7.02	2.80	2.86	0.75	7.21	0.13	7.07	40.60
15%	5.00	5.03	0.78	12.90	0.34	10.65	5.37	5.40	0.75	14.06	0.19	11.85	5.75	5.78	0.66	15.20	0.10	13.44	29.34
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.50	0.75	0.78	1.50	0.24	2.40	0.52	0.77	0.77	1.60	0.18	2.55	0.87	1.03	0.74	2.72	0.05	3.76	60.39
10%	2.55	2.61	0.85	7.08	0.39	6.19	2.77	2.83	0.73	7.64	0.15	7.69	2.77	2.83	0.73	7.64	0.12	7.74	40.10
15%	4.28	4.32	0.85	12.74	0.51	13.20	4.27	4.31	0.84	12.74	0.31	13.41	4.75	4.79	0.60	14.95	0.10	16.30	28.09
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.16	0.58	0.72	1.17	0.19	2.62	-0.16	0.58	0.72	1.33	0.18	2.76	-0.25	0.62	0.69	2.38	0.05	3.89	59.04
10%	-0.64	0.86	0.79	5.26	0.39	7.08	-0.66	0.87	0.62	5.72	0.15	8.51	-0.66	0.87	0.62	5.72	0.15	8.52	37.52
15%	-1.61	1.72	0.89	11.21	0.47	15.01	-1.60	1.70	0.81	11.21	0.29	15.34	-2.01	2.09	0.59	13.56	0.10	18.31	26.29
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-0.21	0.60	0.69	1.40	0.20	2.75	-0.23	0.61	0.68	1.49	0.16	2.87	-0.30	0.64	0.65	2.62	0.05	4.08	57.96
10%	-0.95	1.11	0.91	5.90	0.35	7.72	-1.10	1.24	0.93	6.49	0.13	8.32	-1.08	1.23	0.74	6.49	0.13	9.36	38.17
15%	-1.85	1.95	0.86	11.70	0.50	15.48	-1.85	1.95	0.80	11.70	0.30	15.89	-2.27	2.34	0.58	14.31	0.10	19.05	26.79

Table S.A.15: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields. To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

		Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	-0.46	0.56	19.75	2.08	8.21	11.06	-0.20	0.40	9.53	2.08	0.23	39.88	-0.19	0.39	9.43	3.22	0.14	40.82	54.92
10%	-0.41	0.52	18.75	4.03	8.44	16.93	-0.29	0.45	8.11	7.03	0.22	43.53	-0.29	0.45	8.11	7.03	0.22	43.53	32.09
15%	-0.13	0.38	8.53	9.72	0.85	43.21	-0.26	0.44	8.01	10.78	0.77	43.89	-0.21	0.43	7.20	14.95	0.22	47.23	17.94
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.53	0.62	19.83	2.75	0.28	14.59	0.60	0.69	10.04	2.75	0.25	38.99	0.90	0.97	9.97	3.98	0.14	39.98	58.01
10%	2.21	2.24	19.42	6.97	8.02	15.00	2.81	2.83	9.13	9.29	0.24	42.11	3.06	3.08	9.13	9.94	0.21	42.54	39.30
15%	4.64	4.65	18.14	13.32	1.36	23.72	5.49	5.50	8.20	15.67	0.53	42.47	5.68	5.69	8.05	17.92	0.21	44.23	27.84
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.46	0.56	20.00	3.09	0.28	14.96	0.63	0.72	10.18	3.09	0.26	39.32	0.95	1.01	10.12	4.38	0.14	40.38	57.63
10%	2.09	2.12	19.39	7.06	8.04	15.43	2.69	2.71	9.28	9.67	0.23	42.52	2.69	2.71	9.28	9.67	0.23	42.52	39.24
15%	4.19	4.21	18.71	13.37	1.31	24.32	4.63	4.64	8.88	14.47	0.57	42.39	4.97	4.98	8.37	17.81	0.21	44.71	27.92
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.92	0.97	19.79	2.64	0.26	15.10	-0.72	0.79	9.94	2.64	0.24	39.88	-0.85	0.92	9.91	3.86	0.14	40.81	56.89
10%	-1.48	1.52	18.79	5.78	8.22	15.92	-1.56	1.60	8.82	8.69	0.24	42.83	-1.56	1.60	8.82	8.69	0.24	42.83	36.66
15%	-2.38	2.40	18.22	12.64	1.35	25.66	-2.36	2.39	8.62	13.97	0.60	43.21	-2.93	2.95	8.17	18.11	0.23	45.97	25.15
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-1.07	1.11	20.08	2.66	8.23	10.51	-0.90	0.96	10.13	2.66	0.24	39.26	-1.09	1.14	10.07	3.87	0.14	40.25	56.84
10%	-1.68	1.72	19.03	6.28	8.01	16.04	-1.94	1.97	9.01	8.97	0.24	42.87	-1.94	1.97	9.01	8.97	0.24	42.87	37.51
15%	-2.88	2.90	18.14	12.69	1.30	25.44	-3.04	3.06	8.65	13.95	0.56	42.74	-3.43	3.45	8.22	17.62	0.22	45.23	26.29

Table S.A.16: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets with of 100,000 records each. In addition, there is a 20% overlap and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

		Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	-0.05	0.23	1.29	1.01	0.23	4.72	-0.04	0.23	1.27	1.09	0.21	4.85	-0.01	0.22	1.24	2.06	0.07	5.89 54.95	
10%	-0.12	0.26	1.68	4.24	0.35	12.97	-0.09	0.25	1.59	4.75	0.16	13.71	-0.05	0.23	1.22	4.75	0.14	15.19 31.72	
15%	-0.01	0.23	1.66	9.47	0.46	27.20	-0.01	0.23	1.66	9.47	0.46	27.20	-0.08	0.25	1.38	11.83	0.12	29.92 17.84	
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.67	0.71	1.50	1.73	0.28	4.56	0.74	0.77	1.48	1.89	0.15	4.78	1.02	1.05	1.44	3.06	0.10	5.91 58.17	
10%	2.66	2.67	1.79	6.74	0.45	10.01	2.92	2.93	1.70	7.55	0.22	10.90	3.24	3.25	1.33	8.23	0.18	13.01 39.79	
15%	5.05	5.06	1.82	13.23	0.68	20.29	5.53	5.53	1.68	14.42	0.40	21.60	5.96	5.97	1.55	15.74	0.15	23.26 28.01	
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.61	0.65	1.45	1.84	0.27	4.80	0.66	0.70	1.43	2.02	0.15	5.03	0.94	0.97	1.39	3.12	0.09	6.11 58.34	
10%	2.48	2.50	1.77	6.92	0.45	9.71	2.71	2.72	1.69	7.61	0.21	10.51	2.95	2.96	1.36	8.28	0.17	12.58 39.67	
15%	4.41	4.41	1.89	13.05	0.68	19.39	4.67	4.68	1.73	14.12	0.40	20.64	5.02	5.02	1.62	15.37	0.15	22.22 28.26	
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.25	0.33	1.46	1.25	0.25	5.10	-0.25	0.34	1.44	1.38	0.23	5.28	-0.34	0.40	1.39	2.52	0.07	6.47 56.36	
10%	-0.75	0.78	1.74	5.81	0.38	12.11	-0.83	0.86	1.66	6.52	0.19	12.95	-0.81	0.84	1.33	6.52	0.16	14.46 37.02	
15%	-1.40	1.42	1.84	12.02	0.58	23.75	-1.40	1.42	1.78	12.02	0.38	24.15	-1.87	1.89	1.59	14.68	0.15	26.70 25.37	
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-0.28	0.36	1.44	1.38	0.26	4.80	-0.30	0.38	1.42	1.57	0.24	5.01	-0.40	0.46	1.39	2.71	0.08	6.18 56.99	
10%	-1.06	1.08	1.83	5.94	0.40	12.02	-1.18	1.20	1.76	6.63	0.19	12.87	-1.15	1.17	1.37	6.63	0.16	14.52 37.78	
15%	-2.24	2.25	1.92	12.38	0.58	24.48	-2.24	2.25	1.86	12.38	0.36	24.91	-2.70	2.71	1.65	14.94	0.14	27.42 26.31	

Table S.A.17: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets with of 100,000 records each. In addition, there is a 50% overlap and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95						
	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact			
MISSING COMPLETELY AT RANDOM (MCAR)																			
5%	-0.02	0.18	0.18	1.02	0.17	3.20	-0.02	0.18	1.02	0.15	3.21	0.02	0.18	0.17	2.12	0.07	4.37	54.57	
10%	-0.00	0.18	0.25	3.68	0.40	8.03	-0.03	0.18	0.18	4.59	0.10	10.05	-0.03	0.18	0.18	4.59	0.10	10.06	31.56
15%	-0.02	0.19	0.31	8.21	0.35	19.57	-0.04	0.19	0.27	9.42	0.31	20.69	-0.02	0.19	0.23	11.62	0.08	22.98	17.91
MISSING NOT AT RANDOM (MNAR): INDEPENDENCE																			
5%	0.67	0.70	0.17	1.69	0.22	3.00	0.75	0.77	0.17	1.87	0.18	3.19	1.09	1.11	0.16	3.09	0.09	4.40	58.02
10%	2.70	2.70	0.23	6.88	0.37	6.91	2.99	3.00	0.18	7.62	0.14	8.60	2.99	3.00	0.18	7.62	0.11	8.67	39.32
15%	5.17	5.18	0.25	13.21	0.49	13.58	5.18	5.18	0.25	13.21	0.30	13.82	6.00	6.00	0.19	15.56	0.10	16.85	27.78
MISSING NOT AT RANDOM (MNAR): DEPENDENCE																			
5%	0.63	0.66	0.19	1.70	0.22	3.01	0.70	0.73	0.18	1.89	0.18	3.19	1.01	1.02	0.18	3.06	0.09	4.39	58.07
10%	2.43	2.44	0.24	6.86	0.35	7.01	2.68	2.69	0.19	7.58	0.14	8.64	2.68	2.69	0.19	7.58	0.11	8.70	39.55
15%	4.49	4.50	0.25	13.29	0.50	13.79	4.49	4.50	0.24	13.29	0.31	14.02	5.20	5.20	0.19	15.66	0.10	17.11	28.05
MISSING AT RANDOM (MAR): INDEPENDENCE																			
5%	-0.15	0.23	0.17	1.27	0.19	3.09	-0.16	0.24	0.16	1.38	0.17	3.21	-0.24	0.30	0.16	2.54	0.08	4.38	56.46
10%	-0.66	0.69	0.26	5.04	0.47	7.24	-0.80	0.82	0.18	6.30	0.13	9.53	-0.80	0.82	0.18	6.30	0.10	9.60	36.79
15%	-1.32	1.33	0.35	10.70	0.48	16.10	-1.48	1.49	0.31	11.99	0.42	17.32	-1.80	1.81	0.21	14.68	0.09	20.79	25.41
MISSING AT RANDOM (MAR): DEPENDENCE																			
5%	-0.18	0.25	0.19	1.40	0.20	3.09	-0.20	0.27	0.19	1.56	0.17	3.25	-0.29	0.34	0.18	2.75	0.08	4.46	57.00
10%	-0.95	0.97	0.23	5.94	0.33	7.94	-1.07	1.09	0.18	6.66	0.13	9.60	-1.07	1.09	0.18	6.66	0.10	9.67	37.53
15%	-2.08	2.09	0.32	12.42	0.46	16.21	-2.08	2.09	0.30	12.43	0.28	16.59	-2.56	2.56	0.22	14.99	0.09	19.70	26.32

Table S.A.18: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets with of 100,000 records each. In addition, there is a 80% overlap and five missing data mechanisms are studied across three different proportions of missing data for each linkage field other than year of birth. Measurement error is introduced to all the string valued fields To declare a pair of records to be in the set of matches, three different thresholds are considered. For each linkage field, missing comparisons have been coded as disagreements.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95									
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact				
CLASSICAL MEASUREMENT ERROR																			
20%	-1.96	3.92	10.55	2.50	0.42	9.96	-2.19	4.05	10.14	2.50	0.22	10.94	-2.20	4.06	9.77	3.00	0.11	12.38	34.50
50%	-2.40	4.13	13.06	3.50	0.65	28.36	-2.40	4.13	13.06	3.50	0.65	28.36	-1.73	3.85	9.39	3.50	0.08	33.44	10.50
80%	-1.26	3.69	14.83	11.00	1.85	33.24	-1.99	4.02	14.08	11.50	0.76	36.13	-2.01	4.09	11.11	12.00	0.23	41.24	5.00
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.83	3.44	12.00	1.00	0.32	12.32	-0.38	3.38	11.21	1.00	0.14	13.28	0.32	3.39	10.00	1.00	0.07	14.36	37.00
50%	-1.07	3.47	15.65	3.00	2.35	28.11	-1.95	3.87	13.84	3.50	1.16	35.32	-1.50	3.75	11.79	6.50	0.16	42.20	16.00
80%	-3.19	4.72	14.98	12.00	2.64	29.98	-3.74	5.14	12.44	12.00	1.39	33.60	-3.58	5.09	9.90	13.50	0.15	41.31	6.00
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-1.50	3.67	12.95	2.50	0.58	19.06	-1.27	3.60	12.67	3.50	0.30	20.28	-1.05	3.54	12.27	3.50	0.07	22.22	34.50
50%	-0.83	3.46	16.14	6.5	2.15	24.61	-2.19	4.05	13.82	6.50	1.15	33.81	-1.74	3.89	10.63	7.50	0.15	40.55	15.50
80%	-1.02	3.61	12.86	8.5	2.07	28.13	-0.03	3.51	10.78	9.00	0.60	32.04	1.05	3.73	8.67	10.50	0.15	36.11	11.00
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.61	3.40	13.39	3.00	0.56	11.56	-0.61	3.40	13.39	3.00	0.50	11.85	-1.27	3.65	11.16	4.50	0.08	15.30	35.50
50%	-1.50	3.75	13.68	8.50	1.63	24.85	-2.22	4.12	12.92	9.00	0.90	26.71	-2.26	4.23	10.66	12.00	0.15	32.87	16.50
80%	-3.13	4.63	15.81	9.50	2.55	25.06	-2.72	4.43	12.68	10.50	0.66	32.58	-3.28	4.85	9.64	11.00	0.19	37.13	8.00
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-1.96	3.92	12.39	4.5	0.31	10.10	-1.73	3.82	11.98	4.5	0.24	11.05	-1.50	3.74	11.21	5.00	0.06	12.45	37.00
50%	-3.90	5.12	17.03	5.0	1.59	28.27	-3.30	4.71	15.32	6.00	0.68	32.63	-1.98	3.98	11.90	7.50	0.14	36.41	22.50
80%	-4.41	5.62	14.08	11.5	1.77	32.59	-4.47	5.69	13.86	13.0	1.19	34.11	-3.83	5.26	10.88	14.00	0.13	41.35	7.50

Table S.A.19: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95									
		Bias	RMSE	FDR	FNR	Bias	RMSE	FDR	FNR	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact			
CLASSICAL MEASUREMENT ERROR																			
20%	-0.49	2.27	4.70	2.60	0.26	5.98	-0.59	2.29	4.71	2.80	0.20	6.41	-0.80	2.37	3.59	3.20	0.07	8.25	35.20
50%	0.00	2.24	4.20	4.20	0.47	6.71	0.20	2.26	3.83	4.60	0.16	7.49	0.71	2.37	3.46	5.20	0.08	9.45	14.60
80%	-0.10	2.28	4.95	7.80	1.63	15.36	0.00	2.28	4.38	8.20	0.18	20.27	0.11	2.30	3.38	8.60	0.08	22.40	4.40
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.29	2.23	3.52	1.40	0.14	4.15	-0.29	2.23	3.52	1.40	0.14	4.14	0.00	2.22	3.35	1.80	0.05	5.12	34.60
50%	0.90	2.41	5.39	5.20	0.33	9.72	1.10	2.50	5.21	5.40	0.24	10.01	1.42	2.67	4.07	5.60	0.05	12.22	16.80
80%	2.80	3.64	4.09	11.00	0.43	11.08	3.06	3.85	4.15	12.20	0.30	11.94	3.42	4.15	3.75	12.80	0.09	14.33	9.00
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.20	2.23	4.15	3.00	0.34	3.92	0.20	2.24	3.77	3.00	0.23	4.38	0.20	2.26	3.23	4.00	0.02	7.06	35.60
50%	1.39	2.63	4.56	3.80	0.73	5.77	1.11	2.50	4.02	4.60	0.23	7.17	1.54	2.74	2.87	5.40	0.09	9.70	19.20
80%	1.23	2.58	4.30	6.60	0.76	11.46	1.47	2.72	3.78	8.40	0.22	14.01	1.49	2.75	2.98	8.80	0.08	15.34	9.60
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.10	2.22	3.72	1.60	0.17	5.71	-0.10	2.22	3.72	1.60	0.11	5.86	0.20	2.23	3.54	2.00	0.06	6.49	37.00
50%	-0.30	2.25	5.35	4.40	0.52	10.39	-0.80	2.38	4.82	5.20	0.10	12.00	-0.71	2.37	3.46	5.20	0.06	13.33	16.60
80%	-0.80	2.38	7.23	7.60	2.50	13.28	-0.84	2.44	5.44	9.60	0.58	19.99	-0.75	2.43	3.84	9.80	0.13	27.05	7.80
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-0.78	2.35	3.32	1.00	0.26	3.60	-0.59	2.29	2.94	1.00	0.14	4.20	-0.69	2.33	2.76	1.40	0.02	5.55	32.40
50%	-1.38	2.62	6.13	5.00	0.40	13.43	-1.49	2.68	5.94	5.00	0.26	13.86	-1.71	2.82	4.63	5.20	0.08	16.10	16.40
80%	-0.73	2.40	5.20	8.80	0.56	12.95	-1.17	2.58	4.67	10.20	0.28	14.44	-1.29	2.65	4.08	10.60	0.12	15.65	8.80

Table S.A.20: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95									
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact				
CLASSICAL MEASUREMENT ERROR																			
20%	0.37	1.82	0.38	1.88	0.10	1.77	0.37	1.82	0.08	1.87	0.37	1.82	0.38	2.12	0.01	2.77	33.88		
50%	-0.14	1.79	0.89	2.88	0.55	3.10	-0.21	1.80	0.64	3.00	0.16	4.51	-0.21	1.80	0.64	3.25	0.07	5.37	14.00
80%	-0.11	1.83	0.67	7.00	0.45	6.93	-0.18	1.84	0.67	7.12	0.27	7.81	0.15	1.85	0.41	8.75	0.05	10.65	4.00
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	0.37	1.82	0.64	2.38	0.10	2.37	0.37	1.82	0.64	2.38	0.09	2.47	0.31	1.81	0.64	2.50	0.03	3.39	35.88
50%	0.75	1.94	0.77	2.75	0.39	5.47	0.62	1.90	0.64	3.12	0.22	6.22	0.50	1.87	0.52	3.75	0.06	7.58	18.12
80%	2.01	2.74	1.39	11.00	0.46	8.13	2.15	2.85	1.39	11.25	0.35	8.56	2.47	3.11	1.14	13.00	0.08	11.06	7.00
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.43	1.84	0.64	2.50	0.06	2.26	0.43	1.84	0.64	2.50	0.06	2.26	0.43	1.84	0.64	2.50	0.04	2.49	36.88
50%	1.08	2.10	0.91	4.25	0.23	3.78	1.34	2.25	0.91	4.75	0.12	4.64	1.28	2.21	0.91	5.12	0.03	5.78	20.38
80%	0.76	1.99	1.08	8.00	0.27	7.49	0.96	2.07	1.08	8.38	0.21	7.77	0.97	2.08	0.95	9.00	0.05	9.72	6.88
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.20	1.79	1.01	2.12	0.26	2.17	-0.14	1.79	0.89	2.38	0.18	2.66	-0.27	1.80	0.89	2.62	0.06	3.85	34.25
50%	-0.02	1.80	1.03	4.00	0.42	4.75	0.17	1.81	0.91	4.25	0.16	5.37	-0.03	1.81	0.65	4.62	0.08	7.02	16.62
80%	-1.08	2.14	0.95	9.00	0.35	7.83	-1.08	2.14	0.95	9.00	0.19	8.17	-1.17	2.19	0.83	10.00	0.06	9.75	7.38
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.06	1.78	0.76	1.62	0.17	2.77	-0.01	1.78	0.63	1.62	0.08	3.16	-0.07	1.78	0.51	1.88	0.06	3.48	36.75
50%	-0.41	1.84	1.03	4.25	0.42	4.78	-0.67	1.92	0.78	4.50	0.17	5.88	-0.95	2.05	0.52	5.25	0.07	7.18	18.88
80%	-1.34	2.27	0.95	8.50	0.50	7.27	-1.27	2.24	0.95	8.62	0.45	7.46	-1.39	2.32	0.83	10.62	0.06	10.50	8.25

Table S.A.21: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95					
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
CLASSICAL MEASUREMENT ERROR																			
20%	-0.85	1.36	10.64	2.20	0.46	11.58	-0.87	1.38	10.52	2.20	0.43	11.72	-0.63	1.25	8.54	2.60	0.07	15.08	33.60
50%	-0.90	1.40	11.40	4.05	1.07	17.46	-0.78	1.33	10.25	4.15	0.57	19.79	-0.63	1.26	8.37	4.70	0.14	22.84	15.30
80%	-1.01	1.50	10.87	8.95	1.13	24.14	-1.19	1.63	9.86	9.00	0.59	25.53	-1.11	1.59	7.49	9.80	0.14	30.01	3.75
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.30	1.11	10.95	3.20	0.68	8.66	-0.42	1.16	9.95	3.20	0.30	10.26	-0.06	1.09	8.59	3.70	0.07	12.52	34.75
50%	-0.04	1.07	11.28	4.05	1.14	15.34	0.01	1.08	10.37	4.10	0.70	17.07	0.50	1.21	8.71	5.20	0.19	20.49	18.40
80%	1.24	1.66	11.69	9.70	0.71	22.59	1.23	1.66	11.41	9.90	0.61	22.98	1.22	1.66	8.70	10.85	0.14	27.44	7.20
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-0.55	1.20	10.57	2.25	0.63	10.51	-0.59	1.23	9.46	2.35	0.29	12.19	-0.21	1.11	7.97	2.95	0.07	14.63	36.00
50%	-0.42	1.15	12.45	4.70	1.14	17.22	-0.42	1.16	11.84	5.05	0.71	19.03	-0.18	1.11	10.10	6.10	0.14	22.97	18.95
80%	0.82	1.37	10.94	8.80	0.77	21.01	0.78	1.35	10.74	8.95	0.69	21.33	0.96	1.48	7.89	10.05	0.16	26.21	8.25
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-1.02	1.48	10.32	2.20	0.59	9.42	-0.98	1.45	9.07	2.25	0.23	11.16	-0.79	1.34	8.11	2.55	0.06	12.73	33.60
50%	-1.59	1.92	11.91	4.25	1.08	19.76	-1.58	1.91	11.60	4.70	0.88	20.49	-1.55	1.89	9.27	5.55	0.14	25.77	17.45
80%	-1.92	2.21	12.10	9.55	0.71	24.63	-1.87	2.17	11.72	9.60	0.61	24.97	-1.55	1.92	8.91	10.60	0.14	29.60	7.40
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-1.18	1.59	10.12	2.30	0.65	10.10	-1.25	1.65	8.95	2.30	0.27	11.88	-0.96	1.45	7.66	2.90	0.05	14.18	36.65
50%	-1.46	1.81	12.64	4.95	1.08	16.65	-1.49	1.84	11.87	5.35	0.73	18.08	-1.66	1.99	10.14	6.50	0.14	22.11	19.10
80%	-3.15	3.34	11.60	10.80	1.11	24.61	-3.13	3.32	10.69	11.00	0.59	26.07	-3.12	3.32	8.39	12.05	0.13	30.91	7.90

Table S.A.22: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95									
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact					
CLASSICAL MEASUREMENT ERROR																			
20%	-0.01	0.71	2.21	1.78	0.23	4.24	-0.06	0.71	2.11	1.82	0.15	4.54	-0.02	0.71	1.73	2.26	0.04	5.80	34.12
50%	-0.25	0.75	3.15	3.46	0.59	5.78	-0.32	0.78	3.05	4.02	0.17	6.74	-0.21	0.74	2.49	4.36	0.10	8.49	15.46
80%	-0.21	0.75	3.15	6.66	0.72	11.09	-0.28	0.78	2.94	7.68	0.32	12.68	-0.36	0.81	2.67	8.30	0.12	14.44	4.56
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	0.23	0.74	2.53	2.18	0.24	3.80	0.25	0.75	2.43	2.20	0.16	4.00	0.29	0.77	1.98	2.82	0.05	5.32	34.98
50%	0.59	0.92	3.31	4.32	0.74	7.05	0.76	1.04	2.90	5.04	0.32	8.73	0.92	1.17	2.50	5.52	0.10	10.56	18.50
80%	1.81	1.95	3.10	8.70	0.49	10.51	1.97	2.10	2.84	9.70	0.32	11.65	2.03	2.16	2.12	10.40	0.09	13.81	6.80
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.19	0.73	2.64	2.50	0.40	3.88	0.23	0.74	2.31	2.54	0.17	4.65	0.40	0.81	2.00	3.12	0.05	6.04	36.34
50%	0.59	0.93	3.02	4.30	0.70	7.24	0.64	0.96	2.71	5.08	0.35	8.59	0.77	1.05	2.18	5.60	0.10	10.70	18.60
80%	1.10	1.32	3.04	8.74	0.62	9.76	1.25	1.45	2.82	9.78	0.27	11.02	1.40	1.59	2.29	10.24	0.09	12.95	7.22
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.03	0.71	2.74	2.20	0.50	3.49	-0.01	0.71	2.24	2.22	0.15	4.76	-0.02	0.71	1.80	2.66	0.04	6.00	34.66
50%	-0.15	0.72	3.26	3.76	0.72	7.05	-0.24	0.75	2.93	4.42	0.34	8.41	-0.17	0.74	2.28	4.90	0.10	10.43	16.18
80%	-0.78	1.07	3.66	8.36	0.84	11.76	-0.85	1.12	3.43	9.34	0.36	13.40	-0.75	1.05	2.91	9.86	0.12	15.50	7.40
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.00	0.70	2.70	1.92	0.51	3.21	0.01	0.71	2.22	2.00	0.18	4.31	0.10	0.72	1.85	2.54	0.04	5.64	34.88
50%	-0.68	0.98	3.25	4.24	0.75	6.47	-0.72	1.02	2.91	5.26	0.33	8.16	-0.75	1.04	2.40	5.78	0.10	10.05	17.84
80%	-0.86	1.12	3.31	8.80	0.53	9.38	-0.94	1.19	3.12	9.88	0.32	10.63	-0.89	1.16	2.33	10.42	0.09	12.69	7.80

Table S.A.23: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

	Bias	Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95				25					
		RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact			
CLASSICAL MEASUREMENT ERROR																			
20%	-0.05	0.56	0.51	1.88	0.17	2.09	-0.04	0.56	0.46	1.94	0.10	2.39	-0.01	0.56	0.43	2.11	0.06	2.75	35.30
50%	0.15	0.58	0.82	2.96	0.50	3.61	0.14	0.58	0.68	3.40	0.16	4.89	0.15	0.59	0.54	3.79	0.06	6.00	15.06
80%	-0.06	0.58	0.77	6.06	0.40	7.16	-0.12	0.59	0.68	6.38	0.28	7.62	-0.12	0.59	0.43	7.45	0.06	9.72	4.16
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	0.31	0.64	0.61	2.29	0.18	2.21	0.36	0.67	0.57	2.39	0.12	2.59	0.40	0.69	0.47	2.58	0.06	3.09	35.88
50%	0.82	1.00	0.89	3.80	0.47	4.16	0.98	1.13	0.73	4.28	0.15	5.65	1.13	1.27	0.60	4.67	0.06	6.75	18.71
80%	1.41	1.52	0.85	7.85	0.42	7.55	1.46	1.57	0.77	8.25	0.32	8.24	1.58	1.68	0.59	9.50	0.06	10.43	8.14
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.29	0.63	0.56	2.08	0.23	2.36	0.33	0.65	0.47	2.14	0.12	2.83	0.35	0.67	0.46	2.42	0.06	3.32	36.76
50%	0.73	0.92	0.90	3.84	0.51	3.91	0.87	1.04	0.73	4.33	0.19	5.57	0.96	1.11	0.60	4.85	0.07	6.80	18.88
80%	1.33	1.45	1.01	8.12	0.64	7.76	1.35	1.47	0.96	8.53	0.38	8.59	1.60	1.71	0.68	9.89	0.07	11.20	7.25
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.00	0.56	0.68	1.99	0.20	2.16	0.01	0.56	0.62	2.10	0.11	2.50	0.03	0.56	0.55	2.24	0.06	2.93	34.95
50%	-0.11	0.58	0.86	3.58	0.39	4.27	-0.03	0.57	0.71	3.86	0.15	5.45	-0.04	0.57	0.60	4.25	0.06	6.45	17.34
80%	-0.70	0.91	0.99	7.81	0.40	8.01	-0.61	0.84	0.92	8.12	0.30	8.66	-0.66	0.88	0.69	9.41	0.06	10.95	7.75
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-0.11	0.57	0.58	1.81	0.22	2.22	-0.10	0.57	0.52	1.88	0.11	2.67	-0.11	0.57	0.47	2.10	0.06	3.12	35.91
50%	-0.30	0.64	0.86	3.95	0.43	4.46	-0.34	0.67	0.80	4.49	0.16	5.14	-0.43	0.71	0.61	5.03	0.08	6.63	18.21
80%	-1.03	1.18	1.08	8.06	0.44	7.80	-1.08	1.23	0.95	8.40	0.36	8.39	-1.13	1.27	0.65	9.92	0.06	10.98	7.74

Table S.A.24: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95									
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact				
CLASSICAL MEASUREMENT ERROR																			
20%	-0.23	0.42	7.43	2.42	0.57	9.43	-0.18	0.39	6.80	2.47	0.24	10.97	-0.21	0.41	6.01	2.91	0.07	12.78	34.57
50%	-0.40	0.52	8.83	4.06	1.09	15.89	-0.35	0.49	7.99	4.25	0.59	17.89	-0.22	0.41	6.53	5.03	0.13	21.42	15.05
80%	-0.21	0.41	8.29	8.44	1.12	22.28	-0.21	0.41	7.53	8.67	0.59	23.79	-0.15	0.39	5.64	9.58	0.13	28.43	4.14
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.12	0.36	7.80	2.36	0.68	9.05	-0.04	0.35	7.14	2.43	0.28	10.79	0.05	0.35	6.20	2.90	0.07	12.76	35.70
50%	0.73	0.81	9.06	5.10	1.14	14.37	0.81	0.88	8.21	5.42	0.67	16.24	1.11	1.16	6.91	6.25	0.16	19.74	18.34
80%	1.83	1.87	8.54	10.11	0.74	23.72	1.90	1.93	8.25	10.37	0.62	24.17	2.12	2.15	6.36	11.42	0.14	28.70	7.33
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-0.03	0.34	7.92	2.33	0.64	9.14	0.04	0.35	7.25	2.41	0.28	10.82	0.15	0.38	6.41	2.89	0.07	12.81	35.51
50%	0.78	0.86	9.32	5.05	1.17	14.97	0.82	0.89	8.58	5.27	0.70	16.84	0.99	1.05	7.17	6.31	0.17	20.39	18.64
80%	1.23	1.28	8.73	10.47	0.75	21.89	1.26	1.31	8.48	10.73	0.64	22.29	1.49	1.54	6.62	11.81	0.15	26.85	7.75
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.29	0.45	7.68	2.09	0.65	9.09	-0.27	0.44	6.93	2.17	0.25	10.90	-0.27	0.44	6.12	2.59	0.07	12.82	35.45
50%	-0.56	0.66	9.12	4.54	1.10	15.97	-0.56	0.66	8.22	4.72	0.66	17.81	-0.56	0.66	6.72	5.61	0.14	21.54	16.59
80%	-1.17	1.22	8.79	9.77	0.73	22.40	-1.16	1.22	8.60	10.05	0.61	22.81	-1.17	1.22	6.76	11.09	0.14	27.29	7.62
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-0.41	0.53	7.68	2.36	0.59	9.63	-0.35	0.49	7.03	2.42	0.24	11.27	-0.37	0.51	6.19	2.87	0.07	13.15	35.19
50%	-0.70	0.78	9.26	4.81	1.07	16.91	-0.77	0.84	8.57	5.11	0.68	18.68	-0.83	0.90	7.04	6.06	0.15	22.39	18.00
80%	-1.36	1.40	8.66	10.48	0.77	22.81	-1.38	1.42	8.46	10.73	0.66	23.20	-1.35	1.39	6.73	11.94	0.16	27.87	7.97

Table S.A.25: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets of 100,000 records each. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95						
	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
CLASSICAL MEASUREMENT ERROR																			
20%	-0.07	0.23	1.27	2.09	0.23	3.78	-0.07	0.23	1.20	2.11	0.18	3.97	-0.05	0.23	0.98	2.58	0.05	5.22	34.68
50%	-0.02	0.23	1.53	3.49	0.49	5.97	-0.06	0.23	1.43	3.95	0.35	6.68	-0.05	0.23	1.13	4.28	0.10	8.55	14.77
80%	-0.07	0.24	1.54	6.69	0.68	9.80	-0.05	0.24	1.35	7.63	0.28	11.31	-0.03	0.23	1.13	8.28	0.13	12.68	4.35
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	0.20	0.30	1.36	2.09	0.38	3.75	0.24	0.33	1.21	2.15	0.17	4.54	0.25	0.34	0.98	2.56	0.04	5.79	35.76
50%	0.93	0.96	1.66	4.48	0.65	5.99	1.04	1.06	1.47	5.05	0.33	7.15	1.16	1.18	1.17	5.57	0.10	8.97	18.55
80%	1.61	1.62	1.84	8.56	0.75	9.99	1.82	1.83	1.63	9.56	0.30	11.59	1.85	1.87	1.26	10.12	0.08	13.83	7.73
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.17	0.28	1.39	2.13	0.38	3.48	0.22	0.31	1.23	2.21	0.17	4.21	0.26	0.34	1.00	2.63	0.05	5.41	35.68
50%	0.73	0.77	1.64	4.42	0.62	6.03	0.81	0.84	1.50	4.96	0.33	7.07	0.92	0.95	1.21	5.40	0.10	8.88	18.65
80%	1.36	1.38	1.78	8.65	0.56	9.73	1.49	1.51	1.62	9.62	0.31	11.23	1.52	1.54	1.23	10.14	0.08	13.47	7.97
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	-0.10	0.25	1.34	2.00	0.26	3.53	-0.09	0.24	1.18	2.02	0.18	4.26	-0.09	0.24	0.94	2.35	0.04	5.48	34.84
50%	-0.21	0.31	1.64	3.69	0.59	6.25	-0.24	0.33	1.49	4.22	0.31	7.33	-0.25	0.34	1.20	4.65	0.09	9.19	16.74
80%	-0.63	0.67	1.76	8.08	0.56	10.34	-0.71	0.75	1.60	9.11	0.31	11.81	-0.71	0.75	1.41	9.71	0.08	13.39	7.67
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-0.14	0.26	1.37	2.17	0.39	3.40	-0.13	0.26	1.20	2.22	0.16	4.17	-0.15	0.27	0.99	2.57	0.05	5.24	35.24
50%	-0.47	0.52	1.68	4.13	0.63	6.17	-0.51	0.56	1.52	4.67	0.33	7.31	-0.53	0.58	1.21	5.15	0.10	9.22	18.47
80%	-1.14	1.16	1.82	8.79	0.58	9.98	-1.29	1.31	1.63	9.84	0.31	11.55	-1.34	1.36	1.28	10.44	0.08	13.75	8.23

Table S.A.26: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets of 100,000 records each. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95						
	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
CLASSICAL MEASUREMENT ERROR																			
20%	0.06	0.19	0.16	2.01	0.20	2.38	0.06	0.19	0.13	2.08	0.10	2.82	0.06	0.19	0.12	2.23	0.06	3.20	34.59
50%	0.03	0.18	0.20	3.08	0.45	3.80	0.05	0.19	0.18	3.57	0.15	5.08	0.03	0.18	0.15	3.91	0.07	6.03	15.03
80%	-0.03	0.19	0.24	6.46	0.46	7.81	-0.03	0.19	0.22	6.82	0.33	8.57	-0.07	0.20	0.18	8.24	0.09	10.57	4.38
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	0.25	0.30	0.15	2.13	0.19	2.45	0.27	0.33	0.14	2.18	0.11	2.79	0.31	0.35	0.12	2.40	0.06	3.26	35.93
50%	0.88	0.90	0.20	4.10	0.46	4.51	1.03	1.05	0.18	4.57	0.28	5.21	1.16	1.18	0.17	5.10	0.09	6.69	18.27
80%	1.77	1.78	0.30	8.06	0.62	7.93	1.81	1.81	0.27	8.47	0.36	8.75	2.05	2.06	0.20	9.88	0.07	11.30	7.63
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.26	0.32	0.16	2.11	0.21	2.49	0.27	0.33	0.14	2.15	0.12	2.90	0.32	0.37	0.13	2.39	0.06	3.43	35.73
50%	0.85	0.87	0.20	4.18	0.45	4.27	0.99	1.01	0.16	4.69	0.15	5.69	1.08	1.10	0.15	5.26	0.06	6.58	18.76
80%	1.37	1.38	0.27	8.24	0.49	7.61	1.40	1.41	0.22	8.61	0.34	8.45	1.55	1.57	0.17	9.97	0.07	10.80	7.92
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	0.02	0.18	0.15	2.04	0.19	2.40	0.02	0.18	0.13	2.11	0.10	2.81	0.02	0.18	0.11	2.28	0.06	3.17	35.13
50%	-0.10	0.20	0.22	3.42	0.42	4.18	-0.14	0.23	0.17	3.84	0.15	5.50	-0.18	0.25	0.16	4.32	0.08	6.32	16.81
80%	-0.45	0.49	0.30	7.66	0.51	7.71	-0.47	0.51	0.27	8.02	0.33	8.49	-0.56	0.59	0.19	9.45	0.07	10.97	7.68
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-0.03	0.18	0.16	2.04	0.19	2.35	-0.04	0.18	0.14	2.12	0.11	2.77	-0.04	0.18	0.13	2.32	0.06	3.19	35.24
50%	-0.32	0.37	0.24	3.91	0.45	4.33	-0.38	0.42	0.22	4.39	0.28	5.00	-0.41	0.45	0.18	4.89	0.08	6.43	18.46
80%	-0.89	0.91	0.31	8.38	0.51	7.84	-0.90	0.92	0.27	8.75	0.34	8.57	-1.04	1.06	0.18	10.15	0.07	11.07	8.24

Table S.A.27: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets of 100,000 records each. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered.

Threshold 1: Posterior ≥ 0.75								Threshold 2: Posterior ≥ 0.85								Threshold 3: Posterior ≥ 0.95								
		Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact		
CLASSICAL MEASUREMENT ERROR																								
20%	-1.72	3.76	13.33	2.50	1.16	21.08	-2.18	4.03	10.96	2.50	0.52	23.26	-1.27	3.65	9.30	2.50	0.23	25.47	34.50					
50%	-0.61	3.40	13.39	3.00	1.40	48.28	-1.50	3.73	10.65	3.50	0.49	50.25	-0.54	3.52	8.17	4.50	0.19	52.13	10.50					
80%	-1.26	3.67	13.27	8.50	1.50	58.82	-0.52	3.55	11.76	10.00	0.82	60.10	-0.47	3.63	9.28	12.00	0.39	61.83	4.50					
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																								
20%	-0.39	3.36	12.00	1.00	0.48	22.35	0.07	3.35	11.21	1.00	0.34	22.89	0.08	3.37	10.86	1.50	0.21	24.12	37.00					
50%	-1.29	3.49	18.41	2.50	1.83	45.78	-1.29	3.53	16.31	2.50	1.12	47.67	-0.08	3.44	12.26	7.00	0.34	52.62	1.50					
80%	-2.01	4.09	11.11	12.00	1.06	45.79	-2.27	4.25	9.74	12.00	0.63	46.86	-2.56	4.46	7.45	13.00	0.24	49.32	6.00					
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																								
20%	-0.83	3.44	13.33	2.50	0.63	35.06	-1.28	3.59	12.56	2.50	0.50	35.53	-1.04	3.55	11.93	4.00	0.23	37.56	34.50					
50%	-1.92	3.77	100.00	100.00	14.37	80.83	-1.50	5.51	100.00	100.00	100.00	100.00	-0.52	3.55	10.78	9.00	0.19	46.17	15.50					
80%	-0.55	3.50	13.33	9.00	1.04	48.65	-0.30	3.48	12.92	9.00	0.68	49.75	1.32	3.82	10.77	13.00	0.24	53.06	11.00					
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																								
20%	-0.20	3.31	14.78	2.00	1.07	25.40	-0.15	3.37	12.61	3.00	0.34	27.70	0.33	3.41	11.47	3.50	0.23	28.88	35.50					
50%	-2.17	4.00	17.04	7.50	1.31	46.21	-2.64	4.29	15.98	8.00	0.83	47.35	-3.21	4.75	12.68	10.50	0.18	51.46	16.50					
80%	-2.18	4.03	15.98	8.00	1.55	56.08	-2.68	4.37	13.74	9.00	0.77	57.94	-2.74	4.47	10.45	10.00	0.32	60.66	8.00					
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																								
20%	-2.58	4.19	16.88	4.00	1.25	26.87	-1.04	3.55	12.39	4.50	0.34	30.57	-1.27	3.66	10.80	5.00	0.14	32.57	37.00					
50%	-2.19	4.05	11.52	4.00	0.97	40.23	-2.20	4.08	10.33	4.50	0.60	41.47	-2.47	4.28	10.19	7.50	0.33	43.31	3.50					
80%	-2.94	4.55	12.98	9.50	1.82	46.35	-3.00	4.64	11.50	11.50	1.13	48.55	-2.29	4.29	7.85	12.00	0.43	52.39	0.50					

Table S.A.28: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95										
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
CLASSICAL MEASUREMENT ERROR																				
20%	-0.49	2.27	4.52	2.80	0.32	11.00	-0.49	2.28	4.34	3.00	0.26	11.28	-0.80	2.37	3.59	3.20	0.10	12.84	35.20	
50%	0.00	2.22	5.93	4.80	0.48	19.86	0.20	2.24	5.18	4.80	0.28	20.68	0.40	2.28	4.44	5.20	0.16	21.52	14.60	
80%	0.51	2.32	5.50	7.20	0.95	31.02	0.10	2.28	3.95	7.60	0.36	32.81	0.32	2.33	2.76	8.40	0.16	34.39	4.40	
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	0.19	2.21	4.46	1.40	0.39	7.90	0.00	2.21	3.91	1.60	0.12	8.90	0.10	2.22	3.54	1.80	0.08	9.84	34.60	
50%	1.60	2.75	5.20	5.20	0.47	19.28	1.61	2.77	4.44	5.20	0.26	20.04	1.95	2.99	3.70	6.20	0.13	21.49	16.80	
80%	3.07	3.83	5.07	10.20	0.92	28.26	3.26	4.01	4.13	11.80	0.31	30.24	3.20	3.97	3.53	12.60	0.14	31.72	2.40	
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	0.49	2.27	5.09	3.00	0.65	11.15	0.60	2.31	4.18	3.80	0.22	12.95	0.40	2.28	3.43	4.20	0.11	14.19	35.60	
50%	1.89	2.92	4.57	4.00	0.83	17.46	2.01	3.01	3.61	4.00	0.55	18.67	1.98	3.03	2.30	6.40	0.08	22.25	19.20	
80%	1.41	2.65	4.44	5.20	0.86	24.12	1.74	2.85	3.89	6.00	0.60	25.20	1.70	2.87	2.77	8.60	0.19	27.90	9.60	
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	-0.20	2.22	3.91	1.60	0.33	9.80	-3.21	5.78	100.00	100.00	13.16	98.64	0.10	2.23	3.17	2.20	0.09	11.61	37.00	
50%	-0.20	2.24	5.16	4.40	0.80	17.41	-0.81	2.39	4.05	5.20	0.24	19.56	-0.61	2.34	3.86	5.40	0.20	19.99	16.60	
80%	0.00	2.25	6.65	7.40	0.67	34.10	0.00	2.26	5.89	7.40	0.66	36.19	-0.10	2.29	5.24	9.60	0.20	38.77	2.20	
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	-0.49	2.26	3.88	1.00	0.39	6.43	-0.68	2.32	3.52	1.40	0.21	7.26	-0.50	2.29	1.99	1.40	0.05	9.59	32.40	
50%	-1.29	2.58	5.17	4.60	0.47	24.15	-1.20	2.55	4.62	5.00	0.28	24.86	-1.41	2.65	4.64	5.40	0.16	26.07	16.40	
80%	0.32	2.32	2.96	8.20	0.76	27.71	0.11	2.31	2.77	8.80	0.51	28.41	-0.88	2.51	1.55	11.00	0.19	31.22	8.80	

Table S.A.29: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95										
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
CLASSICAL MEASUREMENT ERROR																				
20%	0.37	1.82	0.38	1.88	0.17	4.39	0.31	1.81	0.25	1.88	0.09	4.79	0.24	1.81	0.26	2.50	0.04	5.33	33.88	
50%	-0.34	1.82	0.51	2.88	0.28	11.26	-0.27	1.81	0.51	3.00	0.14	11.79	-0.34	1.82	0.39	3.00	0.08	12.30	14.00	
80%	-0.30	1.85	0.93	6.62	0.49	19.51	-0.11	1.83	0.80	7.12	0.36	20.14	0.08	1.85	0.41	8.62	0.08	22.41	4.00	
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	0.62	1.88	2.01	2.25	9.38	8.98	0.50	1.85	1.02	2.50	0.21	39.74	0.62	1.90	0.64	3.12	0.06	41.13	35.88	
50%	0.69	1.91	0.76	2.62	0.47	9.95	0.56	1.88	0.64	3.00	0.29	10.67	0.62	1.90	0.52	3.75	0.13	12.07	18.12	
80%	1.99	2.72	1.10	9.75	0.80	19.13	2.08	2.79	1.11	10.62	0.48	20.35	2.68	3.28	0.85	12.62	0.13	23.72	2.62	
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	0.37	1.82	0.76	2.50	0.13	4.85	0.43	1.84	0.76	2.62	0.09	5.05	0.50	1.85	0.77	2.75	0.07	5.37	36.88	
50%	1.01	2.06	0.90	4.12	0.38	11.32	1.21	2.17	0.78	4.38	0.15	12.31	1.34	2.25	0.78	5.12	0.08	13.15	3.50	
80%	1.09	2.13	1.60	7.62	0.70	22.02	1.03	2.11	1.21	8.38	0.25	23.63	1.03	2.11	1.09	9.00	0.11	24.64	2.00	
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	-0.13	1.78	1.14	2.12	0.30	6.09	-0.13	1.78	1.01	2.25	0.22	6.55	-0.27	1.81	0.77	2.75	0.07	8.04	34.25	
50%	-0.02	1.79	1.16	3.88	0.55	11.13	0.04	1.80	0.91	4.25	0.19	12.47	-0.09	1.81	0.78	4.62	0.11	13.17	16.62	
80%	-1.20	2.20	1.22	8.75	0.61	17.24	-1.07	2.13	1.09	8.88	0.32	18.29	-1.09	2.15	0.96	10.00	0.11	19.93	1.75	
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	-0.13	1.78	0.51	1.75	0.15	7.47	-0.13	1.78	0.51	1.75	0.13	7.56	-0.07	1.78	0.51	2.12	0.06	8.28	36.75	
50%	-0.54	1.88	0.78	4.25	0.39	11.79	-0.48	1.86	0.78	4.38	0.24	12.43	-0.95	2.05	0.66	5.62	0.12	13.65	18.88	
80%	-1.33	2.27	1.08	8.38	0.58	16.82	-1.41	2.32	0.95	8.62	0.48	17.34	-1.39	2.32	0.83	10.62	0.12	19.90	8.25	

Table S.A.30: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 1,000 records. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95										
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
CLASSICAL MEASUREMENT ERROR																				
20%	0.41	1.15	8.82	2.25	0.79	6.82	-0.41	1.15	8.82	2.25	0.79	6.82	-0.10	1.12	3.00	3.10	0.09	13.76	33.60	
50%	-0.60	1.25	7.59	4.40	0.93	9.46	-0.60	1.25	7.59	4.40	0.93	9.46	-0.39	1.20	2.71	6.55	0.15	16.82	15.30	
80%	-1.06	1.54	7.84	8.90	0.80	16.12	-1.06	1.54	7.84	8.90	0.80	16.11	-0.88	1.45	5.61	10.85	0.38	19.87	3.05	
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	0.08	1.09	8.27	3.45	0.37	5.59	0.08	1.09	8.27	3.45	0.37	5.59	0.65	1.30	2.20	4.30	0.10	11.88	34.75	
50%	0.62	1.26	7.99	4.40	0.91	10.75	0.62	1.26	7.99	4.40	0.91	10.74	1.92	2.22	6.35	7.75	0.16	15.70	3.20	
80%	1.11	1.58	8.68	9.55	1.00	18.71	1.11	1.58	8.68	9.55	1.00	18.71	1.25	1.70	5.56	11.60	0.41	23.79	2.10	
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	-0.11	1.09	7.51	2.65	0.95	5.67	-0.11	1.09	7.51	2.65	0.95	5.67	0.30	1.16	2.87	3.60	0.13	11.70	36.00	
50%	0.10	1.10	9.33	5.30	1.11	10.53	0.10	1.10	9.33	5.30	1.11	10.53	0.97	1.50	3.23	8.50	0.15	19.87	2.85	
80%	1.07	1.55	7.39	8.55	1.03	15.96	1.07	1.55	7.39	8.55	1.03	15.97	1.94	2.26	3.17	11.40	0.34	22.74	1.80	
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	-0.53	1.21	7.13	2.35	1.32	5.93	-0.53	1.21	7.13	2.35	1.32	5.93	-0.20	1.14	2.02	2.85	0.09	11.80	33.60	
50%	-1.02	1.49	8.22	4.55	0.79	12.37	-1.02	1.49	8.22	4.55	0.79	12.36	-1.24	1.67	6.43	6.80	0.29	16.29	17.45	
80%	-1.65	1.99	9.02	9.20	1.15	16.60	-1.65	1.99	9.02	9.20	1.15	16.61	-0.81	1.42	3.35	12.10	0.33	24.53	2.00	
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	-1.01	1.49	7.37	2.60	0.41	4.96	-1.01	1.49	7.37	2.60	0.41	4.96	-0.31	1.17	2.34	3.90	0.09	11.18	36.65	
50%	-1.42	1.79	8.84	5.70	0.75	13.21	-1.42	1.79	8.84	5.70	0.75	13.20	-2.22	2.49	8.15	8.75	0.24	16.95	19.10	
80%	-2.73	2.95	8.09	10.80	1.21	15.67	-2.73	2.95	8.09	10.80	1.21	15.68	-2.29	2.57	3.39	13.00	0.36	22.57	1.55	

Table S.A.31: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.

	Threshold 1: Posterior ≥ 0.75						Threshold 2: Posterior ≥ 0.85						Threshold 3: Posterior ≥ 0.95						
	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
CLASSICAL MEASUREMENT ERROR																			
20%	0.07	0.71	0.83	1.92	0.24	3.11	0.07	0.72	0.51	2.10	0.13	3.64	0.13	0.73	0.35	2.58	0.05	4.44	34.12
50%	-0.20	0.74	1.88	3.88	0.59	4.77	-0.22	0.75	1.13	4.12	0.26	6.13	-0.08	0.73	0.90	5.06	0.12	7.41	3.66
80%	0.00	0.72	1.97	6.58	0.83	8.24	-0.18	0.75	1.33	7.66	0.39	10.05	-0.21	0.77	0.87	8.90	0.16	11.98	2.70
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	0.37	0.80	0.75	2.36	0.19	2.87	0.37	0.80	0.55	2.54	0.14	3.28	0.49	0.87	0.54	3.36	0.06	4.13	2.00
50%	0.87	1.13	0.96	4.84	0.48	5.84	1.02	1.25	0.76	5.40	0.25	6.69	1.05	1.28	0.51	6.28	0.11	7.98	2.80
80%	1.88	2.01	2.14	8.68	0.70	10.22	2.04	2.17	1.94	9.86	0.51	11.39	2.20	2.32	0.85	11.14	0.16	14.24	6.80
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	0.31	0.78	0.92	2.56	0.35	2.83	0.43	0.84	0.68	2.94	0.13	3.54	0.57	0.92	0.35	3.64	0.05	4.60	36.34
50%	0.73	1.02	2.14	4.94	0.82	5.70	0.86	1.12	1.62	5.42	0.50	6.85	1.19	1.40	0.66	6.74	0.16	9.73	2.64
80%	1.13	1.34	1.68	8.62	0.82	9.85	1.40	1.58	1.03	9.74	0.34	11.71	1.58	1.75	0.69	11.04	0.17	13.39	1.56
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																			
20%	0.06	0.72	0.47	2.38	0.18	1.99	0.09	0.72	0.41	2.58	0.13	2.22	0.08	0.72	0.10	3.10	0.04	3.28	34.66
50%	-0.10	0.72	2.10	4.14	0.71	5.74	-0.08	0.72	1.77	4.72	0.41	6.97	-0.19	0.75	0.86	5.74	0.14	9.49	2.88
80%	-0.66	0.98	2.32	8.30	0.93	10.42	-0.77	1.06	1.71	9.34	0.42	12.32	-0.73	1.04	0.80	10.54	0.16	14.77	1.60
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																			
20%	-0.00	0.71	0.67	2.12	0.27	2.81	0.03	0.71	0.43	2.36	0.12	3.36	0.03	0.72	0.35	2.94	0.06	4.00	34.88
50%	-0.69	1.00	2.14	5.06	0.73	5.71	-0.67	0.98	1.73	5.46	0.28	6.81	-0.78	1.07	0.85	6.34	0.15	8.99	2.70
80%	-0.75	1.05	2.19	8.74	0.91	10.12	-0.85	1.12	1.64	9.82	0.46	12.05	-0.98	1.23	0.74	11.18	0.16	14.63	1.90

Table S.A.32: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.

	Bias	Threshold 1: Posterior ≥ 0.75			Threshold 2: Posterior ≥ 0.85			Threshold 3: Posterior ≥ 0.95			CLASSICAL MEASUREMENT ERROR		
		RMSE	FDR	\widehat{FDR}	Bias	RMSE	FDR	\widehat{FDR}	Bias	RMSE	FDR	\widehat{FDR}	\widehat{FNR}
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE													
20%	-0.02	0.56	0.43	1.95	0.36	2.01	0.02	0.56	0.22	2.03	0.11	3.01	0.03
50%	0.17	0.59	0.59	3.01	0.55	3.60	0.22	0.61	0.31	3.62	0.17	5.02	0.19
80%	-0.02	0.57	0.42	6.08	0.33	6.73	-0.08	0.58	0.33	6.39	0.29	7.13	-0.11
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE													
20%	0.38	0.68	0.23	2.33	0.16	1.06	0.46	0.73	0.13	2.55	0.07	1.51	0.59
50%	0.91	1.07	0.58	3.76	0.61	3.54	1.17	1.30	0.30	4.42	0.21	5.01	1.32
80%	1.50	1.61	0.30	7.84	0.45	7.98	1.55	1.66	0.24	8.20	0.34	8.42	1.76
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE													
20%	0.42	0.70	0.43	2.33	0.44	1.98	0.43	0.71	0.19	2.44	0.13	2.99	0.51
50%	0.76	0.95	0.58	3.81	0.63	3.72	1.01	1.16	0.43	4.66	0.24	5.42	1.18
80%	1.42	1.54	0.32	7.99	0.51	7.64	1.39	1.51	0.27	8.39	0.35	8.27	1.78
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE													
20%	0.04	0.56	0.17	2.01	0.22	0.94	0.01	0.56	0.08	2.21	0.09	1.42	0.03
50%	-0.07	0.57	0.44	3.53	0.46	4.11	-0.05	0.57	0.36	3.99	0.21	4.94	-0.12
80%	-0.63	0.86	0.56	7.58	0.61	7.68	-0.62	0.85	0.39	8.06	0.36	8.61	-0.65
NON-DIFFERENTIAL MEASUREMENT ERROR: STRING-VALUED													
20%	-0.09	0.57	0.20	1.88	0.22	1.34	-0.17	0.59	0.05	2.10	0.08	1.99	-0.21
50%	-0.31	0.65	0.40	4.06	0.42	4.28	-0.33	0.66	0.34	4.69	0.23	5.04	-0.44
80%	-1.02	1.17	0.51	7.96	0.54	7.66	-1.10	1.24	0.41	8.35	0.38	8.32	-1.30

Table S.A.33: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate (\widehat{FDR}), the estimated false negative rate (\widehat{FNR}), and the rate of exact matches (exact), when merging two datasets where one has 100,000 records and the other one has 10,000 records. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95										
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
CLASSICAL MEASUREMENT ERROR																				
20%	-0.06	0.36	0.39	2.77	0.19	2.45	-0.06	0.36	0.38	2.80	0.18	2.48	-0.07	0.37	0.17	3.72	0.06	3.60	4.21	
50%	-0.02	0.36	1.51	4.17	0.56	4.60	0.01	0.36	1.41	4.67	0.43	5.15	0.06	0.37	0.42	6.45	0.13	8.13	3.50	
80%	-0.03	0.37	2.38	8.09	0.85	11.79	-0.02	0.37	1.86	8.70	0.46	12.95	0.01	0.37	1.22	10.83	0.25	15.59	2.44	
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	0.34	0.49	0.48	2.71	0.24	2.82	0.40	0.53	0.43	2.86	0.16	3.03	0.53	0.64	0.29	3.62	0.09	3.90	3.65	
50%	1.20	1.25	1.54	5.49	0.62	5.32	1.38	1.43	1.46	5.94	0.47	5.82	2.17	2.20	0.44	8.56	0.13	9.57	2.96	
80%	2.02	2.06	2.08	9.77	0.86	11.66	2.20	2.23	1.57	10.58	0.51	13.03	2.59	2.62	1.15	12.99	0.27	15.72	1.85	
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	0.39	0.53	0.56	2.72	0.23	2.75	0.41	0.54	0.50	2.82	0.20	2.89	0.47	0.59	0.27	3.58	0.09	3.85	3.98	
50%	1.10	1.16	1.46	5.33	0.68	5.21	1.26	1.31	1.35	5.92	0.55	5.83	1.99	2.02	0.34	8.73	0.15	9.70	2.65	
80%	1.48	1.53	2.51	10.25	0.87	13.37	1.64	1.68	1.93	11.31	0.51	14.94	1.99	2.03	1.32	13.47	0.26	17.60	1.60	
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	0.00	0.36	0.44	2.37	0.21	2.45	0.00	0.36	0.42	2.44	0.18	2.55	-0.04	0.36	0.24	3.20	0.07	3.49	2.42	
50%	-0.11	0.37	1.70	4.72	0.59	6.40	-0.17	0.40	1.41	5.19	0.42	7.13	-0.28	0.46	1.18	7.52	0.14	9.68	3.12	
80%	-0.75	0.83	1.80	9.43	0.77	10.33	-0.81	0.89	1.54	9.89	0.59	11.02	-0.89	0.96	0.86	11.97	0.26	13.91	1.54	
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	-0.17	0.40	0.43	2.77	0.20	2.42	-0.18	0.40	0.43	2.78	0.20	2.45	-0.23	0.43	0.18	3.36	0.08	3.34	3.77	
50%	-0.47	0.60	1.53	5.10	0.63	5.26	-0.54	0.65	1.41	5.62	0.51	5.83	-0.98	1.04	0.55	8.08	0.15	9.30	1.32	
80%	-1.08	1.14	2.56	10.19	0.96	13.82	-1.13	1.19	2.12	10.90	0.58	14.95	-1.33	1.38	1.25	13.02	0.27	18.03	1.65	

Table S.A.34: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets of 100,000 records each. In addition, there is a 20% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95								
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	Exact	
CLASSICAL MEASUREMENT ERROR																		
20%	-0.01	0.23	0.08	2.18	0.14	1.27	-0.02	0.23	0.07	2.43	0.09	1.50	-0.02	0.23	0.05	2.95	0.04	2.43
50%	-0.02	0.23	0.25	3.82	0.31	2.72	-0.05	0.23	0.22	4.15	0.22	3.08	-0.08	0.24	0.08	5.01	0.10	4.44
80%	-0.04	0.23	0.33	6.58	0.54	5.62	-0.04	0.24	0.23	7.59	0.29	6.66	-0.01	0.23	0.17	8.72	0.17	7.92
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																		
20%	0.36	0.43	0.11	2.32	0.15	1.48	0.36	0.43	0.08	2.47	0.11	1.66	0.47	0.52	0.05	3.11	0.04	2.34
50%	1.11	1.13	0.31	4.85	0.44	2.90	1.26	1.28	0.24	5.46	0.28	3.57	1.44	1.46	0.10	6.28	0.14	4.91
80%	1.67	1.69	0.39	8.43	0.61	6.13	1.87	1.88	0.29	9.51	0.33	7.27	2.01	2.02	0.18	10.73	0.17	8.84
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																		
20%	0.31	0.38	0.10	2.38	0.14	1.51	0.29	0.37	0.08	2.49	0.10	1.67	0.42	0.48	0.05	3.15	0.04	2.36
50%	0.90	0.93	0.29	4.77	0.45	3.01	1.03	1.06	0.23	5.39	0.23	3.71	1.16	1.18	0.09	6.20	0.12	5.00
80%	1.40	1.42	0.38	8.51	0.59	6.46	1.52	1.54	0.29	9.56	0.32	7.61	1.60	1.62	0.16	10.75	0.17	9.09
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																		
20%	-0.05	0.23	0.10	2.14	0.15	1.39	-0.07	0.24	0.07	2.36	0.09	1.65	-0.10	0.25	0.05	2.95	0.04	2.27
50%	-0.19	0.30	0.33	3.93	0.38	2.78	-0.20	0.30	0.27	4.40	0.24	3.34	-0.23	0.33	0.11	5.26	0.12	4.63
80%	-0.57	0.62	0.39	7.97	0.59	6.43	-0.66	0.70	0.28	9.11	0.31	7.63	-0.72	0.76	0.17	10.47	0.17	9.25
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																		
20%	-0.12	0.26	0.09	2.38	0.15	1.43	-0.13	0.26	0.08	2.52	0.11	1.60	-0.19	0.29	0.05	3.12	0.04	2.23
50%	-0.42	0.48	0.29	4.43	0.39	2.95	-0.47	0.52	0.22	5.05	0.27	3.59	-0.57	0.61	0.07	5.98	0.14	5.02
80%	-1.07	1.09	0.42	8.64	0.63	6.38	-1.25	1.27	0.30	9.82	0.35	7.62	-1.43	1.45	0.17	11.15	0.18	9.27

Table S.A.35: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), and the rate of exact matches (exact), when merging two datasets of 100,000 records each. In addition, there is a 50% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.

		Threshold 1: Posterior ≥ 0.75				Threshold 2: Posterior ≥ 0.85				Threshold 3: Posterior ≥ 0.95										
		Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Bias	RMSE	FDR	FNR	$\widehat{\text{FDR}}$	$\widehat{\text{FNR}}$	Exact
CLASSICAL MEASUREMENT ERROR																				
20%	0.07	0.19	0.01	2.08	0.12	0.93	0.06	0.19	0.01	2.16	0.09	1.04	0.06	0.19	0.01	2.53	0.04	1.45	2.46	
50%	0.03	0.18	0.05	3.10	0.35	1.89	0.06	0.19	0.04	3.69	0.17	2.53	0.04	0.18	0.02	4.29	0.09	3.40	3.56	
80%	-0.04	0.19	0.08	6.38	0.46	4.99	-0.03	0.19	0.06	6.76	0.34	5.44	-0.09	0.20	0.03	8.75	0.12	7.53	2.58	
DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	0.29	0.34	0.02	2.20	0.15	1.11	0.37	0.41	0.02	2.39	0.07	1.32	0.43	0.47	0.01	2.79	0.04	1.72	2.13	
50%	0.90	0.92	0.05	4.08	0.43	2.20	1.13	1.15	0.04	4.82	0.22	2.97	1.39	1.40	0.02	5.70	0.11	4.12	2.79	
80%	1.79	1.80	0.08	7.97	0.51	5.82	1.83	1.84	0.06	8.39	0.36	6.34	2.17	2.17	0.03	10.15	0.12	8.28	1.67	
DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	0.31	0.36	0.02	2.20	0.15	1.06	0.38	0.42	0.02	2.43	0.07	1.29	0.44	0.47	0.01	2.84	0.04	1.74	2.12	
50%	0.87	0.89	0.05	4.17	0.41	2.29	1.09	1.10	0.04	5.06	0.22	3.19	1.26	1.28	0.01	5.88	0.11	4.28	2.81	
80%	1.37	1.39	0.07	8.14	0.51	5.65	1.41	1.42	0.06	8.53	0.37	6.09	1.66	1.67	0.02	10.25	0.13	8.04	1.63	
NON-DIFFERENTIAL MEASUREMENT ERROR: INDEPENDENCE																				
20%	0.03	0.18	0.02	2.11	0.12	1.08	0.02	0.18	0.02	2.22	0.09	1.21	-0.00	0.18	0.01	2.60	0.04	1.63	2.28	
50%	-0.09	0.20	0.05	3.42	0.38	2.17	-0.16	0.24	0.03	4.18	0.18	2.98	-0.20	0.27	0.02	4.84	0.10	3.89	2.92	
80%	-0.42	0.46	0.08	7.56	0.48	5.65	-0.44	0.48	0.07	7.94	0.36	6.08	-0.59	0.62	0.03	9.72	0.14	8.02	1.64	
NON-DIFFERENTIAL MEASUREMENT ERROR: DEPENDENCE																				
20%	-0.04	0.18	0.02	2.14	0.14	1.02	-0.06	0.19	0.02	2.29	0.09	1.19	-0.09	0.20	0.01	2.71	0.04	1.62	2.20	
50%	-0.30	0.35	0.05	3.90	0.40	2.31	-0.38	0.42	0.04	4.64	0.21	3.08	-0.49	0.52	0.02	5.41	0.11	4.07	2.71	
80%	-0.87	0.89	0.10	8.29	0.50	6.02	-0.88	0.90	0.09	8.69	0.37	6.47	-1.09	1.11	0.03	10.77	0.13	8.77	1.57	

Table S.A.36: The table presents the estimation error (Bias) for the turnout rate, root mean square error (RMSE), the false discovery rate (FDR), the false negative rate (FNR), the estimated false discovery rate ($\widehat{\text{FDR}}$), the estimated false negative rate ($\widehat{\text{FNR}}$), and the rate of exact matches (exact), when merging two datasets of 100,000 records each. In addition, there is a 80% overlap (measured as a percentage of the smaller data set) and five measurement error mechanisms are studied across three different proportions of missing data for the following string-valued linkage fields: first name, last name, and street name. To declare a pair of records to be in the set of matches, three different thresholds are considered. Conditional independence across linkage fields is not assumed and a log-linear model is used to model dependencies among non-matches.