

# Kinetic Sorption Model

## eigen function, (3.14)

$$E_s = ka s \cosh(\sqrt{s}) + \sqrt{s} \sinh(\sqrt{s}) (kd + s)$$

## moments in the Laplace space, (3.13)

$$m0\_hat = \frac{kd \sinh(\sqrt{s}) - ka \sinh(\sqrt{s}) + s \sinh(\sqrt{s}) + ka \sqrt{s} \cosh(\sqrt{s})}{\sqrt{s} (ka s \cosh(\sqrt{s}) + \sqrt{s} \sinh(\sqrt{s}) (kd + s))}$$

$$m1\_hat =$$

$$\left( Pe \left( 8 s^3 \sigma_1 - 48 ka s - 48 ka^2 s - 16 kd s^2 - 8 kd^2 s - 48 ka kd - 8 s^3 + 16 ka^2 s^2 - 42 ka^2 s \sigma_1 + 16 kd s^2 \sigma_1 \right. \right. \\ \left. \left. + 8 kd^2 s \sigma_1 - 48 ka s^{3/2} \sigma_2 + 16 ka s^{5/2} \sigma_2 + 8 ka^2 s^2 \sigma_1 + 45 ka^2 \sqrt{s} \sigma_2 + 48 ka kd \sigma_1 + 48 ka s \sigma_1 \right. \right. \\ \left. \left. - 48 ka kd \sqrt{s} \sigma_2 + 16 ka kd s^{3/2} \sigma_2 \right) \right) / \left( 8 s^3 \left( ka^2 s - 2 kd s + kd^2 \sigma_1 + s^2 \sigma_1 - kd^2 - s^2 + ka^2 s \sigma_1 + 2 ka s^{3/2} \sigma_2 \right. \right. \\ \left. \left. + 2 kd s \sigma_1 + 2 ka kd \sqrt{s} \sigma_2 \right) \right)$$

where

$$\sigma_1 = \cosh(2 \sqrt{s})$$

$$\sigma_2 = \sinh(2 \sqrt{s})$$

$$m2\_hat =$$

$$\left( 320 s^6 \sigma_1 - 960 s^6 \sinh(\sqrt{s}) - 2880 Pe^2 s^{7/2} \cosh(\sqrt{s}) + 8640 Pe^2 kd^3 \sinh(\sqrt{s}) + 8640 Pe^2 s^3 \sinh(\sqrt{s}) \right. \\ \left. + 2880 Pe^2 s^4 \sinh(\sqrt{s}) - 1152 Pe^2 s^5 \sinh(\sqrt{s}) + 960 ka s^{11/2} \sigma_2 + 1120 ka^2 s^{9/2} \cosh(\sqrt{s}) \right. \\ \left. + 1600 ka^3 s^{9/2} \cosh(\sqrt{s}) - 640 ka s^5 \sigma_1 + 1600 ka^2 s^5 \sinh(\sqrt{s}) - 480 ka^3 s^4 \sinh(\sqrt{s}) + 960 kd s^5 \sigma_1 \right. \\ \left. - 2880 kd^2 s^4 \sinh(\sqrt{s}) - 960 kd^3 s^3 \sinh(\sqrt{s}) + 2880 Pe^2 s^{7/2} \sigma_2 - 2880 Pe^2 kd^3 \sigma_1 - 2880 Pe^2 s^3 \sigma_1 \right. \\ \left. - 960 Pe^2 s^4 \sigma_1 + 384 Pe^2 s^5 \sigma_1 - 1120 ka^2 s^{9/2} \sigma_2 + 320 ka^3 s^{9/2} \sigma_2 + 960 ka^2 s^5 \sigma_1 - 480 ka^3 s^4 \sigma_1 \right. \\ \left. + 960 kd^2 s^4 \sigma_1 + 320 kd^3 s^3 \sigma_1 - 960 ka s^{11/2} \cosh(\sqrt{s}) + 1920 ka s^5 \sinh(\sqrt{s}) - 2880 kd s^5 \sinh(\sqrt{s}) \right. \\ \left. - 640 ka kd^2 s^3 \sigma_1 + 960 ka^2 kd s^4 \sigma_1 - 1920 ka kd s^{9/2} \cosh(\sqrt{s}) - \frac{170415 Pe^2 ka^2 s^{3/2} \sigma_2}{2} + 40950 Pe^2 ka^3 s^{3/2} \sigma_2 \right. \\ \left. - 20970 Pe^2 ka^2 s^{5/2} \sigma_2 - 960 Pe^2 ka^3 s^{5/2} \sigma_2 + 384 Pe^2 ka^3 s^{7/2} \sigma_2 + 2880 Pe^2 kd^3 \sqrt{s} \sigma_2 + 8640 Pe^2 kd^2 s^{3/2} \sigma_2 \right. \\ \left. + 3840 ka kd s^4 \sinh(\sqrt{s}) + 81810 Pe^2 ka^2 s^2 \sigma_1 - 2880 Pe^2 ka^2 s^3 \sigma_1 - 11070 Pe^2 ka^3 s^2 \sigma_1 + 1152 Pe^2 ka^2 s^4 \sigma_1 \right. \\ \left. - 2880 Pe^2 kd^2 s^2 \sigma_1 + 1152 Pe^2 kd^2 s^3 \sigma_1 + 384 Pe^2 kd^3 s^2 \sigma_1 - 38160 Pe^2 ka s^{5/2} \cosh(\sqrt{s}) \right. \\ \left. + 2880 Pe^2 ka s^{7/2} \cosh(\sqrt{s}) - 1152 Pe^2 ka s^{9/2} \cosh(\sqrt{s}) - 8640 Pe^2 kd s^{5/2} \cosh(\sqrt{s}) \right. \\ \left. + 129600 Pe^2 ka kd^2 \sinh(\sqrt{s}) + 129600 Pe^2 ka s^2 \sinh(\sqrt{s}) + 41760 Pe^2 ka s^3 \sinh(\sqrt{s}) - \frac{84105 Pe^2 ka^3 s \sinh(\sqrt{s})}{2} \right)$$

$$\begin{aligned}
& - 3840 \text{Pe}^2 \text{ka} s^4 \sinh(\sqrt{s}) + 25920 \text{Pe}^2 \text{kd} s^2 \sinh(\sqrt{s}) + 25920 \text{Pe}^2 \text{kd}^2 s \sinh(\sqrt{s}) + 8640 \text{Pe}^2 \text{kd} s^3 \sinh(\sqrt{s}) \\
& + 2880 \text{Pe}^2 \text{kd}^3 s \sinh(\sqrt{s}) - 3456 \text{Pe}^2 \text{kd} s^4 \sinh(\sqrt{s}) + 1920 \text{ka} \text{kd} s^{9/2} \sigma_2 - 960 \text{ka} \text{kd}^2 s^{7/2} \cosh(\sqrt{s}) \\
& + 1120 \text{ka}^2 \text{kd} s^{7/2} \cosh(\sqrt{s}) - 1280 \text{ka} \text{kd} s^4 \sigma_1 + 1920 \text{ka} \text{kd}^2 s^3 \sinh(\sqrt{s}) + 1600 \text{ka}^2 \text{kd} s^4 \sinh(\sqrt{s}) \\
& + 38160 \text{Pe}^2 \text{ka} s^{5/2} \sigma_2 - 2880 \text{Pe}^2 \text{ka} s^{7/2} \sigma_2 + 1152 \text{Pe}^2 \text{ka} s^{9/2} \sigma_2 + \frac{170415 \text{Pe}^2 \text{ka}^2 s^{3/2} \cosh(\sqrt{s})}{2} \\
& + 127260 \text{Pe}^2 \text{ka}^3 s^{3/2} \cosh(\sqrt{s}) + 29790 \text{Pe}^2 \text{ka}^2 s^{5/2} \cosh(\sqrt{s}) - 6600 \text{Pe}^2 \text{ka}^3 s^{5/2} \cosh(\sqrt{s}) \\
& - 3360 \text{Pe}^2 \text{ka}^2 s^{7/2} \cosh(\sqrt{s}) + 1344 \text{Pe}^2 \text{ka}^3 s^{7/2} \cosh(\sqrt{s}) + 320 \text{Pe}^2 \text{ka}^2 s^{9/2} \cosh(\sqrt{s}) + 8640 \text{Pe}^2 \text{kd} s^{5/2} \sigma_2 \\
& - 2880 \text{Pe}^2 \text{kd}^3 \sqrt{s} \cosh(\sqrt{s}) - 8640 \text{Pe}^2 \text{kd}^2 s^{3/2} \cosh(\sqrt{s}) - 43200 \text{Pe}^2 \text{ka} \text{kd}^2 \sigma_1 - 43200 \text{Pe}^2 \text{ka} s^2 \sigma_1 \\
& - 7200 \text{Pe}^2 \text{ka} s^3 \sigma_1 - \frac{84105 \text{Pe}^2 \text{ka}^3 s \sigma_1}{2} + 86580 \text{Pe}^2 \text{ka}^2 s^2 \sinh(\sqrt{s}) - 7080 \text{Pe}^2 \text{ka}^2 s^3 \sinh(\sqrt{s}) \\
& - 10890 \text{Pe}^2 \text{ka}^3 s^2 \sinh(\sqrt{s}) + 1344 \text{Pe}^2 \text{ka}^2 s^4 \sinh(\sqrt{s}) - 480 \text{Pe}^2 \text{ka}^3 s^3 \sinh(\sqrt{s}) + 320 \text{Pe}^2 \text{ka}^3 s^4 \sinh(\sqrt{s}) \\
& - 8640 \text{Pe}^2 \text{kd} s^2 \sigma_1 - 8640 \text{Pe}^2 \text{kd}^2 s \sigma_1 - 2880 \text{Pe}^2 \text{kd} s^3 \sigma_1 - 960 \text{Pe}^2 \text{kd}^3 s \sigma_1 + 1152 \text{Pe}^2 \text{kd} s^4 \sigma_1 \\
& + 8640 \text{Pe}^2 \text{kd}^2 s^2 \sinh(\sqrt{s}) - 3456 \text{Pe}^2 \text{kd}^2 s^3 \sinh(\sqrt{s}) - 1152 \text{Pe}^2 \text{kd}^3 s^2 \sinh(\sqrt{s}) + 960 \text{ka} \text{kd}^2 s^{7/2} \sigma_2 \\
& - 1120 \text{ka}^2 \text{kd} s^{7/2} \sigma_2 + 76320 \text{Pe}^2 \text{ka} \text{kd} s^{3/2} \sigma_2 - 5760 \text{Pe}^2 \text{ka} \text{kd} s^{5/2} \sigma_2 + 2304 \text{Pe}^2 \text{ka} \text{kd} s^{7/2} \sigma_2 \\
& - 38160 \text{Pe}^2 \text{ka} \text{kd}^2 \sqrt{s} \cosh(\sqrt{s}) + \frac{170415 \text{Pe}^2 \text{ka}^2 \text{kd} \sqrt{s} \cosh(\sqrt{s})}{2} + 2880 \text{Pe}^2 \text{ka} \text{kd}^2 s^{3/2} \cosh(\sqrt{s}) \\
& + 29790 \text{Pe}^2 \text{ka}^2 \text{kd} s^{3/2} \cosh(\sqrt{s}) - 1152 \text{Pe}^2 \text{ka} \text{kd}^2 s^{5/2} \cosh(\sqrt{s}) - 3360 \text{Pe}^2 \text{ka}^2 \text{kd} s^{5/2} \cosh(\sqrt{s}) \\
& + 320 \text{Pe}^2 \text{ka}^2 \text{kd} s^{7/2} \cosh(\sqrt{s}) - 14400 \text{Pe}^2 \text{ka} \text{kd} s^2 \sigma_1 - 7200 \text{Pe}^2 \text{ka} \text{kd}^2 s \sigma_1 + 81810 \text{Pe}^2 \text{ka}^2 \text{kd} s \sigma_1 \\
& - 3840 \text{Pe}^2 \text{ka} \text{kd}^2 s^2 \sinh(\sqrt{s}) - 7080 \text{Pe}^2 \text{ka}^2 \text{kd} s^2 \sinh(\sqrt{s}) + 1344 \text{Pe}^2 \text{ka}^2 \text{kd} s^3 \sinh(\sqrt{s}) \\
& + 259200 \text{Pe}^2 \text{ka} \text{kd} s \sinh(\sqrt{s}) + 38160 \text{Pe}^2 \text{ka} \text{kd}^2 \sqrt{s} \sigma_2 - \frac{170415 \text{Pe}^2 \text{ka}^2 \text{kd} \sqrt{s} \sigma_2}{2} - 2880 \text{Pe}^2 \text{ka} \text{kd}^2 s^{3/2} \sigma_2 \\
& - 20970 \text{Pe}^2 \text{ka}^2 \text{kd} s^{3/2} \sigma_2 + 1152 \text{Pe}^2 \text{ka} \text{kd}^2 s^{5/2} \sigma_2 - 2880 \text{Pe}^2 \text{ka}^2 \text{kd} s^2 \sigma_1 + 1152 \text{Pe}^2 \text{ka}^2 \text{kd} s^3 \sigma_1 \\
& - 76320 \text{Pe}^2 \text{ka} \text{kd} s^{3/2} \cosh(\sqrt{s}) + 5760 \text{Pe}^2 \text{ka} \text{kd} s^{5/2} \cosh(\sqrt{s}) - 2304 \text{Pe}^2 \text{ka} \text{kd} s^{7/2} \cosh(\sqrt{s}) \\
& - 86400 \text{Pe}^2 \text{ka} \text{kd} s \sigma_1 + 83520 \text{Pe}^2 \text{ka} \text{kd} s^2 \sinh(\sqrt{s}) + 41760 \text{Pe}^2 \text{ka} \text{kd}^2 s \sinh(\sqrt{s}) \\
& + 86580 \text{Pe}^2 \text{ka}^2 \text{kd} s \sinh(\sqrt{s}) - 7680 \text{Pe}^2 \text{ka} \text{kd} s^3 \sinh(\sqrt{s}) \bigg) \bigg/ \left( 640 s^5 \right. \\
& \left( \text{kd}^3 \sigma_3 + s^3 \sigma_3 + 3 \text{ka} s^{5/2} \sigma_4 + 3 \text{ka}^2 s^2 \sinh(\sqrt{s}) + 3 \text{kd} s^2 \sigma_3 + 3 \text{kd}^2 s \sigma_3 + \text{ka}^3 s^{3/2} \sigma_4 + 3 \text{ka}^2 s^2 \sigma_3 \right. \\
& - 3 \text{ka} s^{5/2} \cosh(\sqrt{s}) - 6 \text{ka} \text{kd} s^{3/2} \cosh(\sqrt{s}) + 3 \text{ka}^2 \text{kd} s \sinh(\sqrt{s}) - 3 \text{ka} \text{kd}^2 \sqrt{s} \cosh(\sqrt{s}) + 6 \text{ka} \text{kd} s^{3/2} \sigma_4 \\
& \left. \left. + 3 \text{ka}^2 \text{kd} s \sigma_3 + 3 \text{ka} \text{kd}^2 \sqrt{s} \sigma_4 \right) \right)
\end{aligned}$$

where

$$\sigma_1 = \sinh(3 \sqrt{s})$$

$$\sigma_2 = \cosh(3 \sqrt{s})$$

$$\sigma_3 = \sinh(\sqrt{s})^3$$

$$\sigma_4 = \cosh(\sqrt{s})^3$$

### coefficents (3.20)

(Note that the expressions for zeroth-order terms can't be recovered by setting  $p_k = 0$  in the solution for  $a_k, b_{k1}, b_{k2}, c_{k1}, c_{k2}, c_{k3}$  because in deriving the general solution, we have used  $ka/(p_k^2 - kd) = \tan(p_k)/p_k$ , which is not valid for  $p_k = 0$ .)

$$a_0 = \frac{kd}{ka + kd}$$

$$a_k = \frac{2 ka^2}{ka^2 p_k^2 + ka kd + ka p_k^2 + kd^2 - 2 kd p_k^2 + p_k^4}$$

$$b_0^{(1)} = \frac{2 Pe ka kd (6 ka + kd + 15)}{15 (ka + kd)^3}$$

$$b_k^{(1)} = \frac{- (Pe ka (-6 ka^5 p_k^6 + 15 ka^5 p_k^4 + 16 ka^4 kd p_k^4 + 51 ka^4 kd p_k^2 - 24 ka^4 p_k^6 + 30 ka^4 p_k^4 - 8 ka^3 kd^2 p_k^4 + 93 ka^3 kd^2 p_k^2 + 30 ka^3 kd^2 + 24 ka^3 kd p_k^6 - 96 ka^3 kd p_k^4 + 51 ka^3 kd p_k^2 - 16 ka^3 p_k^8 + 3 ka^3 p_k^6 + 15 ka^3 p_k^4 + 40 ka^2 kd^3 p_k^2 + 84 ka^2 kd^3 - 128 ka^2 kd^2 p_k^4 - 51 ka^2 kd^2 p_k^2 + 136 ka^2 kd p_k^6 - 54 ka^2 kd p_k^4 - 48 ka^2 p_k^8 + 21 ka^2 p_k^6 - 2 ka kd^4 p_k^2 + 78 ka kd^4 + 16 ka kd^3 p_k^4 - 222 ka kd^3 p_k^2 - 36 ka kd^2 p_k^6 + 198 ka kd^2 p_k^4 + 32 ka kd p_k^8 - 42 ka kd p_k^6 - 10 ka p_k^{10} - 12 ka p_k^8 + 24 kd^5 - 120 kd^4 p_k^2 + 240 kd^3 p_k^4 - 240 kd^2 p_k^6 + 120 kd p_k^8 - 24 p_k^{10}))}{(2 p_k^4 (ka^2 p_k^2 + ka kd + ka p_k^2 + kd^2 - 2 kd p_k^2 + p_k^4)^3)}$$

$$b_0^{(2)} = \frac{Pe kd^2}{(ka + kd)^2}$$

$$b_k^{(2)} = \frac{Pe ka^2 (4 ka^2 p_k^4 + 3 ka^2 p_k^2 - 3 ka kd + 3 ka p_k^2 + 4 kd^2 p_k^2 - 3 kd^2 - 8 kd p_k^4 + 6 kd p_k^2 + 4 p_k^6 - 3 p_k^4)}{2 p_k^2 (ka^2 p_k^2 + ka kd + ka p_k^2 + kd^2 - 2 kd p_k^2 + p_k^4)^2}$$

$$c_0^{(1)} = (kd (1824 Pe^2 ka^4 - 620 Pe^2 ka^3 kd + 8100 Pe^2 ka^3 - 418 Pe^2 ka^2 kd^2 - 5220 Pe^2 ka^2 kd + 9450 Pe^2 ka^2 - 80 Pe^2 ka kd^3 - 720 Pe^2 ka kd^2 - 9450 Pe^2 ka kd - 6 Pe^2 kd^4 + 2100 ka^4 + 4200 ka^3 kd + 6300 ka^3 + 2100 ka^2 kd^2 + 12600 ka^2 kd + 6300 ka kd^2))/(1575 (ka + kd)^5)$$

$$c_k^{(1)} = \frac{- (-280 Pe^2 ka^{10} p_k^{12} + 7530 Pe^2 ka^{10} p_k^{10} - 16875 Pe^2 ka^{10} p_k^8 + 2632 Pe^2 ka^9 kd p_k^{10} + 15810 Pe^2 ka^9 kd p_k^8 - 74925 Pe^2 ka^9 kd p_k^6 - 2240 Pe^2 ka^9 p_k^{12} + 45180 Pe^2 ka^9 p_k^{10} - 67500 Pe^2 ka^9 p_k^8 - 728 Pe^2 ka^8 kd^2 p_k^{10} + 42194 Pe^2 ka^8 kd^2 p_k^8 - 104415 Pe^2 ka^8 kd^2 p_k^6 - 129195 Pe^2 ka^8 kd^2 p_k^4 + 2240 Pe^2 ka^8 kd p_k^{12} - 63176 Pe^2 ka^8 kd p_k^{10} + 243210 Pe^2 ka^8 kd p_k^8 - 224775 Pe^2 ka^8 kd p_k^6 - 1352 Pe^2 ka^8 p_k^{14} + 26630 Pe^2 ka^8 p_k^{12} + 36135 Pe^2 ka^8 p_k^{10} - 101250 Pe^2 ka^8 p_k^8 + 10560 Pe^2 ka^7 kd^3 p_k^8 + 31032 Pe^2 ka^7 kd^3 p_k^6 - 357540 Pe^2 ka^7 kd^3 p_k^4 - 97605 Pe^2 ka^7 kd^3 p_k^2 - 30968 Pe^2 ka^7 kd^2 p_k^{10})}{(1575 (ka + kd)^5)}$$

$$\begin{aligned}
& + 126894 \text{ Pe}^2 \text{ ka}^7 \text{ kd}^2 p_k^8 + 259095 \text{ Pe}^2 \text{ ka}^7 \text{ kd}^2 p_k^6 - 258390 \text{ Pe}^2 \text{ ka}^7 \text{ kd}^2 p_k^4 + 30352 \text{ Pe}^2 \text{ ka}^7 \text{ kd} p_k^{12} \\
& - 302148 \text{ Pe}^2 \text{ ka}^7 \text{ kd} p_k^{10} + 401640 \text{ Pe}^2 \text{ ka}^7 \text{ kd} p_k^8 - 224775 \text{ Pe}^2 \text{ ka}^7 \text{ kd} p_k^6 - 9624 \text{ Pe}^2 \text{ ka}^7 p_k^{14} \\
& + 156030 \text{ Pe}^2 \text{ ka}^7 p_k^{12} - 87375 \text{ Pe}^2 \text{ ka}^7 p_k^{10} - 67500 \text{ Pe}^2 \text{ ka}^7 p_k^8 - 664 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^4 p_k^8 + 76490 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^4 p_k^6 \\
& - 292545 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^4 p_k^4 - 380835 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^4 p_k^2 - 27000 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^4 + 4368 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^3 p_k^{10} \\
& - 253884 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^3 p_k^8 + 1031610 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^3 p_k^6 - 78210 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^3 p_k^4 - 97605 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^3 p_k^2 \\
& - 9280 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^2 p_k^{12} + 309992 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^2 p_k^{10} - 981810 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^2 p_k^8 + 560160 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^2 p_k^6 \\
& - 129195 \text{ Pe}^2 \text{ ka}^6 \text{ kd}^2 p_k^4 + 8112 \text{ Pe}^2 \text{ ka}^6 \text{ kd} p_k^{14} - 165636 \text{ Pe}^2 \text{ ka}^6 \text{ kd} p_k^{12} + 67530 \text{ Pe}^2 \text{ ka}^6 \text{ kd} p_k^{10} \\
& + 136890 \text{ Pe}^2 \text{ ka}^6 \text{ kd} p_k^8 - 74925 \text{ Pe}^2 \text{ ka}^6 \text{ kd} p_k^6 - 2536 \text{ Pe}^2 \text{ ka}^6 p_k^{16} + 33038 \text{ Pe}^2 \text{ ka}^6 p_k^{14} + 182895 \text{ Pe}^2 \text{ ka}^6 p_k^{12} \\
& - 140085 \text{ Pe}^2 \text{ ka}^6 p_k^{10} - 16875 \text{ Pe}^2 \text{ ka}^6 p_k^8 + 15704 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^5 p_k^6 - 18978 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^5 p_k^4 \\
& - 551895 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^5 p_k^2 - 133920 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^5 - 78752 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^4 p_k^8 + 330660 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^4 p_k^6 \\
& + 1250160 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^4 p_k^4 - 147285 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^4 p_k^2 + 159120 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^3 p_k^{10} - 1061244 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^3 p_k^8 \\
& - 285450 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^3 p_k^6 + 176130 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^3 p_k^4 - 160608 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^2 p_k^{12} + 1403760 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^2 p_k^{10} \\
& - 958260 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^2 p_k^8 + 196650 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^2 p_k^6 + 80344 \text{ Pe}^2 \text{ ka}^5 \text{ kd} p_k^{14} - 851538 \text{ Pe}^2 \text{ ka}^5 \text{ kd} p_k^{12} \\
& + 531705 \text{ Pe}^2 \text{ ka}^5 \text{ kd} p_k^{10} - 37350 \text{ Pe}^2 \text{ ka}^5 \text{ kd} p_k^8 - 15808 \text{ Pe}^2 \text{ ka}^5 p_k^{16} + 197340 \text{ Pe}^2 \text{ ka}^5 p_k^{14} \\
& + 13740 \text{ Pe}^2 \text{ ka}^5 p_k^{12} - 54225 \text{ Pe}^2 \text{ ka}^5 p_k^{10} - 264 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^6 p_k^6 + 55446 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^6 p_k^4 \\
& - 344325 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^6 p_k^2 - 267120 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^6 + 2656 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^5 p_k^8 - 290352 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^5 p_k^6 \\
& + 1660530 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^5 p_k^4 + 374895 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^5 p_k^2 - 10120 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^4 p_k^{10} + 620502 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^4 p_k^8 \\
& - 2988345 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^4 p_k^6 + 346545 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^4 p_k^4 + 19200 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^3 p_k^{12} - 688752 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^3 p_k^{10} \\
& + 2263140 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^3 p_k^8 - 604890 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^3 p_k^6 - 19480 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^2 p_k^{14} + 415074 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^2 p_k^{12} \\
& - 292095 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^2 p_k^{10} - 35550 \text{ Pe}^2 \text{ ka}^4 \text{ kd}^2 p_k^8 + 10144 \text{ Pe}^2 \text{ ka}^4 \text{ kd} p_k^{16} - 126816 \text{ Pe}^2 \text{ ka}^4 \text{ kd} p_k^{14} \\
& - 488550 \text{ Pe}^2 \text{ ka}^4 \text{ kd} p_k^{12} + 227835 \text{ Pe}^2 \text{ ka}^4 \text{ kd} p_k^{10} - 2136 \text{ Pe}^2 \text{ ka}^4 p_k^{18} + 14898 \text{ Pe}^2 \text{ ka}^4 p_k^{16} \\
& + 189645 \text{ Pe}^2 \text{ ka}^4 p_k^{14} - 41715 \text{ Pe}^2 \text{ ka}^4 p_k^{12} + 10176 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^7 p_k^4 - 65880 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^7 p_k^2 \\
& - 269280 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^7 - 72744 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^6 p_k^6 + 527130 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^6 p_k^4 + 1046745 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^6 p_k^2 \\
& + 223824 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^5 p_k^8 - 1752420 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^5 p_k^6 - 1276560 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^5 p_k^4 - 383160 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^4 p_k^{10} \\
& + 3163350 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^4 p_k^8 + 58005 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^4 p_k^6 + 393120 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^3 p_k^{12} - 3366000 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^3 p_k^{10} \\
& + 1023480 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^3 p_k^8 - 241176 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^2 p_k^{14} + 2118630 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^2 p_k^{12} - 699165 \text{ Pe}^2 \text{ ka}^3 \text{ kd}^2 p_k^{10} \\
& + 81744 \text{ Pe}^2 \text{ ka}^3 \text{ kd} p_k^{16} - 732180 \text{ Pe}^2 \text{ ka}^3 \text{ kd} p_k^{14} + 83160 \text{ Pe}^2 \text{ ka}^3 \text{ kd} p_k^{12} - 11784 \text{ Pe}^2 \text{ ka}^3 p_k^{18} \\
& + 107370 \text{ Pe}^2 \text{ ka}^3 p_k^{16} + 33615 \text{ Pe}^2 \text{ ka}^3 p_k^{14} - 48 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^8 p_k^4 + 12180 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^8 p_k^2 - 139320 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^8 \\
& + 528 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^7 p_k^6 - 85980 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^7 p_k^4 + 882090 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^7 p_k^2 - 2832 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^6 p_k^8 \\
& + 259620 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^6 p_k^6 - 2307060 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^6 p_k^4 + 8592 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^5 p_k^{10} - 434220 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^5 p_k^8
\end{aligned}$$

$$\begin{aligned}
& + 3120390 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^5 p_k^6 - 15600 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^4 p_k^{12} + 433500 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^4 p_k^{10} - 2116800 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^4 p_k^8 \\
& + 17328 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^3 p_k^{14} - 256980 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^3 p_k^{12} + 333270 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^3 p_k^{10} - 11568 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^2 p_k^{16} \\
& + 82380 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^2 p_k^{14} + 480060 \text{ Pe}^2 \text{ ka}^2 \text{ kd}^2 p_k^{12} + 4272 \text{ Pe}^2 \text{ ka}^2 \text{ kd} p_k^{18} - 10020 \text{ Pe}^2 \text{ ka}^2 \text{ kd} p_k^{16} \\
& - 312390 \text{ Pe}^2 \text{ ka}^2 \text{ kd} p_k^{14} - 672 \text{ Pe}^2 \text{ ka}^2 p_k^{20} - 480 \text{ Pe}^2 \text{ ka}^2 p_k^{18} + 59760 \text{ Pe}^2 \text{ ka}^2 p_k^{16} + 2400 \text{ Pe}^2 \text{ ka} \text{ kd}^9 p_k^2 \\
& - 31680 \text{ Pe}^2 \text{ ka} \text{ kd}^9 - 22560 \text{ Pe}^2 \text{ ka} \text{ kd}^8 p_k^4 + 274320 \text{ Pe}^2 \text{ ka} \text{ kd}^8 p_k^2 + 94080 \text{ Pe}^2 \text{ ka} \text{ kd}^7 p_k^6 \\
& - 1054080 \text{ Pe}^2 \text{ ka} \text{ kd}^7 p_k^4 - 228480 \text{ Pe}^2 \text{ ka} \text{ kd}^6 p_k^8 + 2358720 \text{ Pe}^2 \text{ ka} \text{ kd}^6 p_k^6 + 356160 \text{ Pe}^2 \text{ ka} \text{ kd}^5 p_k^{10} \\
& - 3386880 \text{ Pe}^2 \text{ ka} \text{ kd}^5 p_k^8 - 369600 \text{ Pe}^2 \text{ ka} \text{ kd}^4 p_k^{12} + 3235680 \text{ Pe}^2 \text{ ka} \text{ kd}^4 p_k^{10} + 255360 \text{ Pe}^2 \text{ ka} \text{ kd}^3 p_k^{14} \\
& - 2056320 \text{ Pe}^2 \text{ ka} \text{ kd}^3 p_k^{12} - 113280 \text{ Pe}^2 \text{ ka} \text{ kd}^2 p_k^{16} + 838080 \text{ Pe}^2 \text{ ka} \text{ kd}^2 p_k^{14} + 29280 \text{ Pe}^2 \text{ ka} \text{ kd} p_k^{18} \\
& - 198720 \text{ Pe}^2 \text{ ka} \text{ kd} p_k^{16} - 3360 \text{ Pe}^2 \text{ ka} p_k^{20} + 20880 \text{ Pe}^2 \text{ ka} p_k^{18} - 1440 \text{ Pe}^2 \text{ kd}^{10} + 14400 \text{ Pe}^2 \text{ kd}^9 p_k^2 \\
& - 64800 \text{ Pe}^2 \text{ kd}^8 p_k^4 + 172800 \text{ Pe}^2 \text{ kd}^7 p_k^6 - 302400 \text{ Pe}^2 \text{ kd}^6 p_k^8 + 362880 \text{ Pe}^2 \text{ kd}^5 p_k^{10} - 302400 \text{ Pe}^2 \text{ kd}^4 p_k^{12} \\
& + 172800 \text{ Pe}^2 \text{ kd}^3 p_k^{14} - 64800 \text{ Pe}^2 \text{ kd}^2 p_k^{16} + 14400 \text{ Pe}^2 \text{ kd} p_k^{18} - 1440 \text{ Pe}^2 p_k^{20} + 800 \text{ ka}^9 \text{ kd} p_k^{12} \\
& + 320 \text{ ka}^8 \text{ kd}^2 p_k^{12} + 2080 \text{ ka}^8 \text{ kd}^2 p_k^{10} - 320 \text{ ka}^8 \text{ kd} p_k^{14} + 2400 \text{ ka}^8 \text{ kd} p_k^{12} + 3040 \text{ ka}^7 \text{ kd}^3 p_k^{10} \\
& + 1760 \text{ ka}^7 \text{ kd}^3 p_k^8 - 4800 \text{ ka}^7 \text{ kd}^2 p_k^{12} + 4160 \text{ ka}^7 \text{ kd}^2 p_k^{10} + 1760 \text{ ka}^7 \text{ kd} p_k^{14} + 2400 \text{ ka}^7 \text{ kd} p_k^{12} \\
& + 960 \text{ ka}^6 \text{ kd}^4 p_k^{10} + 4480 \text{ ka}^6 \text{ kd}^4 p_k^8 + 480 \text{ ka}^6 \text{ kd}^4 p_k^6 - 2880 \text{ ka}^6 \text{ kd}^3 p_k^{12} - 3200 \text{ ka}^6 \text{ kd}^3 p_k^{10} \\
& + 1760 \text{ ka}^6 \text{ kd}^3 p_k^8 + 2880 \text{ ka}^6 \text{ kd}^2 p_k^{14} - 5760 \text{ ka}^6 \text{ kd}^2 p_k^{12} + 2080 \text{ ka}^6 \text{ kd}^2 p_k^{10} - 960 \text{ ka}^6 \text{ kd} p_k^{16} \\
& + 4480 \text{ ka}^6 \text{ kd} p_k^{14} + 800 \text{ ka}^6 \text{ kd} p_k^{12} + 3680 \text{ ka}^5 \text{ kd}^5 p_k^8 + 1760 \text{ ka}^5 \text{ kd}^5 p_k^6 - 12160 \text{ ka}^5 \text{ kd}^4 p_k^{10} \\
& + 640 \text{ ka}^5 \text{ kd}^4 p_k^8 + 14400 \text{ ka}^5 \text{ kd}^3 p_k^{12} - 4160 \text{ ka}^5 \text{ kd}^3 p_k^{10} - 7040 \text{ ka}^5 \text{ kd}^2 p_k^{14} - 640 \text{ ka}^5 \text{ kd}^2 p_k^{12} \\
& + 1120 \text{ ka}^5 \text{ kd} p_k^{16} + 2400 \text{ ka}^5 \text{ kd} p_k^{14} + 960 \text{ ka}^4 \text{ kd}^6 p_k^8 + 2400 \text{ ka}^4 \text{ kd}^6 p_k^6 - 4800 \text{ ka}^4 \text{ kd}^5 p_k^{10} \\
& - 6240 \text{ ka}^4 \text{ kd}^5 p_k^8 + 9600 \text{ ka}^4 \text{ kd}^4 p_k^{12} + 2240 \text{ ka}^4 \text{ kd}^4 p_k^{10} - 9600 \text{ ka}^4 \text{ kd}^3 p_k^{14} + 6720 \text{ ka}^4 \text{ kd}^3 p_k^{12} \\
& + 4800 \text{ ka}^4 \text{ kd}^2 p_k^{16} - 7200 \text{ ka}^4 \text{ kd}^2 p_k^{14} - 960 \text{ ka}^4 \text{ kd} p_k^{18} + 2080 \text{ ka}^4 \text{ kd} p_k^{16} + 1440 \text{ ka}^3 \text{ kd}^7 p_k^6 \\
& - 7360 \text{ ka}^3 \text{ kd}^6 p_k^8 + 15200 \text{ ka}^3 \text{ kd}^5 p_k^{10} - 16000 \text{ ka}^3 \text{ kd}^4 p_k^{12} + 8800 \text{ ka}^3 \text{ kd}^3 p_k^{14} - 2240 \text{ ka}^3 \text{ kd}^2 p_k^{16} \\
& + 160 \text{ ka}^3 \text{ kd} p_k^{18} + 320 \text{ ka}^2 \text{ kd}^8 p_k^6 - 2240 \text{ ka}^2 \text{ kd}^7 p_k^8 + 6720 \text{ ka}^2 \text{ kd}^6 p_k^{10} - 11200 \text{ ka}^2 \text{ kd}^5 p_k^{12} \\
& + 11200 \text{ ka}^2 \text{ kd}^4 p_k^{14} - 6720 \text{ ka}^2 \text{ kd}^3 p_k^{16} + 2240 \text{ ka}^2 \text{ kd}^2 p_k^{18} - 320 \text{ ka}^2 \text{ kd} p_k^{20}) / (40 p_k^8 \\
& (\text{ka}^2 p_k^2 + \text{ka} \text{ kd} + \text{ka} p_k^2 + \text{kd}^2 - 2 \text{ kd} p_k^2 + p_k^4)^5)
\end{aligned}$$

$$c_0^{(2)} = \frac{2 \text{ kd}^2 (135 \text{ Pe}^2 \text{ ka}^2 + 32 \text{ Pe}^2 \text{ ka} \text{ kd} + 315 \text{ Pe}^2 \text{ ka} + 2 \text{ Pe}^2 \text{ kd}^2 + 105 \text{ ka}^2 + 210 \text{ ka} \text{ kd} + 105 \text{ kd}^2)}{105 (\text{ka} + \text{kd})^4}$$

$$\begin{aligned}
c_k^{(2)} = & (\text{ka} (232 \text{ Pe}^2 \text{ ka}^7 p_k^{10} - 270 \text{ Pe}^2 \text{ ka}^7 p_k^8 - 765 \text{ Pe}^2 \text{ ka}^7 p_k^6 - 776 \text{ Pe}^2 \text{ ka}^6 \text{ kd} p_k^8 - 3450 \text{ Pe}^2 \text{ ka}^6 \text{ kd} p_k^6 \\
& - 1755 \text{ Pe}^2 \text{ ka}^6 \text{ kd} p_k^4 + 904 \text{ Pe}^2 \text{ ka}^6 p_k^{10} + 450 \text{ Pe}^2 \text{ ka}^6 p_k^8 - 2295 \text{ Pe}^2 \text{ ka}^6 p_k^6 + 536 \text{ Pe}^2 \text{ ka}^5 \text{ kd}^2 p_k^8
\end{aligned}$$

$$\begin{aligned}
& -4458 \text{Pe}^2 \text{ka}^5 \text{kd}^2 p_k^6 - 5025 \text{Pe}^2 \text{ka}^5 \text{kd}^2 p_k^4 + 1035 \text{Pe}^2 \text{ka}^5 \text{kd}^2 p_k^2 - 1392 \text{Pe}^2 \text{ka}^5 \text{kd} p_k^{10} \\
& + 4404 \text{Pe}^2 \text{ka}^5 \text{kd} p_k^8 - 210 \text{Pe}^2 \text{ka}^5 \text{kd} p_k^6 - 3510 \text{Pe}^2 \text{ka}^5 \text{kd} p_k^4 + 856 \text{Pe}^2 \text{ka}^5 p_k^{12} - 138 \text{Pe}^2 \text{ka}^5 p_k^{10} \\
& + 1035 \text{Pe}^2 \text{ka}^5 p_k^8 - 2295 \text{Pe}^2 \text{ka}^5 p_k^6 - 2432 \text{Pe}^2 \text{ka}^4 \text{kd}^3 p_k^6 - 8160 \text{Pe}^2 \text{ka}^4 \text{kd}^3 p_k^4 + 1980 \text{Pe}^2 \text{ka}^4 \text{kd}^3 p_k^2 \\
& + 1485 \text{Pe}^2 \text{ka}^4 \text{kd}^3 + 7872 \text{Pe}^2 \text{ka}^4 \text{kd}^2 p_k^8 + 12720 \text{Pe}^2 \text{ka}^4 \text{kd}^2 p_k^6 - 9540 \text{Pe}^2 \text{ka}^4 \text{kd}^2 p_k^4 \\
& + 1035 \text{Pe}^2 \text{ka}^4 \text{kd}^2 p_k^2 - 8128 \text{Pe}^2 \text{ka}^4 \text{kd} p_k^{10} - 5280 \text{Pe}^2 \text{ka}^4 \text{kd} p_k^8 + 7920 \text{Pe}^2 \text{ka}^4 \text{kd} p_k^6 \\
& - 1755 \text{Pe}^2 \text{ka}^4 \text{kd} p_k^4 + 2688 \text{Pe}^2 \text{ka}^4 p_k^{12} + 720 \text{Pe}^2 \text{ka}^4 p_k^{10} - 360 \text{Pe}^2 \text{ka}^4 p_k^8 - 765 \text{Pe}^2 \text{ka}^4 p_k^6 \\
& + 376 \text{Pe}^2 \text{ka}^3 \text{kd}^4 p_k^6 - 7578 \text{Pe}^2 \text{ka}^3 \text{kd}^4 p_k^4 - 615 \text{Pe}^2 \text{ka}^3 \text{kd}^4 p_k^2 + 5175 \text{Pe}^2 \text{ka}^3 \text{kd}^4 - 2144 \text{Pe}^2 \text{ka}^3 \text{kd}^3 p_k^8 \\
& + 22440 \text{Pe}^2 \text{ka}^3 \text{kd}^3 p_k^6 - 5100 \text{Pe}^2 \text{ka}^3 \text{kd}^3 p_k^4 - 7020 \text{Pe}^2 \text{ka}^3 \text{kd}^3 p_k^2 + 4176 \text{Pe}^2 \text{ka}^3 \text{kd}^2 p_k^{10} \\
& - 22044 \text{Pe}^2 \text{ka}^3 \text{kd}^2 p_k^8 + 14790 \text{Pe}^2 \text{ka}^3 \text{kd}^2 p_k^6 - 2160 \text{Pe}^2 \text{ka}^3 \text{kd}^2 p_k^4 - 3424 \text{Pe}^2 \text{ka}^3 \text{kd} p_k^{12} \\
& + 7080 \text{Pe}^2 \text{ka}^3 \text{kd} p_k^{10} - 11820 \text{Pe}^2 \text{ka}^3 \text{kd} p_k^8 + 4680 \text{Pe}^2 \text{ka}^3 \text{kd} p_k^6 + 1016 \text{Pe}^2 \text{ka}^3 p_k^{14} + 102 \text{Pe}^2 \text{ka}^3 p_k^{12} \\
& + 2745 \text{Pe}^2 \text{ka}^3 p_k^{10} - 675 \text{Pe}^2 \text{ka}^3 p_k^8 - 2616 \text{Pe}^2 \text{ka}^2 \text{kd}^5 p_k^4 - 3990 \text{Pe}^2 \text{ka}^2 \text{kd}^5 p_k^2 + 6615 \text{Pe}^2 \text{ka}^2 \text{kd}^5 \\
& + 13528 \text{Pe}^2 \text{ka}^2 \text{kd}^4 p_k^6 + 11190 \text{Pe}^2 \text{ka}^2 \text{kd}^4 p_k^4 - 22185 \text{Pe}^2 \text{ka}^2 \text{kd}^4 p_k^2 - 27632 \text{Pe}^2 \text{ka}^2 \text{kd}^3 p_k^8 \\
& - 9180 \text{Pe}^2 \text{ka}^2 \text{kd}^3 p_k^6 + 25650 \text{Pe}^2 \text{ka}^2 \text{kd}^3 p_k^4 + 27888 \text{Pe}^2 \text{ka}^2 \text{kd}^2 p_k^{10} + 300 \text{Pe}^2 \text{ka}^2 \text{kd}^2 p_k^8 \\
& - 9990 \text{Pe}^2 \text{ka}^2 \text{kd}^2 p_k^6 - 13912 \text{Pe}^2 \text{ka}^2 \text{kd} p_k^{12} + 2130 \text{Pe}^2 \text{ka}^2 \text{kd} p_k^{10} - 1305 \text{Pe}^2 \text{ka}^2 \text{kd} p_k^8 \\
& + 2744 \text{Pe}^2 \text{ka}^2 p_k^{14} - 450 \text{Pe}^2 \text{ka}^2 p_k^{12} + 1215 \text{Pe}^2 \text{ka}^2 p_k^{10} + 72 \text{Pe}^2 \text{ka} \text{kd}^6 p_k^4 - 3390 \text{Pe}^2 \text{ka} \text{kd}^6 p_k^2 \\
& + 3645 \text{Pe}^2 \text{ka} \text{kd}^6 - 752 \text{Pe}^2 \text{ka} \text{kd}^5 p_k^6 + 16980 \text{Pe}^2 \text{ka} \text{kd}^5 p_k^4 - 19170 \text{Pe}^2 \text{ka} \text{kd}^5 p_k^2 + 2680 \text{Pe}^2 \text{ka} \text{kd}^4 p_k^8 \\
& - 34050 \text{Pe}^2 \text{ka} \text{kd}^4 p_k^6 + 41175 \text{Pe}^2 \text{ka} \text{kd}^4 p_k^4 - 4640 \text{Pe}^2 \text{ka} \text{kd}^3 p_k^{10} + 34200 \text{Pe}^2 \text{ka} \text{kd}^3 p_k^8 \\
& - 45900 \text{Pe}^2 \text{ka} \text{kd}^3 p_k^6 + 4280 \text{Pe}^2 \text{ka} \text{kd}^2 p_k^{12} - 17250 \text{Pe}^2 \text{ka} \text{kd}^2 p_k^{10} + 27675 \text{Pe}^2 \text{ka} \text{kd}^2 p_k^8 \\
& - 2032 \text{Pe}^2 \text{ka} \text{kd} p_k^{14} + 3540 \text{Pe}^2 \text{ka} \text{kd} p_k^{12} - 8370 \text{Pe}^2 \text{ka} \text{kd} p_k^{10} + 392 \text{Pe}^2 \text{ka} p_k^{16} - 30 \text{Pe}^2 \text{ka} p_k^{14} \\
& + 945 \text{Pe}^2 \text{ka} p_k^{12} - 960 \text{Pe}^2 \text{kd}^7 p_k^2 + 720 \text{Pe}^2 \text{kd}^7 + 6720 \text{Pe}^2 \text{kd}^6 p_k^4 - 5040 \text{Pe}^2 \text{kd}^6 p_k^2 - 20160 \text{Pe}^2 \text{kd}^5 p_k^6 \\
& + 15120 \text{Pe}^2 \text{kd}^5 p_k^4 + 33600 \text{Pe}^2 \text{kd}^4 p_k^8 - 25200 \text{Pe}^2 \text{kd}^4 p_k^6 - 33600 \text{Pe}^2 \text{kd}^3 p_k^{10} + 25200 \text{Pe}^2 \text{kd}^3 p_k^8 \\
& + 20160 \text{Pe}^2 \text{kd}^2 p_k^{12} - 15120 \text{Pe}^2 \text{kd}^2 p_k^{10} - 6720 \text{Pe}^2 \text{kd} p_k^{14} + 5040 \text{Pe}^2 \text{kd} p_k^{12} + 960 \text{Pe}^2 p_k^{16} - 720 \text{Pe}^2 p_k^{14} \\
& + 160 \text{ka}^7 p_k^{12} + 160 \text{ka}^6 \text{kd} p_k^{10} + 480 \text{ka}^6 p_k^{12} + 480 \text{ka}^5 \text{kd}^2 p_k^{10} - 160 \text{ka}^5 \text{kd}^2 p_k^8 - 960 \text{ka}^5 \text{kd} p_k^{12} \\
& + 320 \text{ka}^5 \text{kd} p_k^{10} + 480 \text{ka}^5 p_k^{14} + 480 \text{ka}^5 p_k^{12} + 320 \text{ka}^4 \text{kd}^3 p_k^8 - 160 \text{ka}^4 \text{kd}^3 p_k^6 + 320 \text{ka}^4 \text{kd}^2 p_k^{10} \\
& - 160 \text{ka}^4 \text{kd}^2 p_k^8 - 1600 \text{ka}^4 \text{kd} p_k^{12} + 160 \text{ka}^4 \text{kd} p_k^{10} + 960 \text{ka}^4 p_k^{14} + 160 \text{ka}^4 p_k^{12} + 480 \text{ka}^3 \text{kd}^4 p_k^8 \\
& - 160 \text{ka}^3 \text{kd}^4 p_k^6 - 1920 \text{ka}^3 \text{kd}^3 p_k^{10} + 640 \text{ka}^3 \text{kd}^3 p_k^8 + 2880 \text{ka}^3 \text{kd}^2 p_k^{12} - 320 \text{ka}^3 \text{kd}^2 p_k^{10} \\
& - 1920 \text{ka}^3 \text{kd} p_k^{14} - 640 \text{ka}^3 \text{kd} p_k^{12} + 480 \text{ka}^3 p_k^{16} + 480 \text{ka}^3 p_k^{14} + 160 \text{ka}^2 \text{kd}^5 p_k^6 - 160 \text{ka}^2 \text{kd}^4 p_k^8 \\
& - 960 \text{ka}^2 \text{kd}^3 p_k^{10} + 2240 \text{ka}^2 \text{kd}^2 p_k^{12} - 1760 \text{ka}^2 \text{kd} p_k^{14} + 480 \text{ka}^2 p_k^{16} + 160 \text{ka} \text{kd}^6 p_k^6 - 960 \text{ka} \text{kd}^5 p_k^8 \\
& + 2400 \text{ka} \text{kd}^4 p_k^{10} - 3200 \text{ka} \text{kd}^3 p_k^{12} + 2400 \text{ka} \text{kd}^2 p_k^{14} - 960 \text{ka} \text{kd} p_k^{16} + 160 \text{ka} p_k^{18})) / (40 p_k^6 \\
& (\text{ka}^2 p_k^2 + \text{ka} \text{kd} + \text{ka} p_k^2 + \text{kd}^2 - 2 \text{kd} p_k^2 + p_k^4)^4)
\end{aligned}$$

$$c_0^{(3)} = \frac{Pe^2\,kd^3}{(ka+kd)^3}$$

$$c_k^{(3)} = \frac{Pe^2\,ka^2\,(4\,ka^2\,p_k^4+3\,ka^2\,p_k^2-3\,ka\,kd+3\,ka\,p_k^2+4\,kd^2\,p_k^2-3\,kd^2-8\,kd\,p_k^4+6\,kd\,p_k^2+4\,p_k^6-3\,p_k^4)^2}{8\,p_k^4\,(ka^2\,p_k^2+ka\,kd+ka\,p_k^2+kd^2-2\,kd\,p_k^2+p_k^4)^3}$$