

Appendix

Appendix B. Coefficients occurring in the linearized equations (59), (61), (66), (68), and (69)

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elliptic

$$a_{11} = -\epsilon \sqrt{T'} X_* h_3 \quad \square$$

$$a_{12} = c_1 - 2\theta_w \epsilon \sqrt{T'} h_3 \quad \square$$

$$a_{13} = \theta_w^2 \epsilon \sqrt{T'} h_3 + \frac{\theta_w \sin \phi \nu X_* f_2}{V} \frac{d\sigma'_c}{d\nu} \quad \square$$

$$a_{14} = \frac{12\epsilon \sqrt{T'} h'_2}{X_*} \quad \square$$

$$a_{15} = -\frac{6\theta_w \epsilon \sqrt{T'} h'_2}{X_*} + \frac{\nu}{V} (\alpha_0 - \alpha_1 + \sin \phi (f_0 - f_1 + \theta_w^2 f_2)) \frac{d\sigma'_c}{d\nu} \quad \square$$

$$a_{16} = \frac{6\epsilon \sqrt{T'} h'_2}{X_*^2} (V \theta_w - 2 \oint U \partial) + \frac{\nu}{X_*} (\alpha_0 - \alpha_1 + \sin \phi (f_0 - f_1 + \theta_w^2 f_2)) \frac{d\sigma'_c}{d\nu} \quad \square$$

$$a_{17} = \frac{6\epsilon \sqrt{T'} h'_2}{X_*} (2 \oint U \partial - V \theta_w) + (\sigma'_c + 2\nu \frac{d\sigma'_c}{d\nu}) (\alpha_1 - \alpha_0) \\ + \sin \phi (f_1 - f_0 - \theta_w^2 f_2) + \theta_w^2 \sin \phi \nu f_2 \frac{d\sigma'_c}{d\nu} \quad \square$$

$$b_{11} = -\epsilon \sqrt{T'} X_* h'_2 \quad \square$$

$$b_{12} = -\theta_w \epsilon \sqrt{T'} h'_2 - \frac{\epsilon T' \nu X_*}{V} \frac{dh_1}{d\nu} - \frac{\nu X_*}{V} (\bar{\alpha} - \sin \phi \bar{f}) \frac{d\sigma'_c}{d\nu} + c_1 \quad \square$$

$$b_{13} = \epsilon X_* h_1 \quad \square$$

$$b_{14} = -\frac{8\theta_w \epsilon \sqrt{T'} h'_2}{X_*} \quad \square$$

$$b_{15} = \frac{5\theta_w^2 \epsilon \sqrt{T'} h'_2}{X_*} + \frac{\theta_w \nu}{V} (\alpha_1 - \bar{\alpha} + \sin \phi (f_1 + \bar{f})) \frac{d\sigma'_c}{d\nu} - \frac{c_1}{V^2} \quad \square$$

$$b_{16} = 0 \quad \square$$

$$b_{17} = \frac{\theta_w \epsilon \sqrt{T'} h'_2}{X_*^2} (8 \oint U \partial - 5V \theta_w) + \frac{\theta_w \nu}{X_*} (\alpha_1 - \bar{\alpha} + \sin \phi (\bar{f} + f_1)) \frac{d\sigma'_c}{d\nu} \quad \square$$

$$b_{18} = -\theta_w \epsilon T' \nu \frac{dh_1}{d\nu} + \frac{\theta_w \epsilon \sqrt{T'} h'_2}{X_*} (5V \theta_w - 8 \oint U \partial) \\ + \theta_w \sigma'_c (\bar{\alpha} - \alpha_1 - \sin \phi (\bar{f} + f_1)) \quad \square$$

$T^{1/2}$ sh (num on)
 $X^{1/2}$, h

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(X)

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$$+ \theta_w \nu \frac{d\sigma'_c}{d\nu} (\bar{\alpha} - 2\alpha_1 - \sin \phi (\bar{f} + 2f_1)) + \frac{2c_1}{V} h$$

$c_{11} = -\epsilon \sqrt{T} X_* h_4 \quad \square$

$c_{12} = -\theta_w \epsilon \sqrt{T} h_4 + \left(\frac{3}{2}\right) c_1 h$

$c_{13} = \frac{16\sqrt{T} h_3}{105} \left(-16X_* \frac{d\langle U \rangle}{d\bar{Y}} + X_* \theta_w \frac{dV}{d\bar{Y}} \right) + \theta_w (11V \theta_w - 8 \langle U \rangle) \left(\begin{array}{c} \text{Small frac} \\ \times 4 \end{array} \right) \left(\begin{array}{c} \langle \rangle \\ \times 15 \end{array} \right)$

$c_{14} = T' X_* h_1 - 2\sqrt{T} \left(\bar{h}_2 V \theta_w + X_* h'_2 \frac{dV}{d\bar{Y}} \right)$
 $+ \frac{2\theta_w \sqrt{T} h_3}{105} \left(8X_* \frac{d\langle U \rangle}{d\bar{Y}} - 11\theta_w X_* \frac{dV}{d\bar{Y}} + \theta_w (47V \theta_w - 80 \langle U \rangle) \right)$

$c_{15} = \frac{64\sqrt{T} h'_2}{5X_*} (V \theta_w - 2 \langle U \rangle) + \frac{\theta_w^2 \sqrt{T} h_3}{105X_*} (928V \theta_w - 1408 \langle U \rangle)$

$c_{16} = \theta_w T' h_1 - T' \nu \left(\theta_w \frac{dh_1}{d\nu} + \frac{\sqrt{T} X_* dh_6}{V} \right)$
 $+ \frac{\theta_w \sqrt{T} h'_2}{5X_*} (64 \langle U \rangle - 42V \theta_w) + \frac{\theta_w^3 \sqrt{T} h_3}{105X_*} (928 \langle U \rangle - 646V \theta_w)$

$c_{17} = h_1 V \theta_w + \frac{3}{2} \sqrt{T} X_* h_6$

$c_{18} = -\frac{\theta_w T' V \nu}{X_*} \frac{dh_1}{d\nu} + T'^{3/2} \left(h_6 - \nu \frac{dh_6}{d\nu} \right)$
 $+ \frac{\sqrt{T} h'_2}{5X_*^2} (64 \langle U \rangle (\langle U \rangle - V \theta_w) + 21(V \theta_w)^2)$
 $+ \frac{\theta_w^2 \sqrt{T} h_3}{105X_*^2} (704 \langle U \rangle^2 - 928 \langle U \rangle V \theta_w + 323(V \theta_w)^2)$

$c_{19} = \frac{\sqrt{T} X_* h_3}{105} \left(128 \left(\frac{d\langle U \rangle}{d\bar{Y}} \right)^2 + 11 \left(\theta_w \frac{dV}{d\bar{Y}} \right)^2 \right.$
 $- 16 \theta_w \frac{d\langle U \rangle dV}{d\bar{Y} d\bar{Y}} \left. + \sqrt{T} X_* h'_2 \left(\frac{dV}{d\bar{Y}} \right)^2 + \theta_w T' V \left(2\nu \frac{dh_1}{d\nu} - h_1 \right) \right)$
 $+ X_* T'^{3/2} \left(2\nu \frac{dh_6}{d\nu} - \frac{3}{2} h_6 \right)$

$p_{11} = -\frac{1}{V^2}$

$p_{12} = \frac{2}{V}$

$a_{23} = \epsilon \sqrt{T} \left(\bar{h}_2 + \frac{\theta_w h_3}{V} (\langle U \rangle - V \theta_w) \right) + \frac{\theta_w \sin \phi X_* f_2}{V} \left(\sigma'_c + \nu \frac{d\sigma'_c}{d\nu} \right)$

$$\begin{aligned}
a_{24} &= \epsilon \sqrt{T'} h_3 \left(2\theta_w - \frac{\oint U \oint}{V} \right) - \frac{\sin \phi X_* f_2 \sigma'_c}{V} \\
a_{25} &= \frac{4\epsilon \sqrt{T'} h'_2}{X_*} \\
a_{26} &= \frac{\epsilon T' \nu dh_1}{V d\nu} + \frac{2\theta_w^2 \sin \phi f_2}{V} \sigma'_c + \frac{\nu}{V} (\alpha_0 + \sin \phi f_0) \frac{d\sigma'_c}{d\nu} \\
a_{27} &= \frac{-\epsilon \sqrt{T'} h'_2}{X_*} - \frac{\theta_w \sin \phi f_2}{V} \left(2\sigma'_c - \nu \frac{d\sigma'_c}{d\nu} \right) \\
a_{28} &= -\epsilon h_1 \\
a_{29} &= \frac{\epsilon T' \nu dh_1}{X_* d\nu} + \frac{\epsilon \sqrt{T'} h'_2}{X_*^2} (V \theta_w - 4 \langle U \rangle) + \frac{\nu}{X_*} (\alpha_0 + \sin \phi (f_0 + \theta_w^2 f_2)) \frac{d\sigma'_c}{d\nu} \\
a_{30} &= -2\epsilon T' \nu \frac{dh_1}{d\nu} + \frac{\epsilon \sqrt{T'} h'_2}{X_*} (4 \langle U \rangle - V \theta_w) - (\alpha_0 + \sin \phi (f_0 + \theta_w^2 f_2)) \sigma'_c \\
&\quad - (2\alpha_0 + \sin \phi (2f_0 + \theta_w^2 f_2)) \nu \frac{d\sigma'_c}{d\nu} \\
b_{23} &= -\epsilon \sqrt{T'} \bar{h}_2 \\
b_{25} &= -\frac{\theta_w \epsilon T' h_1}{V} - \frac{\theta_w}{V} (\bar{\alpha} - \sin \phi \bar{f}) \sigma'_c - \frac{c_1}{V^2} \\
b_{26} &= \frac{\epsilon T'}{V} (h_1 - \nu \frac{dh_1}{d\nu}) + \frac{(\bar{\alpha} - \sin \phi \bar{f})}{V} (\sigma'_c - \nu \frac{d\sigma'_c}{d\nu}) \\
b_{27} &= \theta_w \epsilon h_1 \\
b_{28} &= -\frac{\theta_w \epsilon T' \nu}{X_*} \frac{dh_1}{d\nu} - \frac{\theta_w \nu}{X_*} (\bar{\alpha} - \sin \phi \bar{f}) \frac{d\sigma'_c}{d\nu} \\
b_{29} &= \theta_w \epsilon T' \nu \frac{dh_1}{d\nu} + \theta_w (\sigma'_c + \nu \frac{d\sigma'_c}{d\nu}) (\bar{\alpha} - \sin \phi \bar{f}) + \frac{2c_1}{V} \\
c_{24} &= T' X_* h_1 - 2\sqrt{T'} (\bar{h}_2 V \theta_w + X_* h'_2 \frac{dV}{d\bar{Y}}) \\
c_{25} &= \frac{2\sqrt{T'} h_3}{105} (8X_* \frac{d \langle U \rangle}{d\bar{Y}} - 11X_* \theta_w \frac{dV}{d\bar{Y}} + \theta_w (47V \theta_w - 80 \langle U \rangle)) \\
c_{27} &= -T' \nu (\theta_w \frac{dh_1}{d\nu} + \frac{\sqrt{T'} X_*}{V} \frac{dh_6}{d\nu}) \\
c_{28} &= T' h_1 + \frac{\sqrt{T'} h'_2}{5X_*} (64 \langle U \rangle - 42V \theta_w) + \frac{\theta_w^2 \sqrt{T'} h_3}{105X_*} (928 \langle U \rangle - 646V \theta_w) \\
d_{21} &= -\epsilon \sqrt{T'} \bar{h}_2 \\
d_{22} &= \frac{8\epsilon \sqrt{T'} h'_2}{X_*}
\end{aligned}$$

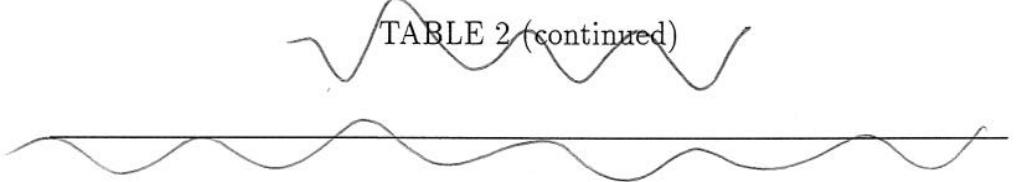
$$\begin{aligned}
d_{23} &= -\frac{\epsilon T' \nu}{V} \frac{dh_1}{d\nu} - \frac{\nu}{V} (\alpha_1 + \sin \phi f_1) \frac{d\sigma'_c}{d\nu} \\
d_{24} &= -\frac{5\epsilon \sqrt{T'} h'_2}{X_*} \\
d_{25} &= \epsilon h_1 \\
d_{26} &= -\frac{\epsilon T' \nu}{X_*} \frac{dh_1}{d\nu} + \frac{\epsilon \sqrt{T'} h'_2}{X_*^2} (5V \theta_w - 8 \langle U \rangle) - \frac{\nu}{X_*} (\alpha_1 + \sin \phi f_1) \frac{d\sigma'_c}{d\nu} \\
d_{27} &= 2\epsilon T' \nu \frac{dh_1}{d\nu} + \frac{\epsilon \sqrt{T'} h'_2}{X_*} (8 \langle U \rangle - 5V \theta_w) + (\alpha_1 + \sin \phi f_1) (\sigma'_c + 2\nu \frac{d\sigma'_c}{d\nu}) \\
p_{21} &= \frac{3}{2} c_1 \\
p_{22} &= \frac{T' \nu X_*}{V} \left(\frac{1}{V} \frac{dh_1}{d\nu} - \sqrt{T'} \frac{dh_6}{d\nu} \right) \\
p_{23} &= X_* \left(\frac{3}{2} \sqrt{T'} h_6 - \frac{h_1}{V} \right) \\
p_{24} &= T' \frac{3}{2} \left(h_6 - \nu \frac{dh_6}{d\nu} \right) + \frac{T'}{V} \left(\nu \frac{dh_1}{d\nu} - h_1 \right) - \frac{\sqrt{T'} h'_2}{V^2} \\
p_{25} &= \frac{T' X_*}{V} \left(h_1 - 2\nu \frac{dh_1}{d\nu} \right) + T'^{3/2} X_* \left(2\nu \frac{dh_6}{d\nu} - \frac{3}{2} h_6 \right)
\end{aligned}$$

TABLE 2. Coefficients occurring in the linearized equations (62)-(64), and (66). The constants a_{1j} and d_{2j} are defined in Appendix B.

$g_{21} = a_{11}$	$g_{22} = -\frac{a_{24}d_{21}}{d_{24}}$	$g_{23} = a_{12} - \frac{a_{24}d_{22}}{d_{24}}$
$g_{24} = a_{23} - \frac{d_{23}a_{24} + d_{21}a_{27}}{d_{24}}$	$g_{25} = -\frac{a_{24}d_{25}}{d_{24}}$	$g_{26} = -\frac{a_{24}d_{26}}{d_{24}}$
$g_{27} = a_{25} - \frac{a_{27}d_{22}}{d_{24}}$	$g_{28} = a_{26} - \frac{a_{27}d_{23}}{d_{24}}$	$g_{29} = a_{28} - \frac{a_{27}d_{25}}{d_{24}}$
$g_{20} = a_{29} - \frac{a_{27}d_{26}}{d_{24}}$	$h_{21} = 1 + \frac{a_{27} + k'a_{24}}{d_{24}}$	$h_{22} = a_{20} - \frac{a_{27}d_{27}}{d_{24}}$
$l_{21} = b_{11} - \frac{b_{23}d_{21}}{d_{24}}$	$l_{22} = -\frac{b_{23}d_{22}}{d_{24}}$	$l_{23} = b_{12} - \frac{b_{26}d_{21} + b_{23}d_{23}}{d_{24}}$
$l_{24} = b_{13} - \frac{b_{23}d_{25}}{d_{24}}$	$l_{25} = -\frac{b_{23}d_{26}}{d_{24}}$	$l_{26} = -\frac{b_{26}d_{22}}{d_{24}}$
$l_{27} = b_{25} - \frac{b_{26}d_{23}}{d_{24}}$	$l_{28} = b_{27} - \frac{b_{26}d_{25}}{d_{24}}$	$l_{29} = b_{28} - \frac{b_{26}d_{26}}{d_{24}}$
$l_{20} = \frac{b_{26} + k'b_{23}}{d_{24}} - \theta_w$	$h_{23} = b_{29} - \frac{b_{26}d_{27}}{d_{24}}$	

insert rest of
table that
appears on p 54

TABLE 2 (continued)



$$\begin{array}{lll}
 m_{21} = -\frac{c_{25}d_{21}}{d_{24}} & m_{22} = c_{11} & m_{23} = c_{13} - \frac{c_{25}d_{22}}{d_{24}} \\
 m_{24} = c_{24} - \frac{c_{25}d_{23} + c_{28}d_{21}}{d_{24}} & m_{25} = c_{12} - \frac{c_{25}d_{25}}{d_{24}} & m_{26} = -\frac{c_{25}d_{26}}{d_{24}} \\
 m_{27} = c_{15} - \frac{c_{28}d_{22}}{d_{24}} & m_{28} = c_{27} - \frac{c_{28}d_{23}}{d_{24}} & m_{29} = c_{17} - \frac{c_{28}d_{25}}{d_{24}} \\
 m_{20} = c_{18} - \frac{c_{28}d_{26}}{d_{24}} & h_{24} = \frac{c_{28} + k'c_{25}}{d_{24}} & h_{25} = c_{19} - \frac{c_{28}d_{27}}{d_{24}} \\
 \\
 n_{21} = \frac{d_{21}}{Vd_{24}} & n_{22} = \frac{d_{22}}{Vd_{24}} & n_{23} = \frac{\theta_w}{V} + \frac{d_{23}}{Vd_{24}} \\
 n_{24} = \frac{d_{25}}{Vd_{24}} & n_{25} = \frac{d_{26}}{Vd_{24}} & n_{26} = -\frac{1}{Vd_{24}} \\
 n_{27} = -\theta_w + \frac{d_{27}}{Vd_{24}} & &
 \end{array}$$


Combine with table on p 53